Virtual Diesel Particulate Filters: Simulation of the Structure, Exhaust Gas Flow and Particle Deposition

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Overview

1. Virtual Material Design Cycle
2. Virtual Filter Geometries
3. Simulation of Filtration Processes
   a) Modeling
   b) Simulation Results
   c) Software Tools
4. Summary and Future Developments
1. Virtual Material Design Cycle

Property Requirements Fulfilled?

Virtual Design Cycle

Selection of Media Types, Dimensions, etc.

Computation of Macroscopic Properties of the Filter

Computation of Microscopic Properties of the Filter Medium
2. Virtual Filter Geometries

Multilayer Virtual Nonwoven

- Stochastic generation of the structure with guaranteed adjustable properties, e.g.
  - Distribution of fiber diameters and cross sections
  - Fiber orientation
  - Porosity
  - Layer thickness
  - ...
- Stacking of layers with different parameters
- Use of highly flexible voxel meshes
2. Virtual Filter Geometries

**Virtual Sinter Structure I**

- Stochastic generation based on
  - Packings of spheres
  - Morphological operations (to generate sinter necks)

- Packings of spheres selected to match the initial grain size distribution of the sinter process

- Approach was applied in an industrial project when no tomographies were available due to
  - Too coarse resolution
  - Difficult preprocessing of samples
2. Virtual Filter Geometries

SEM image

Virtual Reconstruction
2. Virtual Filter Geometries

Quality Measures for Virtual Structures

- “The Eye”
- Porosity
- Cord length distributions: Virtual vs. real SEM cross sections
- Pore size analysis
- Flow properties, e.g. effective permeability or flow resistivity
- Filtration properties
- …

Effective Flow Permeability

<table>
<thead>
<tr>
<th>Measurement</th>
<th>Simulation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$5.9 \times 10^{-13} \text{ m}^2$</td>
<td>$5.1 \times 10^{-13} \text{ m}^2$</td>
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~ 14.5% deviation!
3. Simulation of Filtration Processes

A) Modeling
- Flow
- Particle Transport
- Particle Deposition

B) Simulation Results
- Design of Diesel Particulate Filters

C) Software Tools
- GEO DICT
- FILTER DICT
3. Simulation of Filtration Processes - Modeling

Flow simulation is based on Navier-Stokes-Brinkmann equations

\[-\mu \Delta \vec{u} + \nabla \vec{u} \cdot \vec{u} + \kappa^{-1} \vec{u} + \nabla p = \vec{f},\]  
(momentum balance)

\[\nabla \cdot \vec{u} = 0,\]  
(continuity)

+ boundary conditions,

\[\vec{u}: \text{ velocity}\]
\[p: \text{ pressure}\]
\[\vec{f}: \text{ force (density)}\]
\[\mu: \text{ fluid viscosity}\]
\[\kappa: \text{ permeability of porous voxel}\]

Remark

• convective term optional -> fast flow
• Brinkmann term optional -> subgrid particle deposition and effective porous media
3. Simulation of Filtration Processes - Modeling

Lagrangian Particle Transport

\[
\frac{d\vec{x}}{dt} = \vec{v} \\
\frac{d\vec{v}}{dt} = -\gamma (\vec{v}(\vec{x}) - \vec{u}(\vec{x})) + \frac{Q E_0(\vec{x})}{m} + \sigma \frac{d\vec{W}(t)}{dt} \\
\gamma = 6\pi \rho \mu \frac{R}{m} \\
\sigma^2 = \frac{2k_B T \gamma}{m} \\
\langle dW_i(t), dW_j(t) \rangle = \delta_{ij} dt
\]

Particle Deposition

- Collision handling
- Adhesion model

Modification of Geometry

- Solid deposition model (particles resolved by voxels)
- Porous deposition model (small particles)

\begin{align*}
t & : \text{time} \\
\vec{x} & : \text{particle position} \\
\vec{v} & : \text{particle velocity} \\
R & : \text{particle radius} \\
m & : \text{particle mass} \\
Q & : \text{particle charge} \\
T & : \text{temperature} \\
k_B & : \text{Boltzmann constant} \\
d\vec{W}(t) & : \text{3d probability measure} \\
E_0 & : \text{electrical field} \\
\vec{v}_0 & : \text{fluid velocity} \\
\rho & : \text{fluid density} \\
\mu & : \text{fluid viscosity}
\end{align*}
3. Simulation of Filtration Processes - Modeling

Model inherent filtration mechanisms

A) Barrier effect    D) Sieving
B) Inertia effect    E) Electrostatic attraction
C) Diffusion effect (Brownian motion)
3. Simulation of Filtration Processes - Modeling

1. Determine parameters of the real filter
2. Generate 3d virtual structure
3. Compute flow field
4. Compute particle transport and deposition
5. Modify geometry
6. Compute filter efficiency, pressure drop, lifetime
7. New material parameters
3. Simulation of Filtration Processes - Simulation Results

Design study of a Diesel particulate filter

- What is the effect of an additional fibrous layer on top of a sintered substrate?

- Soot particles (~80nm) are much smaller than voxels (1µm) -> porous deposition model

- Navier-Stokes-Brinkmann model to handle free and porous flow

- Permeability and maximum degree of filling of porous voxels are determined by high resolution single fiber experiments

- Some hundreds of millions of particles are needed for a lifetime computation
3. Simulation of Filtration Processes – Simulation Results

- Single Fiber Nanosimulation
- Soot Layer Cut-Out
- Effective Microproperties

- Porosity = 85 %
- Permeability = 1e-15 m^2
3. Simulation of Filtration Processes - Simulation Results

Soot Deposition
3. Simulation of Filtration Processes - Simulation Results

![Graph showing pressure drop evolution with deposited soot for depth filtration and surface filtration, comparing substrates with and without a fiber layer.](image)

**Pressure Drop Evolution**

- **Deposited Soot [g/m^2]**
- **Pressure Drop [Pa]**

**Comparison**
- **Depth Filtration**
- **Surface Filtration**

**Graph Notes**
- **Substrate only**
- **Substrate with fiber layer**

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3. Simulation of Filtration Processes – Simulation Tools

- **GeoFiber**: Nonwoven generator
- **GeoSinter**: Sinter structure generator
- **GeoProcess / GeoLayer**: structure processing
- **FilterDict**: Particle filtration
- **SatuDict**: pressure-saturation relations
- **PoroDict**: Pore size distributions
4. Summary and Future Developments

Today

• Virtual structure generation
• Effective flow properties
• Filter efficiencies
• Filter lifetime
• Coupling of scales
• All methods are available by software tools

Tomorrow (DPF related)

• Extending virtual structure generation
• Coupling of length scales
• General particle shapes
• Fractional Slip Phenomena

Tomorrow (in general)

• Standard Tests
• Particle re-entry into fluid flow
• Electrostatic effects
• Particle-particle interaction
• Fluid-structure interaction

Fraunhofer Institute for Techno- and Wirtschaftsmathematik
GeoDict development teams

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Software for Generation, Simulation, Visualization:

GEODICT

www.geodict.com

Thank you for attending this presentation.