
Virtual Diesel Particulate Filters: Simulation of the Structure, Exhaust Gas Flow and Particle Deposition

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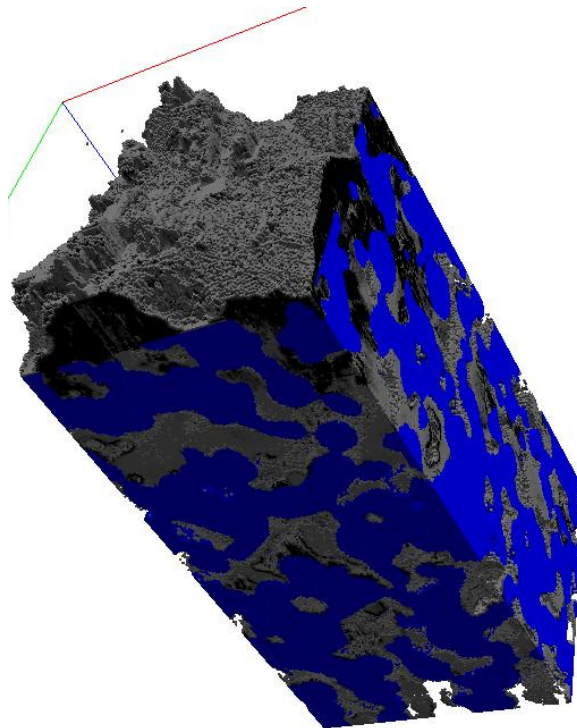
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3rd AFS Conference "Emission Solutions in
Transportations"

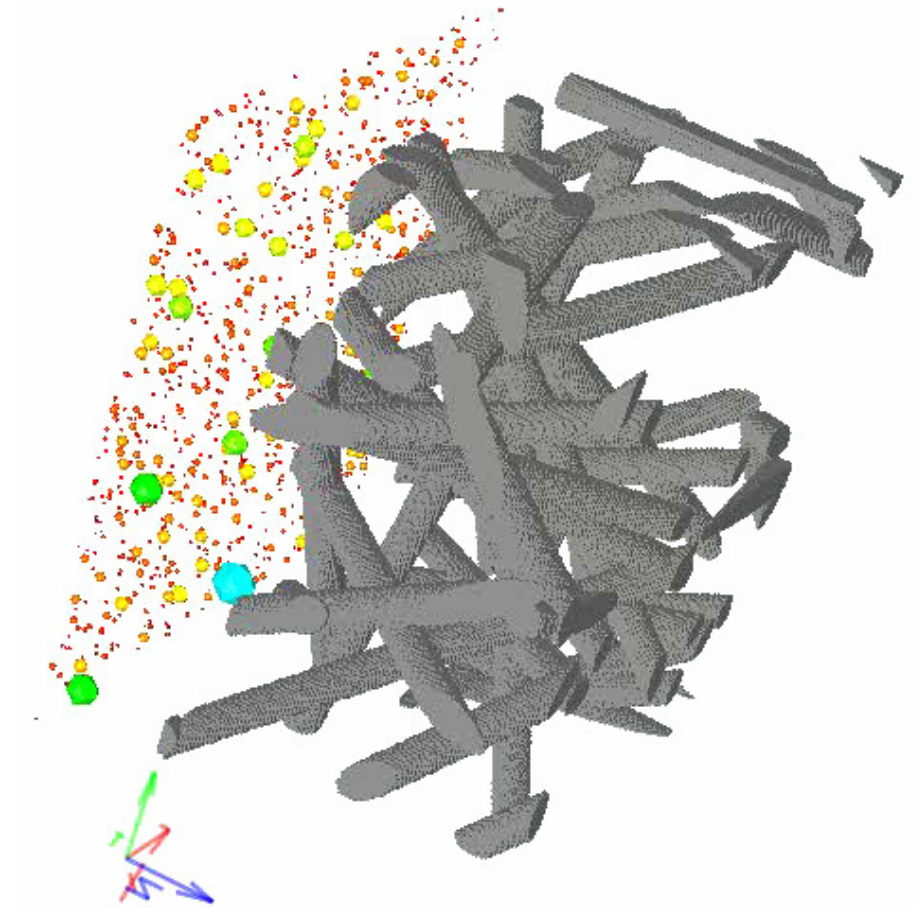
October 15-18, 2007, Ann Arbor, MI



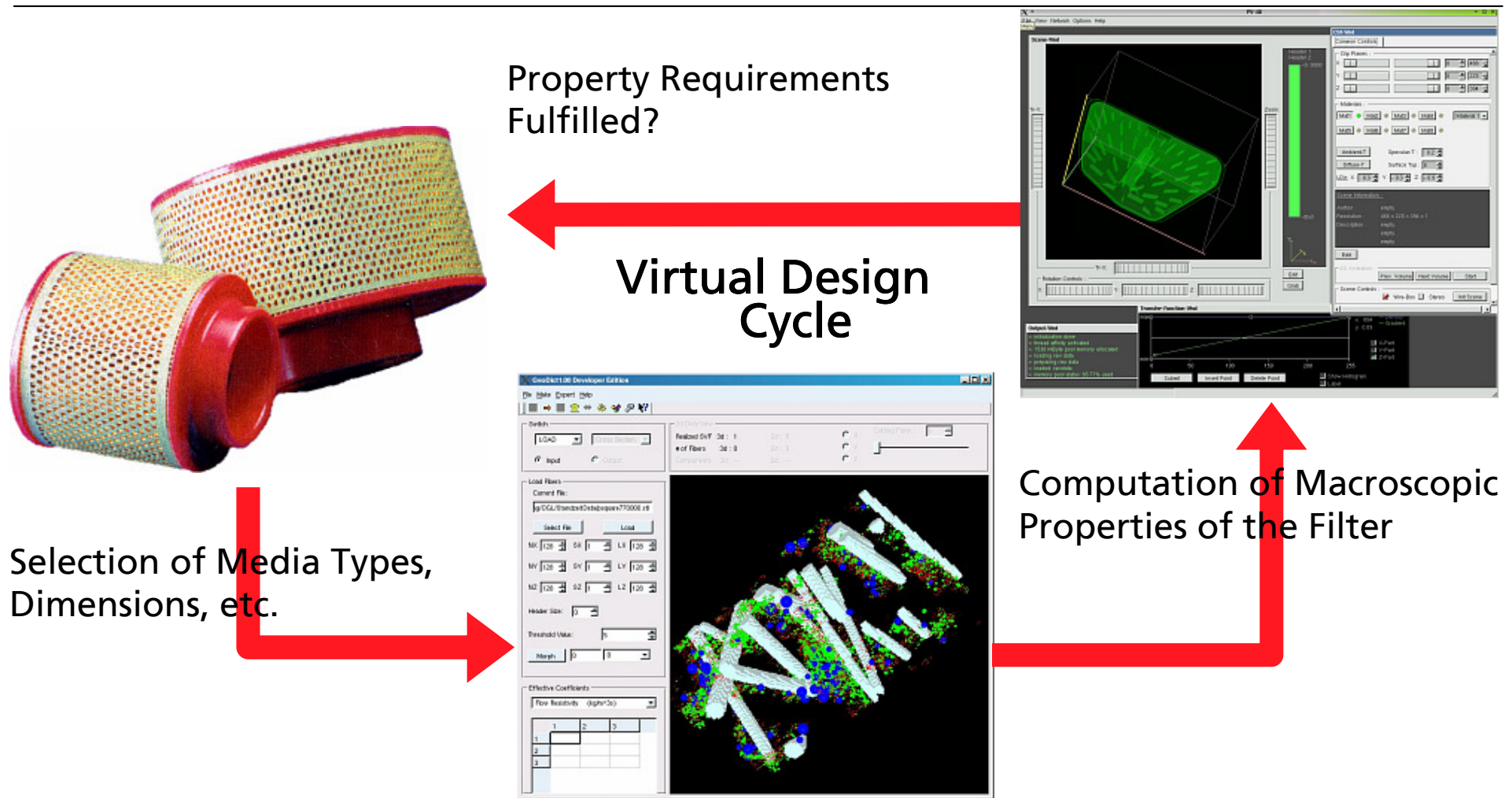
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Overview

1. Virtual Material Design Cycle
2. Virtual Filter Geometries
3. Simulation of Filtration Processes
 - a) Modeling
 - b) Simulation Results
 - c) Software Tools
4. Summary and Future Developments



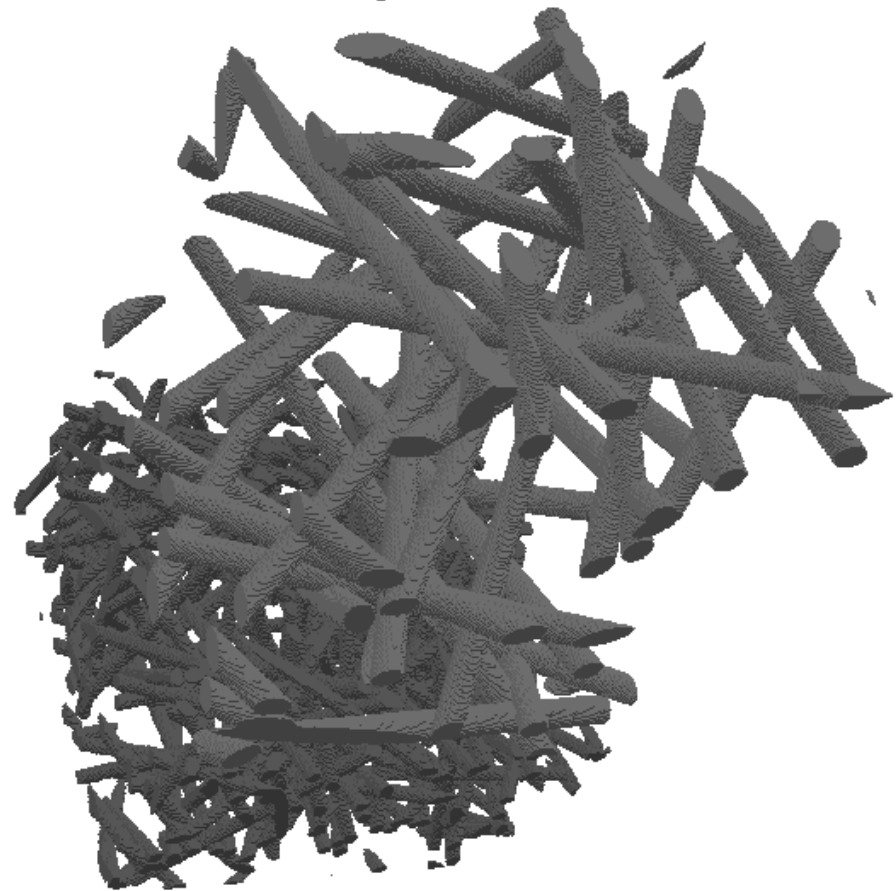
1. Virtual Material Design Cycle



2. Virtual Filter Geometries

Multilayer Virtual Nonwoven

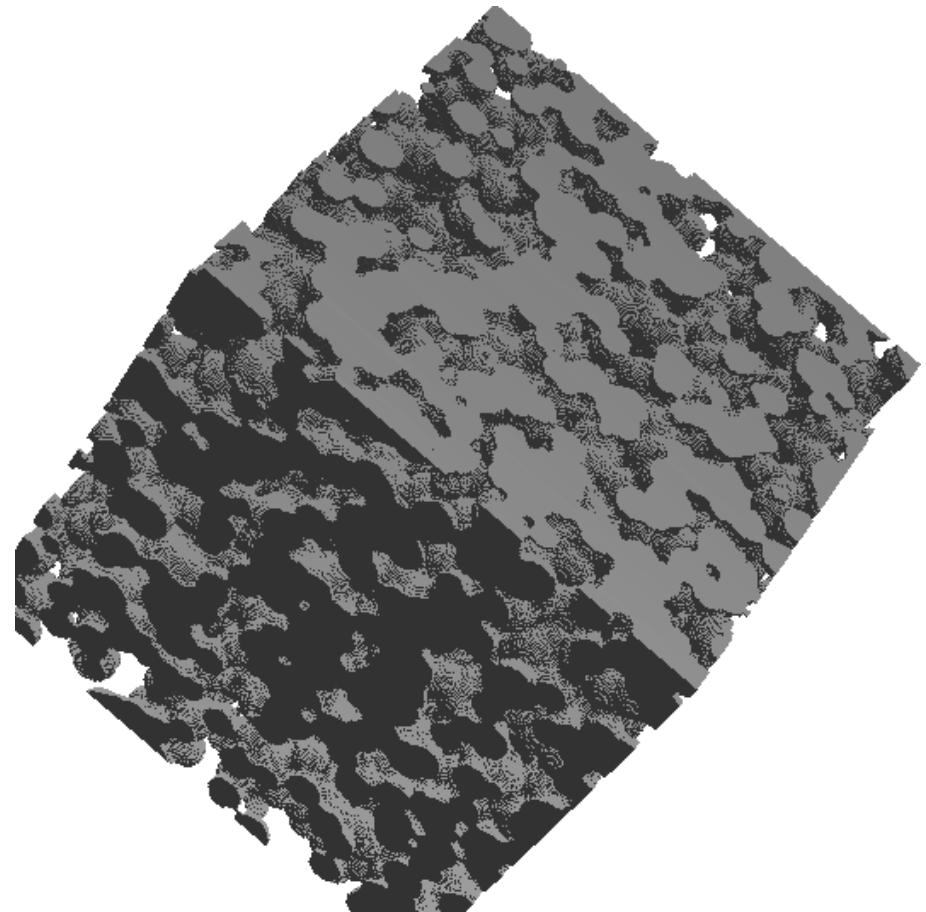
- Stochastic generation of the structure with guaranteed adjustable properties, e.g.
 - Distribution of fiber diameters and cross sections
 - Fiber orientation
 - Porosity
 - Layer thickness
 - ...
- Stacking of layers with different parameters
- Use of highly flexible voxel meshes



2. Virtual Filter Geometries

Virtual Sinter Structure I

- Stochastic generation based on
 - Packings of spheres
 - Morphological operations (to generate sinter necks)
- Packings of spheres selected to match the initial grain size distribution of the sinter process
- Approach was applied in an industrial project when no tomographies were available due to
 - Too coarse resolution
 - Difficult preprocessing of samples

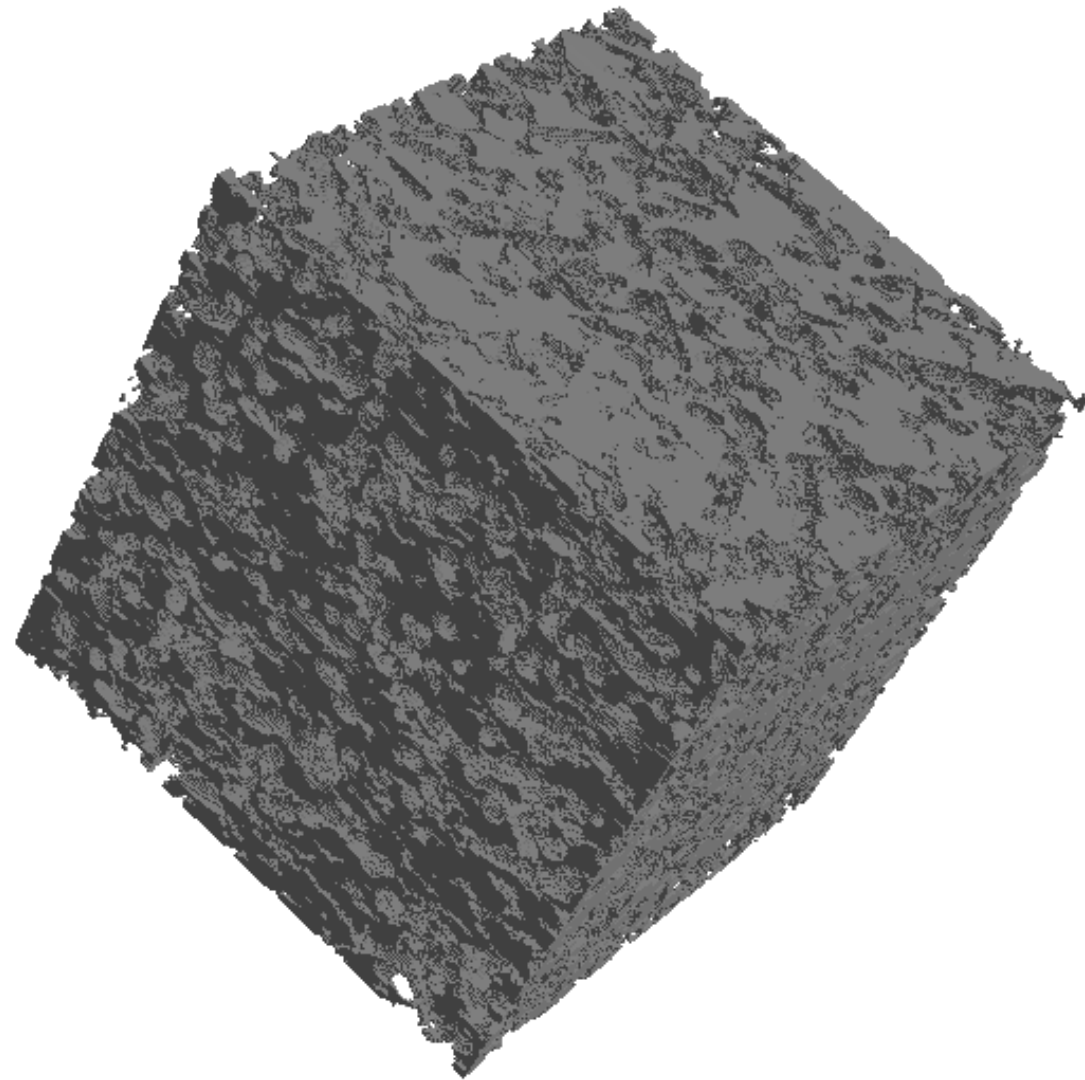


2. Virtual Filter Geometries

SEM image



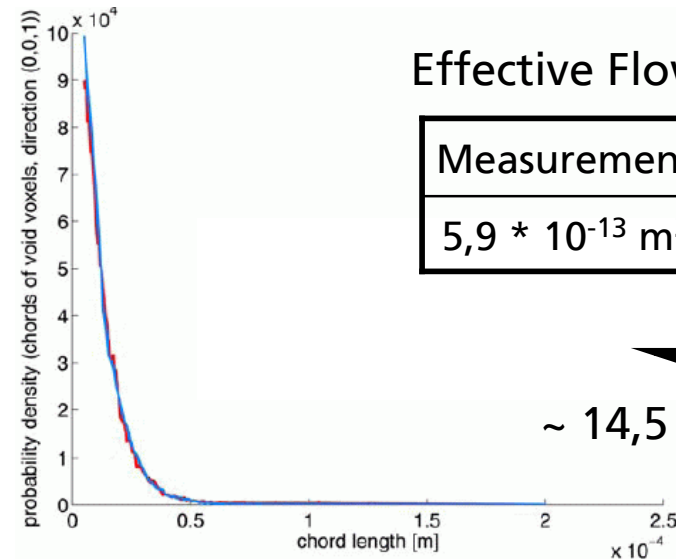
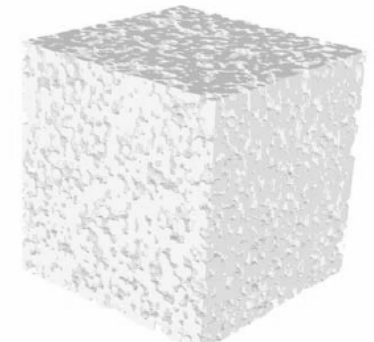
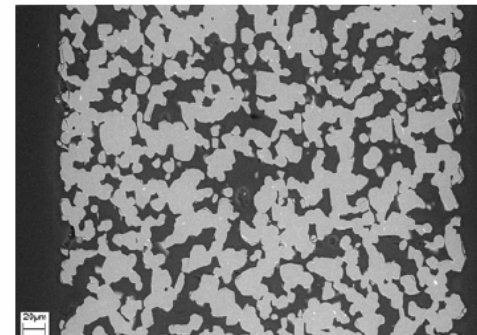
Virtual Reconstruction



2. Virtual Filter Geometries

Quality Measures for Virtual Structures

- “The Eye”
- Porosity
- Cord length distributions: Virtual vs. real SEM cross sections
- Pore size analysis
- Flow properties, e.g. effective permeability or flow resistivity
- Filtration properties
- ...



Effective Flow Permeability

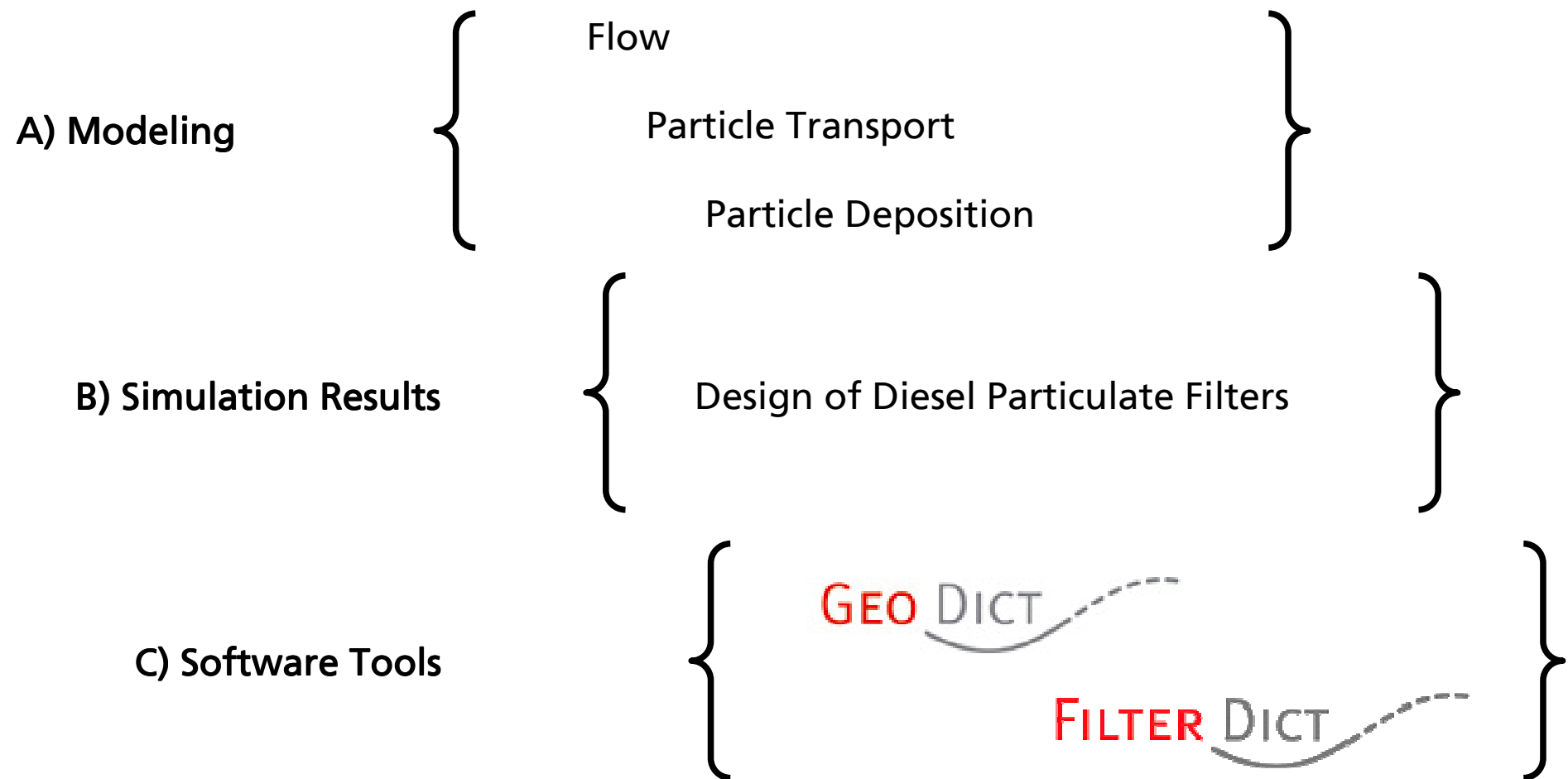
Measurement	Simulation
$5,9 \cdot 10^{-13} \text{ m}^2$	$5,1 \cdot 10^{-13} \text{ m}^2$



~ 14,5 % deviation !



3. Simulation of Filtration Processes



3. Simulation of Filtration Processes - Modeling

Flow simulation is based on Navier-Stokes-Brinkmann equations

$$\begin{aligned} -\mu \Delta \vec{u} + \nabla \vec{u} \cdot \vec{u} + \kappa^{-1} \vec{u} + \nabla p &= \vec{f}, & (\text{momentum balance}) \\ \nabla \cdot \vec{u} &= 0, & (\text{continuity}) \end{aligned}$$

+ boundary conditions,

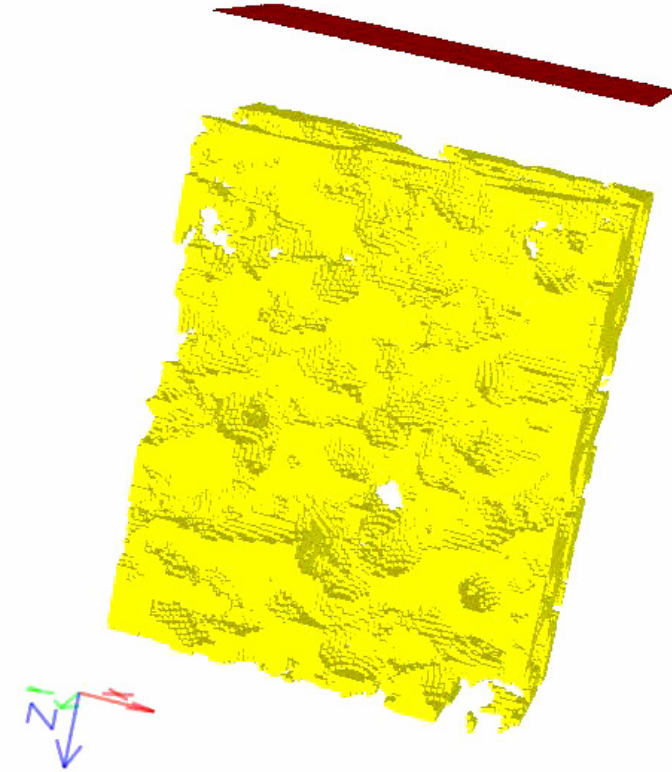
$\vec{u}$: velocity

p : pressure

$\vec{f}$: force (density)

μ : fluid viscosity

κ : permeability of porous voxel



Remark

- convective term optional -> fast flow
- Brinkmann term optional -> subgrid particle deposition and effective porous media

3. Simulation of Filtration Processes - Modeling

Lagrangian Particle Transport

$$\frac{d\vec{x}}{dt} = \vec{v}$$

$$\frac{d\vec{v}}{dt} = -\gamma (\vec{v}(\vec{x}) - \vec{u}(\vec{x})) + \frac{Q\vec{E}_o(\vec{x})}{m} + \sigma \frac{d\vec{W}(t)}{dt}$$

$$\gamma = 6\pi\rho\mu\frac{R}{m}$$

$$\sigma^2 = \frac{2k_B T \gamma}{m}$$

$$\langle dW_i(t), dW_j(t) \rangle = \delta_{ij} dt$$

t :	time
$\vec{x}$:	particle position
$\vec{v}$:	particle velocity
R :	particle radius
m :	particle mass
Q :	particle charge
T :	temperature
k_B :	Boltzmann constante
$d\vec{W}(t)$:	3d probability measure
$\vec{E}_o$:	elektric field
$\vec{v}_o$:	fluid velocity
ρ :	fluid density
μ :	fluid viscosity

Particle Deposition

- Collision handling
- Adhesion model

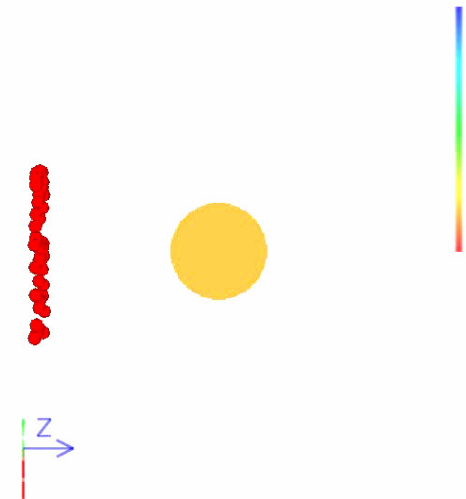
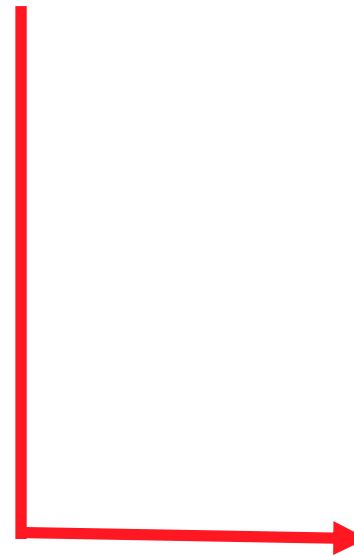
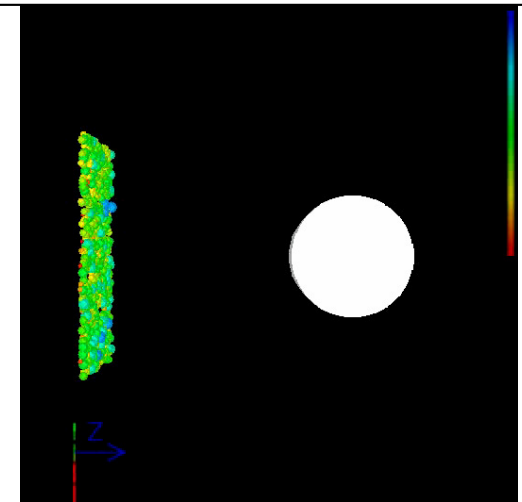
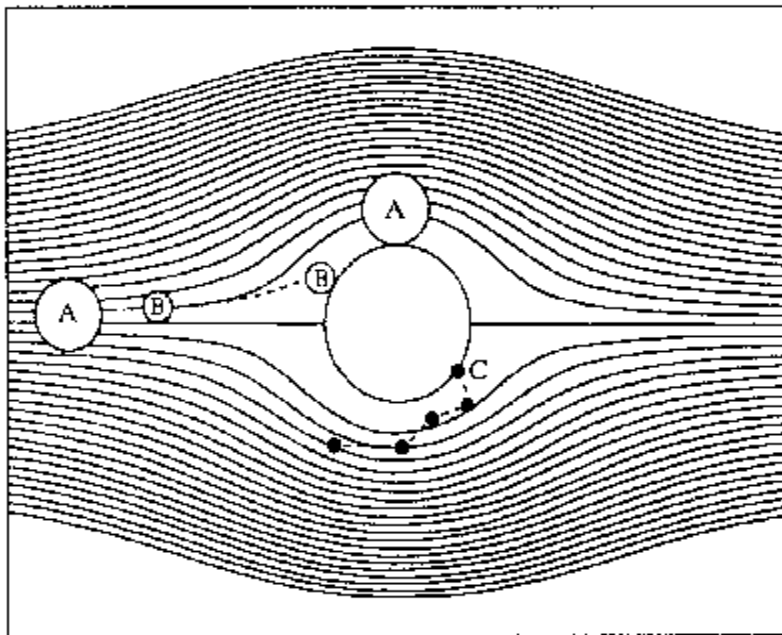
Modification of Geometry

- Solid deposition model (particles resolved by voxels)
- Porous deposition model (small particles)

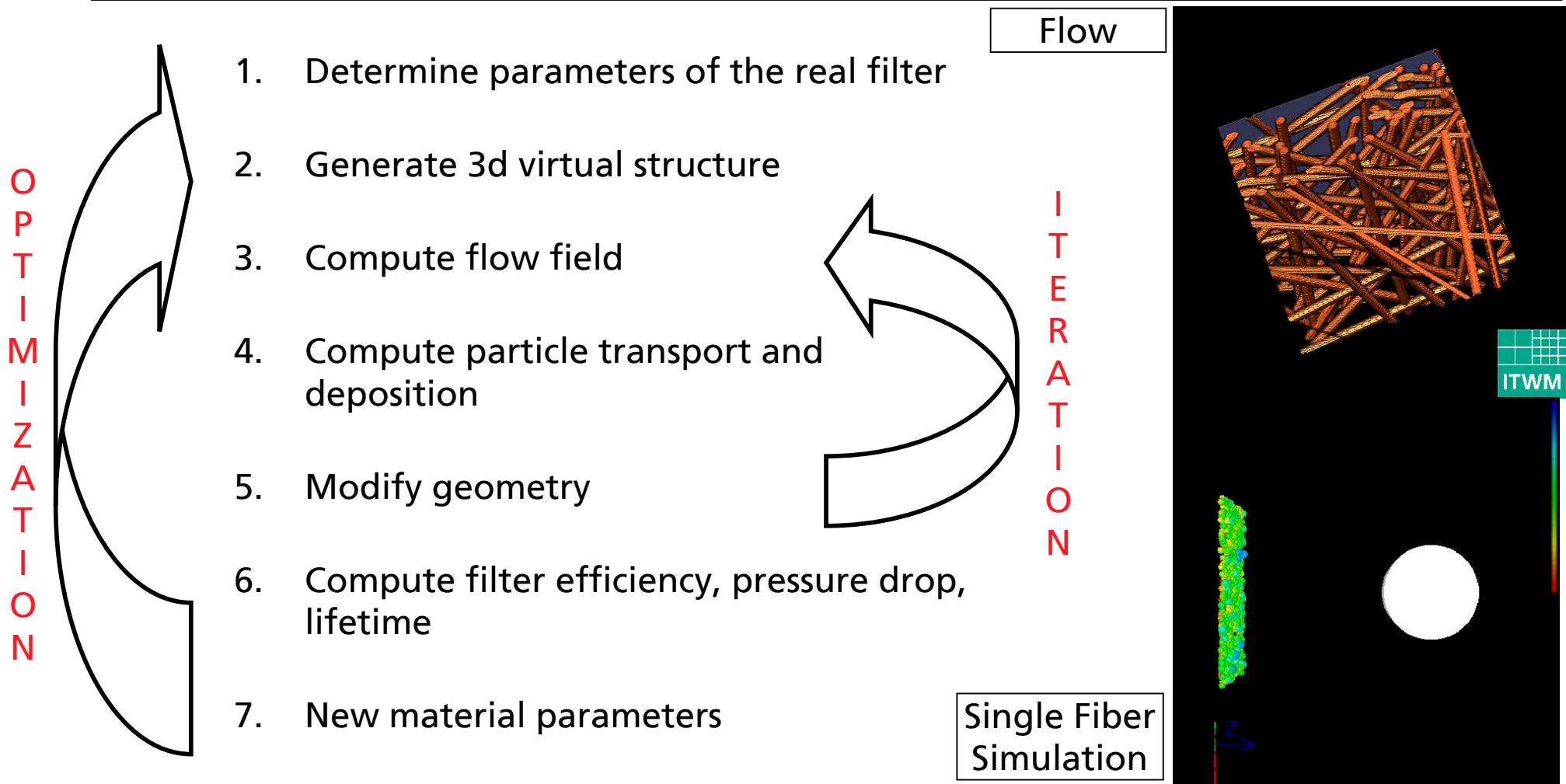
3. Simulation of Filtration Processes - Modeling

Model inherent filtration mechanisms

- A) Barrier effect
- B) Inertia effect
- C) Diffusion effect (Brownian motion)
- D) Sieving
- E) Electrostatic attraction



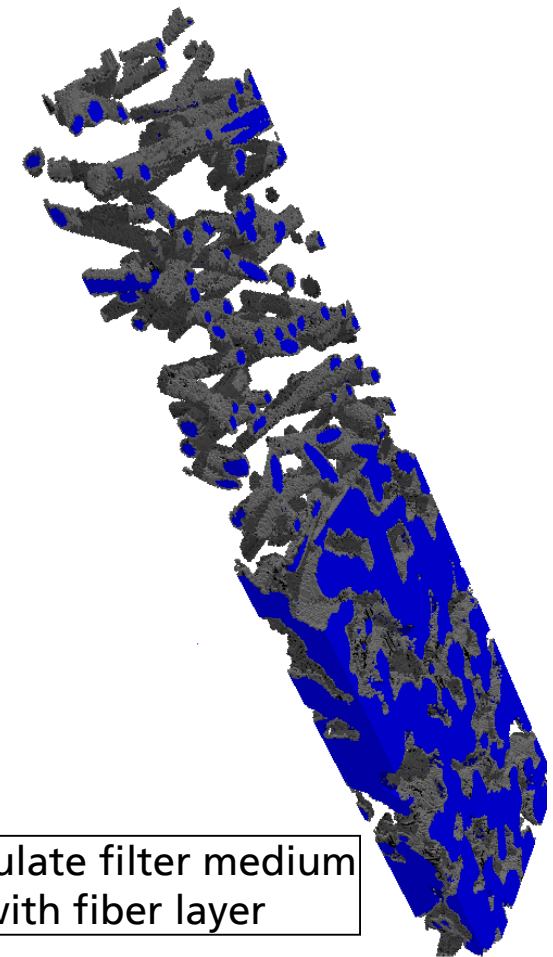
3. Simulation of Filtration Processes - Modeling



3. Simulation of Filtration Processes - Simulation Results

Design study of a Diesel particulate filter

- What is the effect of an additional fibrous layer on top of a sintered substrate ?
- Soot particles ($\sim 80\text{nm}$) are much smaller than voxels ($1\mu\text{m}$) -> porous deposition model
- Navier-Stokes-Brinkmann model to handle free and porous flow
- Permeability and maximum degree of filling of porous voxels are determined by high resolution single fiber experiments
- Some hundreds of millions of particles are needed for a lifetime computation



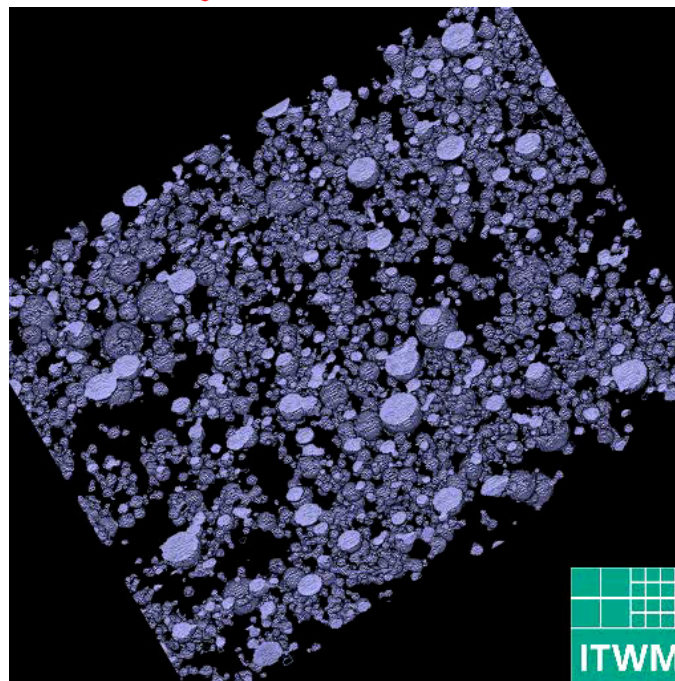
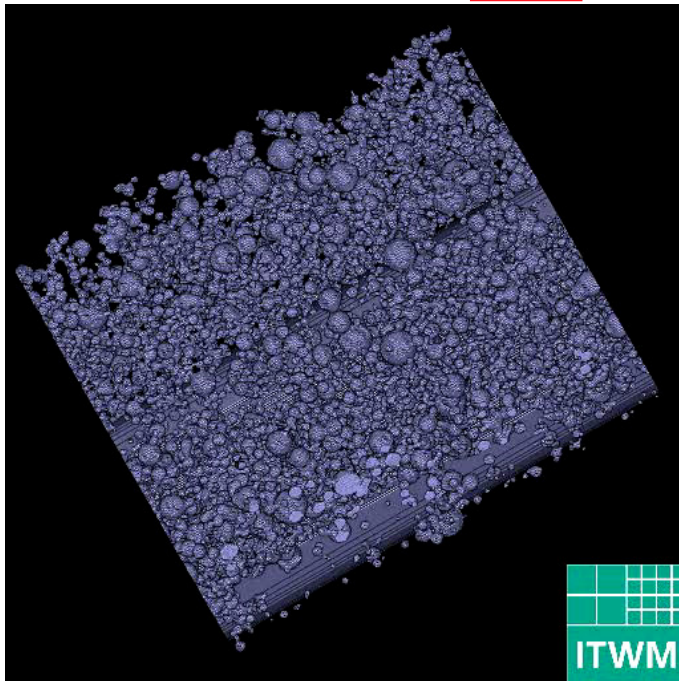
Particulate filter medium
with fiber layer

3. Simulation of Filtration Processes – Simulation Results

Single Fiber
Nanosimulation

Soot Layer Cut-Out

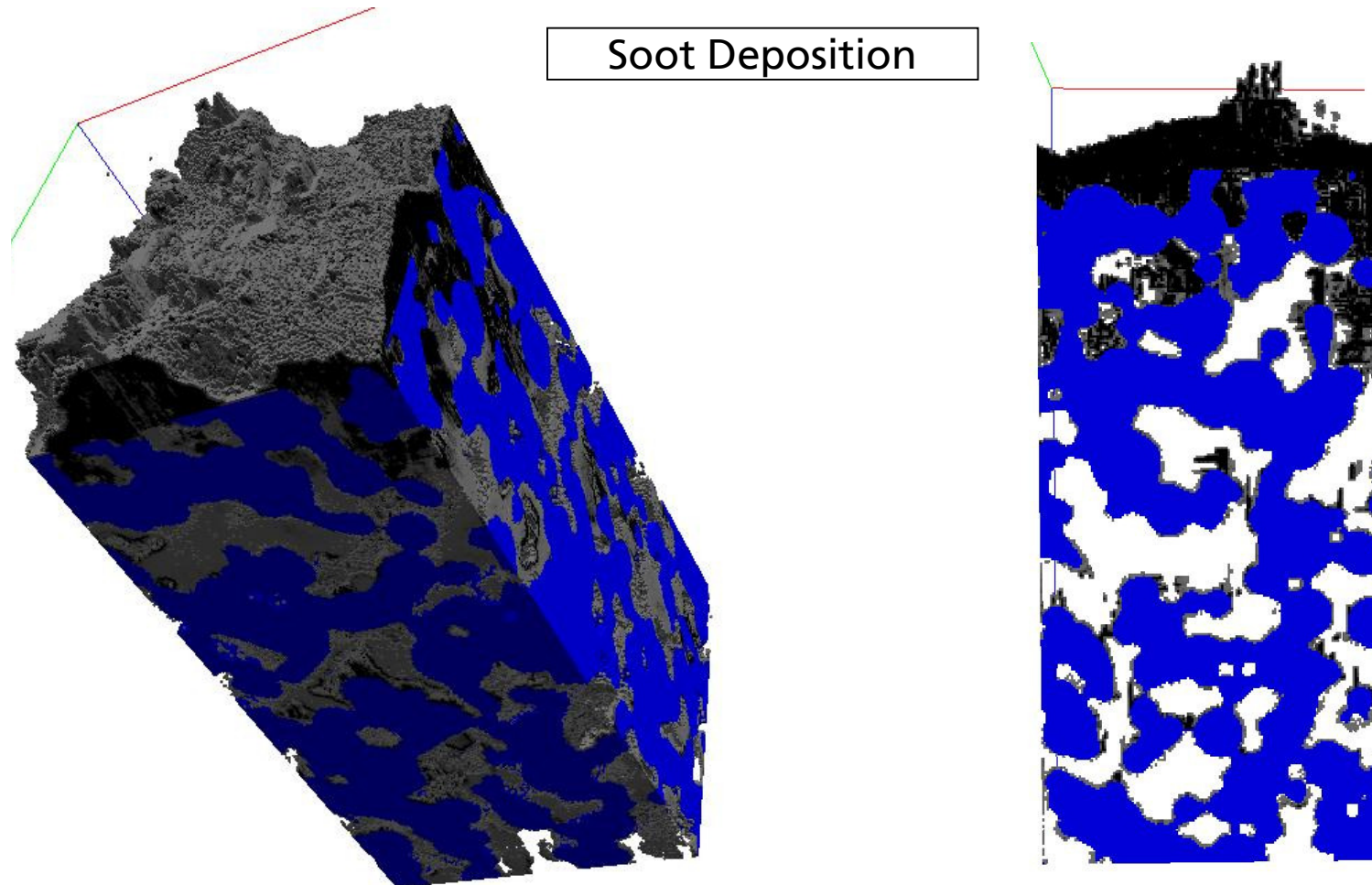
Effective
Microproperties



- Porosity = 85 %
- Permeability = $1e-15 \text{ m}^2$

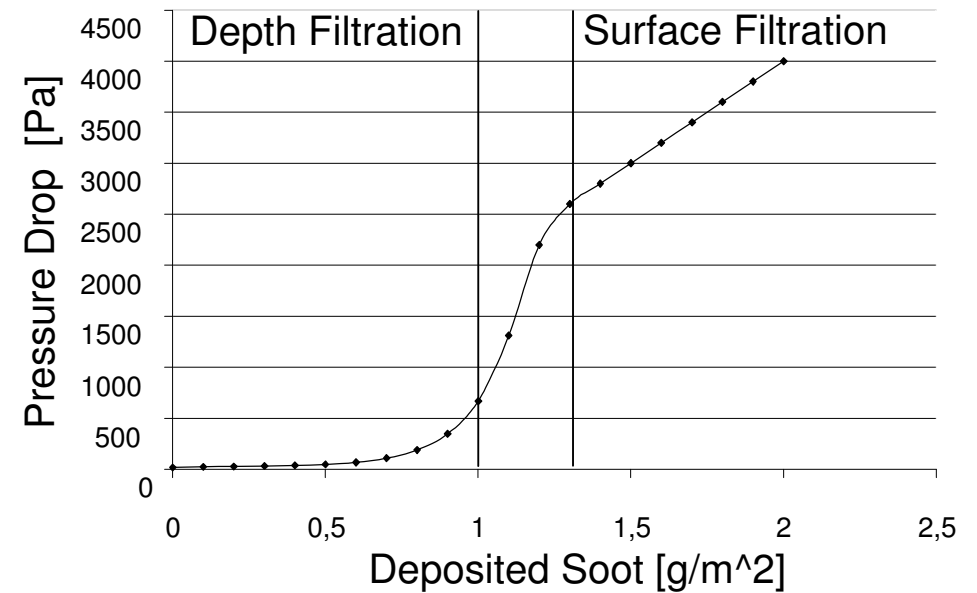
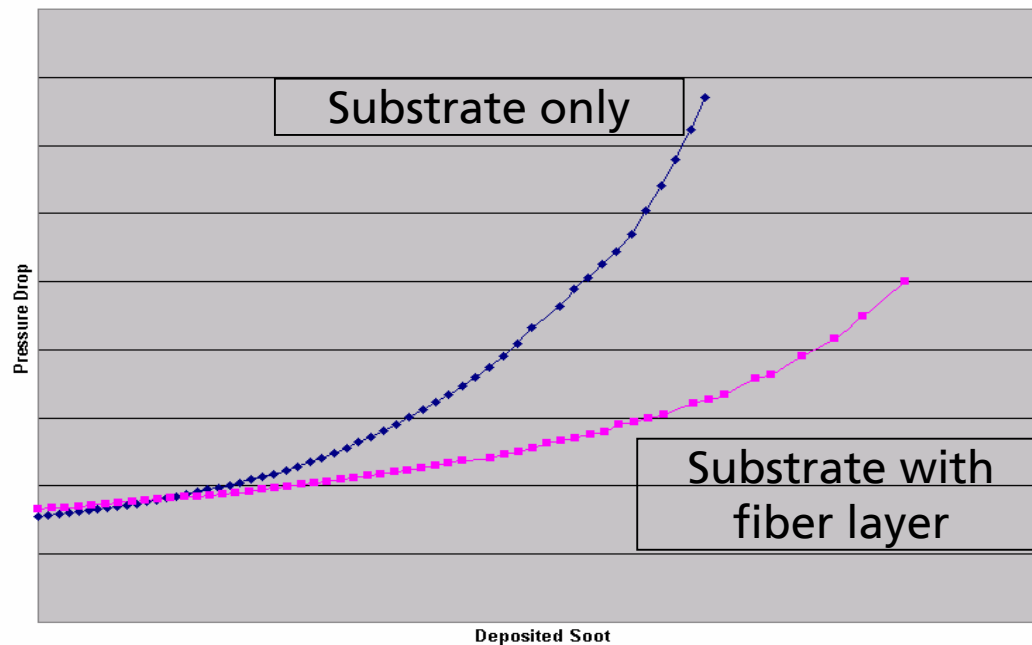


3. Simulation of Filtration Processes - Simulation Results



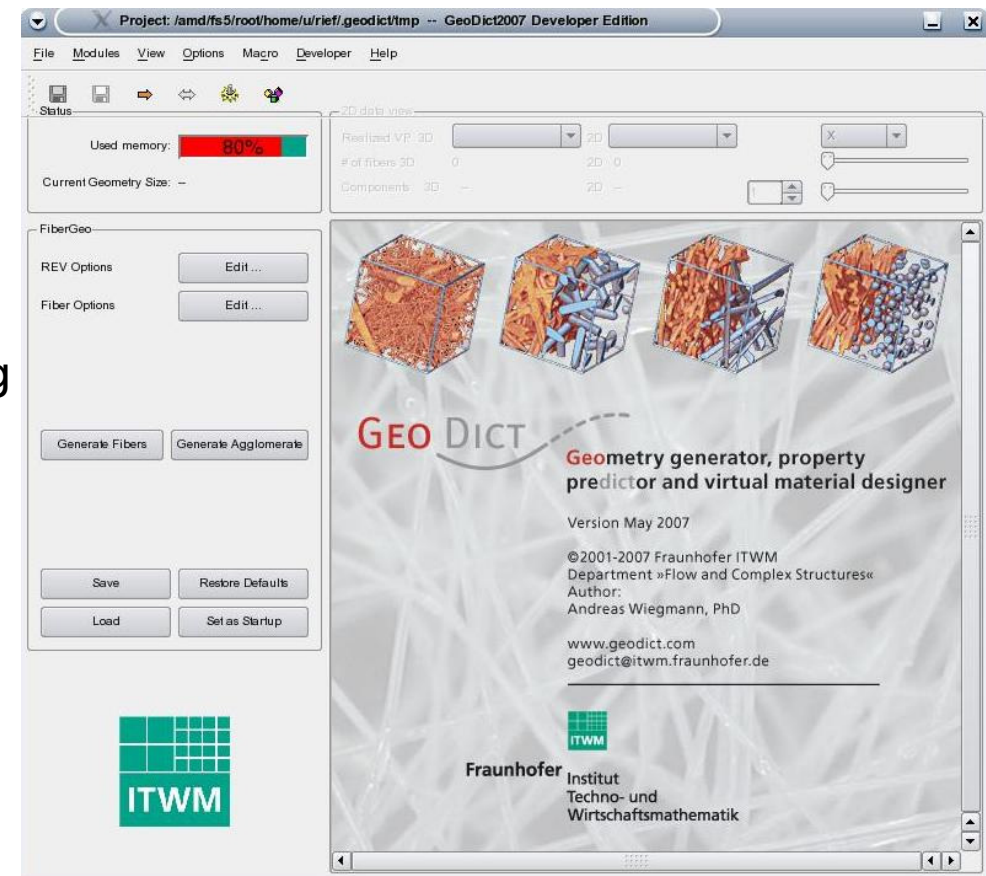
3. Simulation of Filtration Processes - Simulation Results

Pressure Drop Evolution



3. Simulation of Filtration Processes – Simulation Tools

- Software Tool 
 - **GeoFiber**: Nonwoven generator
 - **GeoSinter**: Sinter structure generator
 - **GeoProcess / GeoLayer**: structure processing
 - **FilterDict**: Particle filtration
 - **SatuDict**: pressure-saturation relations
 - **PoroDict**: Pore size distributions



4. Summary and Future Developments

Today

- Virtual structure generation
- Effective flow properties
- Filter efficiencies
- Filter lifetime
- Coupling of scales
- All methods are available by software tools



Tomorrow (DPF related)

- Extending virtual structure generation
- Coupling of length scales
- General particle shapes
- Fractional Slip Phenomena

Tomorrow (in general)

- Standard Tests
- Particle re-entry into fluid flow
- Electrostatic effects
- Particle-particle interaction
- Fluid-structure interaction

GeoDict development teams

The **GeoDict** Team

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Software for Generation, Simulation, Visualization:



www.geodict.com

Thank you for attending this presentation.