# Werkstoffmodellierung und –eigenschaftsberechnung auf Basis von CT-Aufnahmen

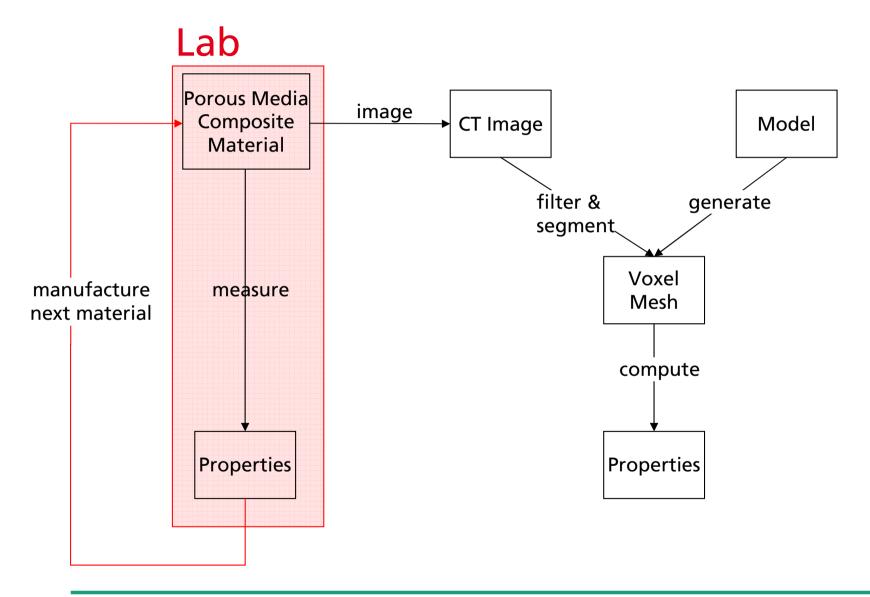
Fachtagung Computertomografie, 27.09.2010

Erik Glatt, Jürgen Becker, Stefan Rief und Andreas Wiegmann

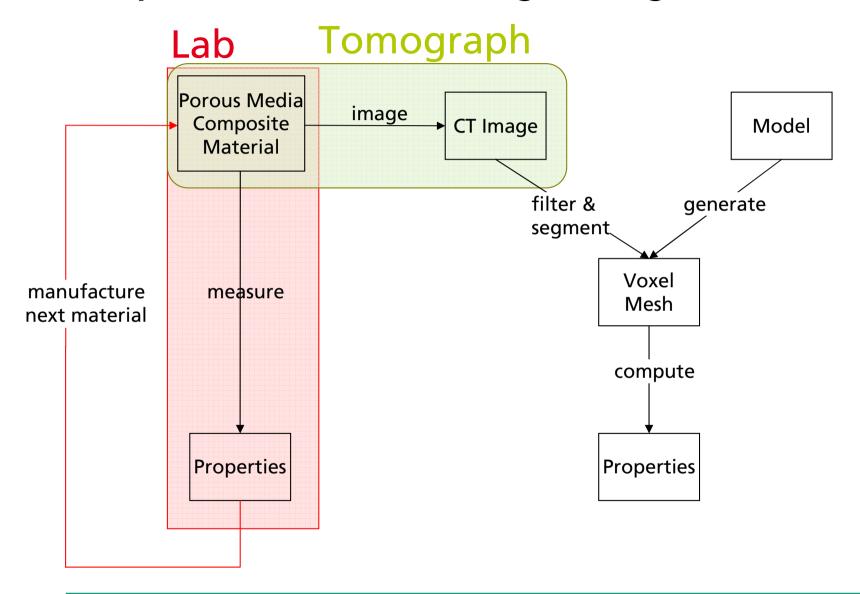
Fraunhofer Institut Techno und Wirtschaftsmathematik,

Kaiserslautern

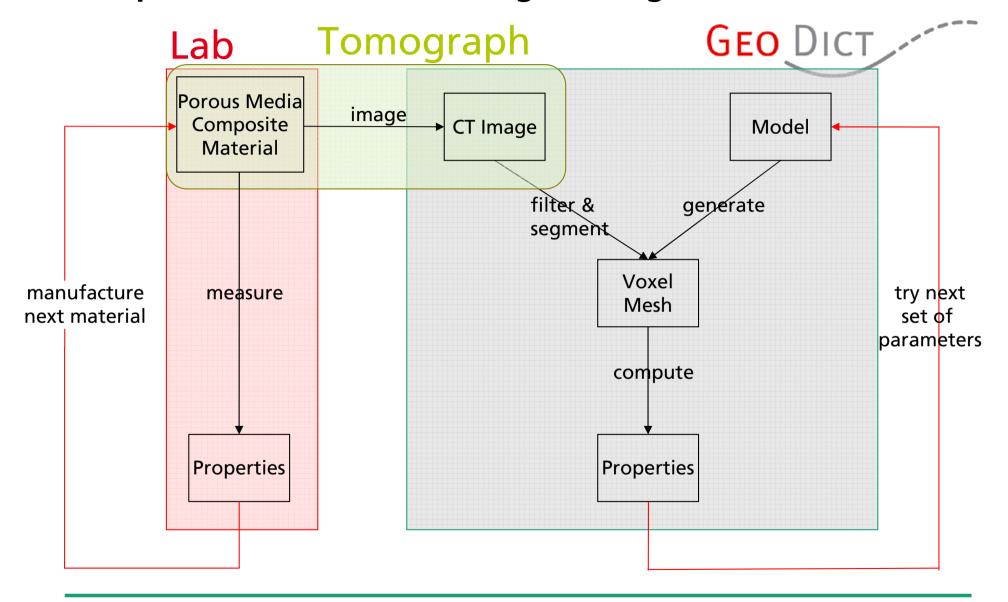




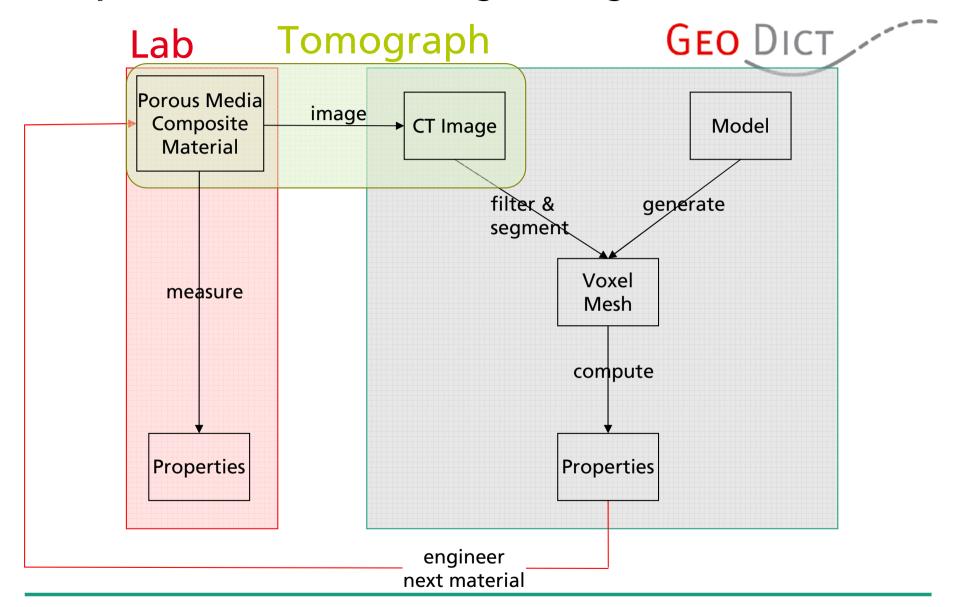










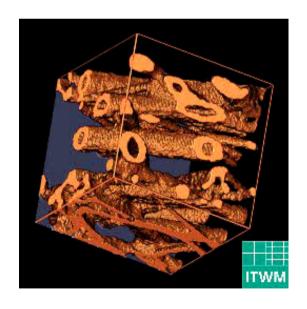


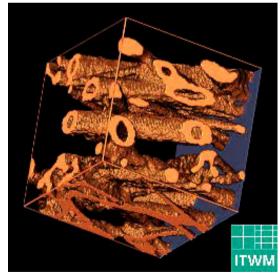


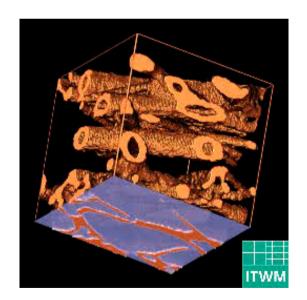
#### **Computation of permeability**

Darcy-Law:  $\overline{\mathbf{u}} = \frac{1}{L} \mathbf{K} \cdot \Delta \mathbf{p}$  Generalized:  $\vec{\mathbf{u}} = -\kappa \cdot \nabla \mathbf{p}$ 

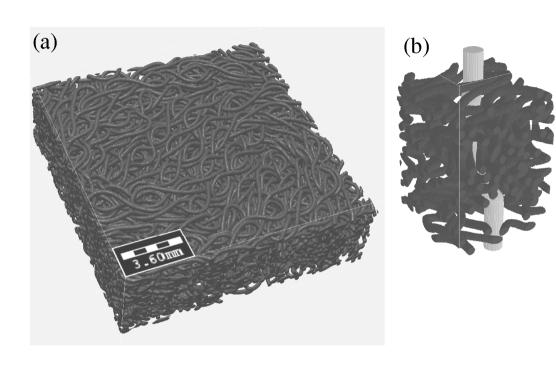
Permeability tensor: 
$$\mathbf{K} = \begin{pmatrix} k_{11} & k_{12} & k_{13} \\ k_{21} & k_{22} & k_{23} \\ k_{32} & k_{32} & k_{33} \end{pmatrix}$$
 Find anisotropic material behavior





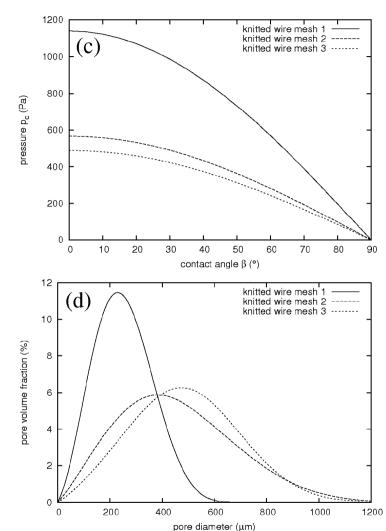


#### **Knitted Wire Meshes: Geometry-Based Property Analyses**





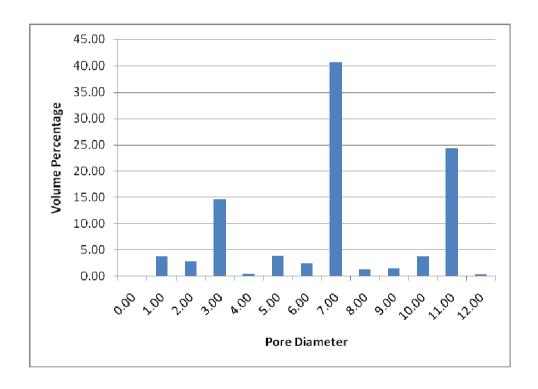
- (b): Largest through pore.
- (c): Bubble point pressure in dependency of the contact angle.
- (d): Pore size distribution.



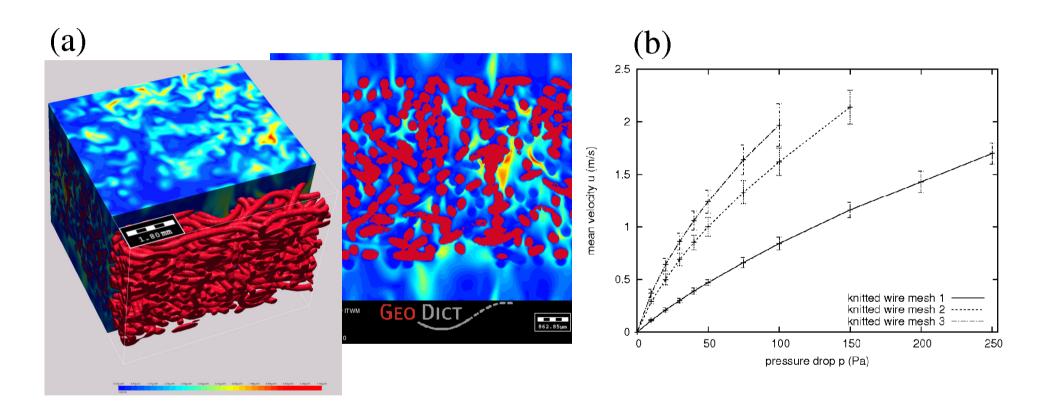


# Use PSD for solids to get fiber diameters





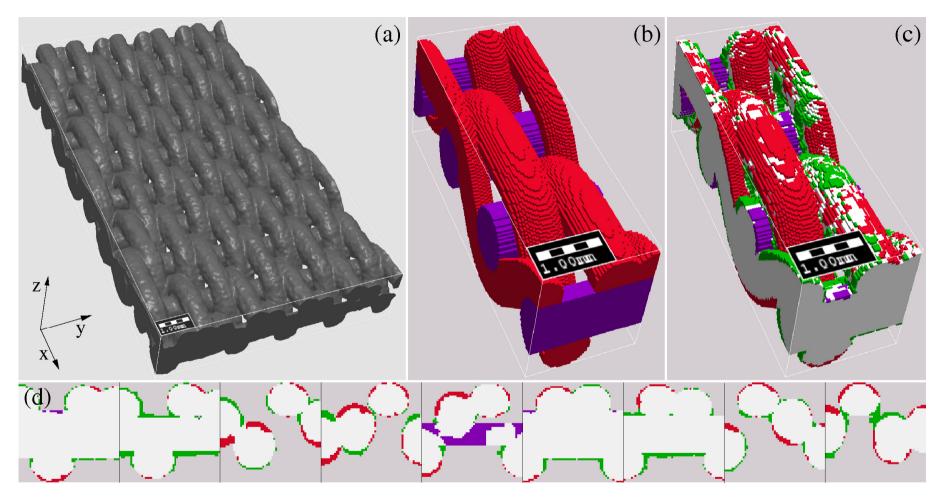
# Knitted Wire Meshes: Partial-Differential-Equation-Based Property Analysis



- (a): Magnitude of velocity in a CT-scan of a knitted wire mesh.
- (b): Mean velocity as function of pressure drop for three knitted wire meshes.



#### **Woven Metal Wire Meshes: Geometric Validation**



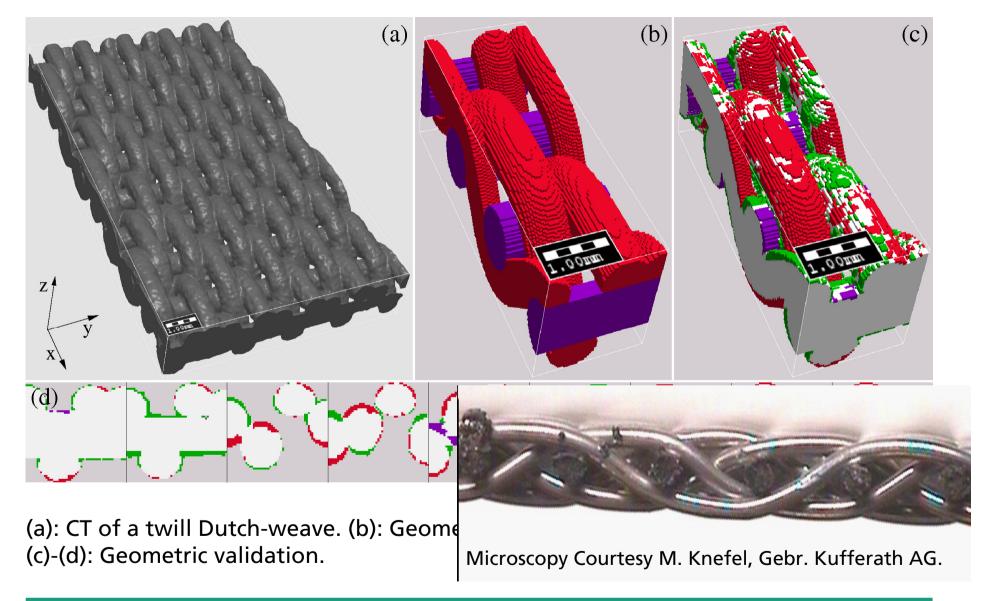
(a): CT of a twill Dutch-weave. (b): Geometry model.

(c)-(d): Geometric validation. Microse

Microscopy Courtesy M. Knefel, Gebr. Kufferath AG.

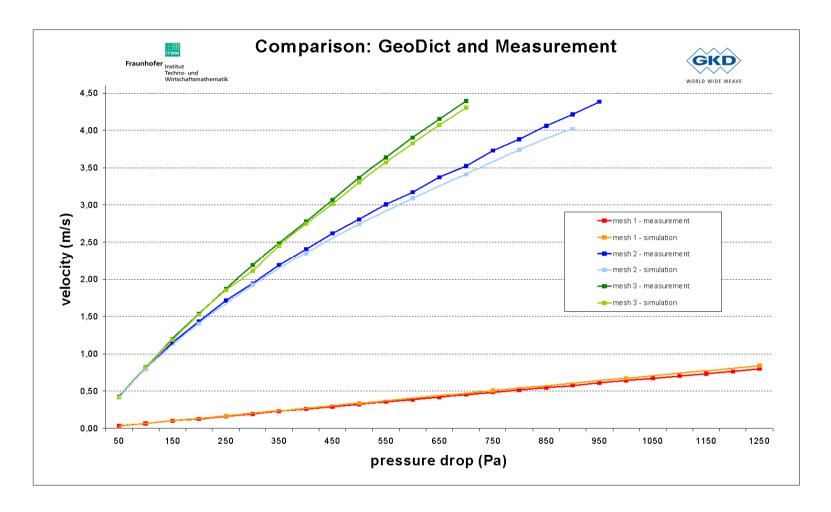


#### **Woven Metal Wire Meshes: Geometric Validation**





#### **Woven Metal Wire Meshes: Measurement and Simulation**



Velocity dependent pressure drop: Comparison between measurements and simulations on corresponding geometry models.

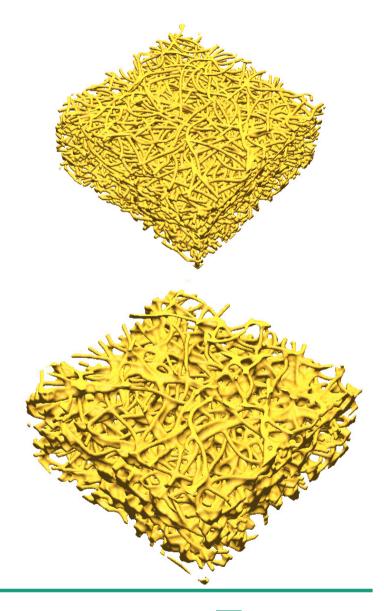


#### **Model: Curved Fibers with inder**

#### **Process:**

- fibers consist of straight segments
- start with one segment, then add segments
- direction of added segment:
  - direction of prev. segment + random disturbance
  - direction of first segment + random disturbance
  - keep current curvature + random disturbance
- add binder

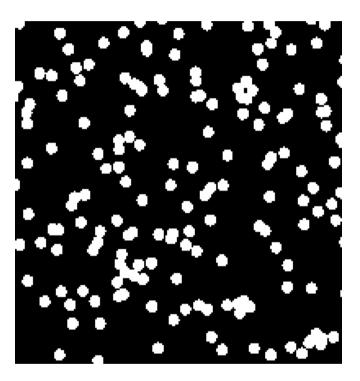






# **Relative Permeability**

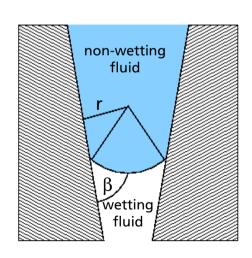
Two-step approach:

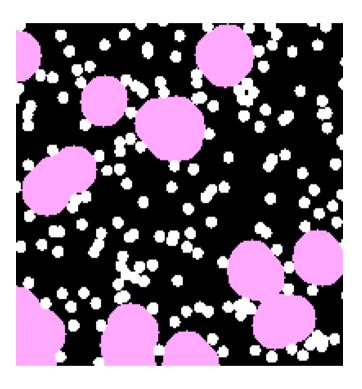


#### **Relative Permeability**

#### Two-step approach:

- 1. Use pore morphology method (Hilpert, 2001) to determine distribution of air and water phase.
  - Idea: a pore is filled with the non-wetting fluid (=water), if  $p_c \geq \frac{2\sigma}{r}\cos\beta$



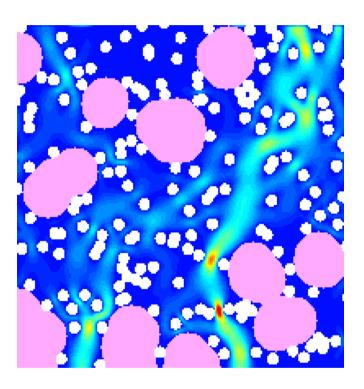




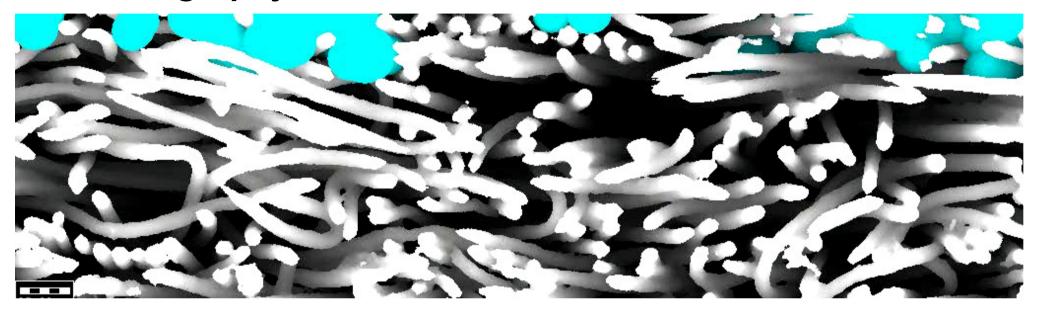
#### **Relative Permeability**

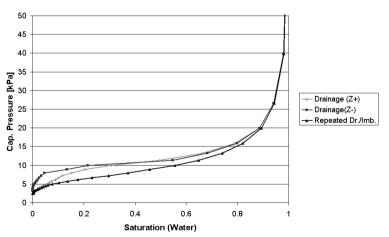
#### Two-step approach:

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  - Idea: a pore is filled with the non-wetting fluid (=water), if  $p_c \geq \frac{2\sigma}{r}\cos\beta$
- 2. Solve Stokes equation on the remaining pore space to determine wetting phase (=air) permebility



# Simulated mercury Distribution at Bubble Point in tomography





pc= 10.6 kPa (r= $10.5 \mu \text{m}$ )





uncompressed

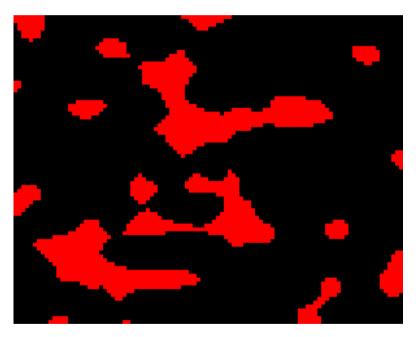




uncompressed

Geometric Algorithm: (Schulz, Becker, Wiegmann, Mukherjee, Wang, J. Electrochem Soc. 154, 2007)

- compression in z-direction
- handles each z-column separately
- mass is kept by shifting solid blocks
- No knowledge about applied forces



compressed (20%, red. model) computation time: 0.25 s





uncompressed



compressed (20%, FE model) computation time: 5 days





uncompressed

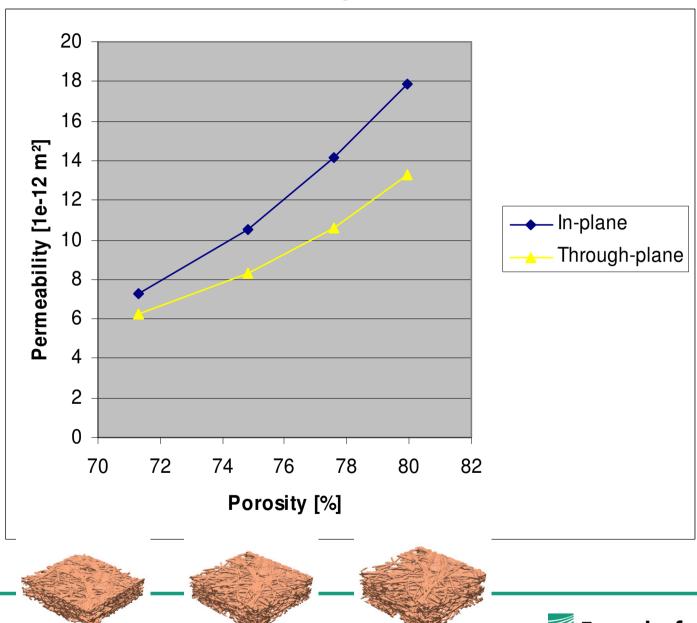


compressed (20%, comparison)



#### **Compression Effect on Permeability**

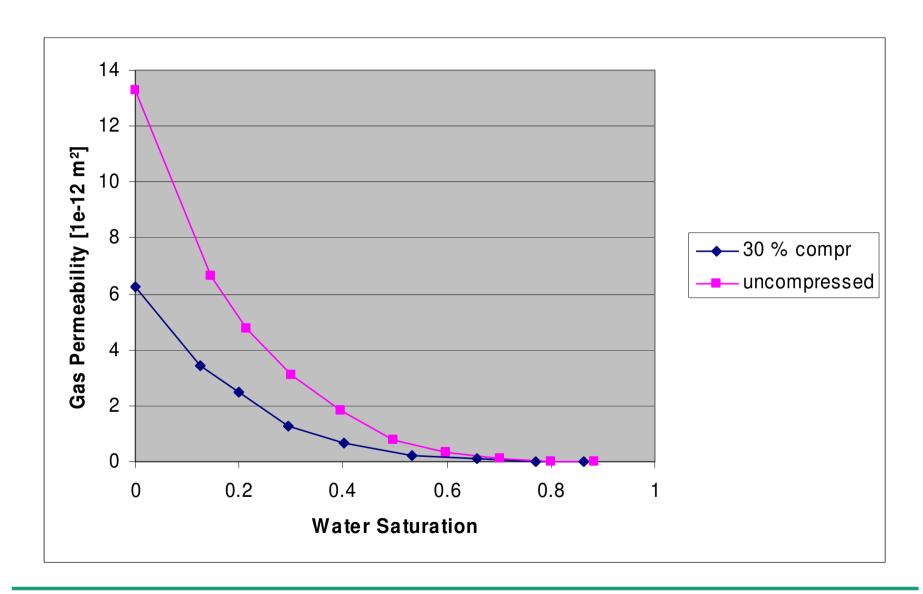
• calculated for 0%, 10%, 20%, 30% compression







#### **Compression Effect on Relative Permeability**

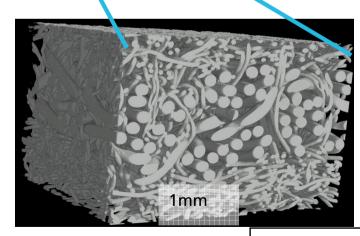




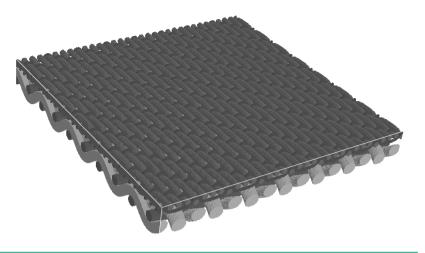
# **Tomography and Models of felts**



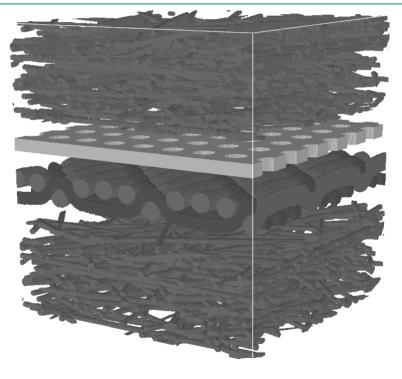
Papiermaschine



Tomographie

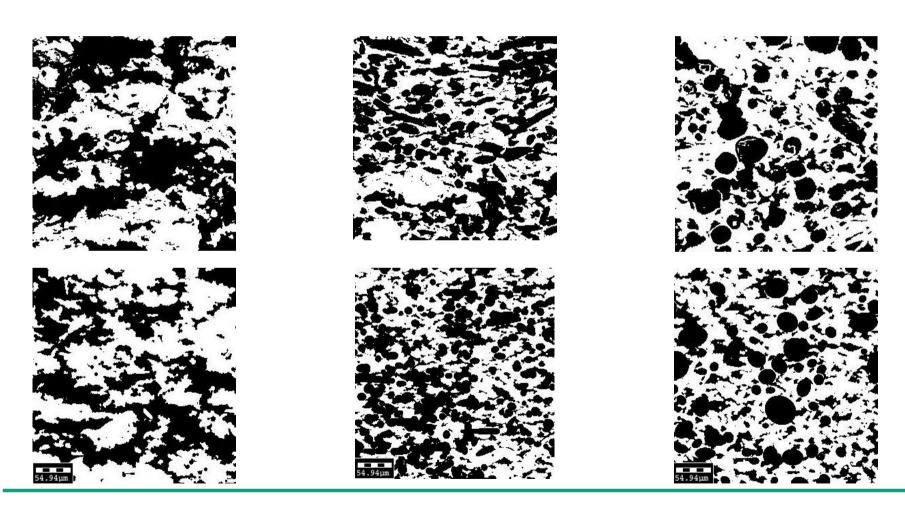


Forming fabric and dewatering felt



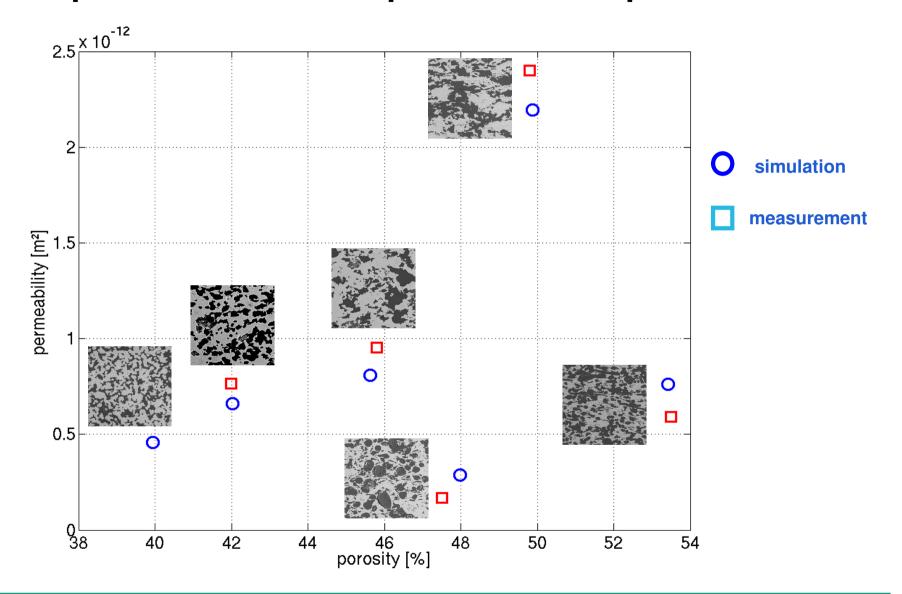


# Binarized SEM (top) and virtual sintered ceramics (bottom)

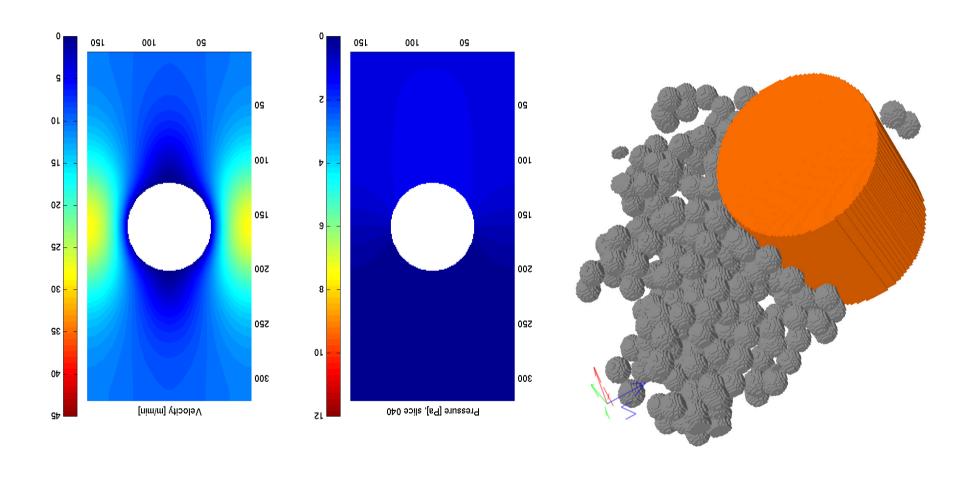




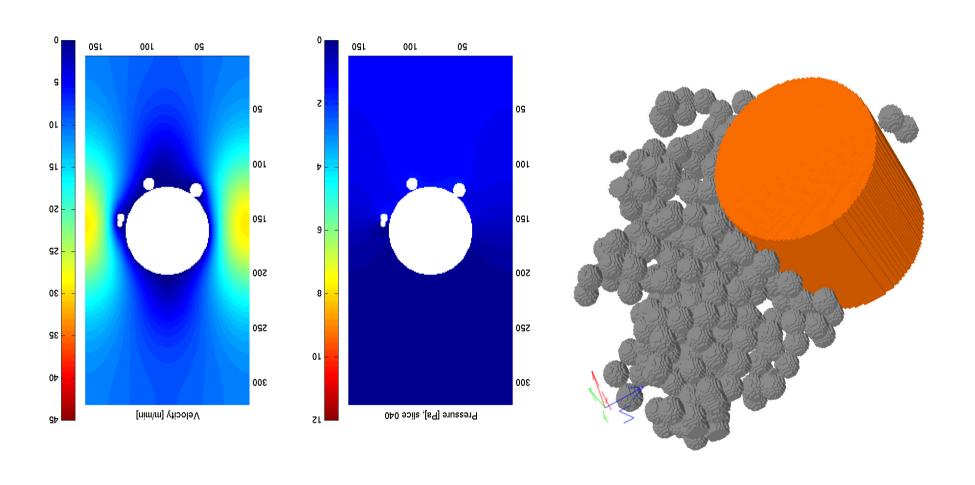
# Computed vs measured porosities and permeabilities



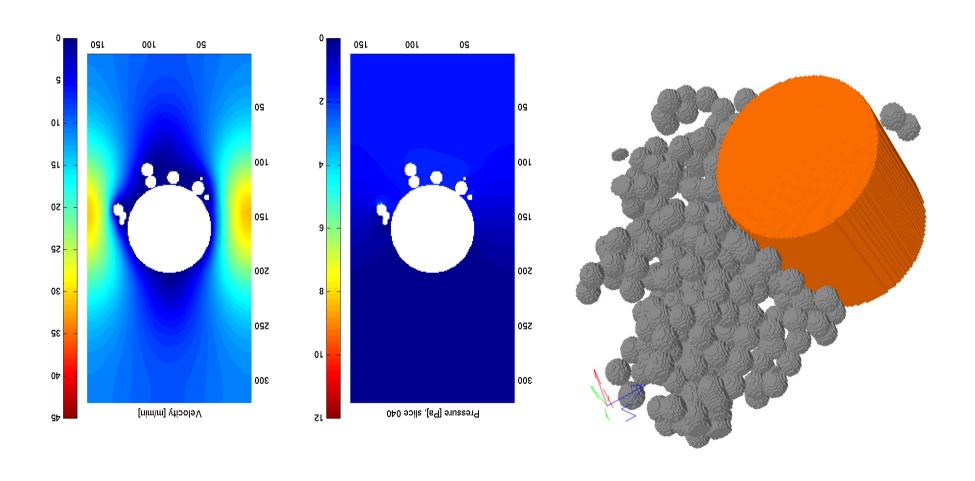




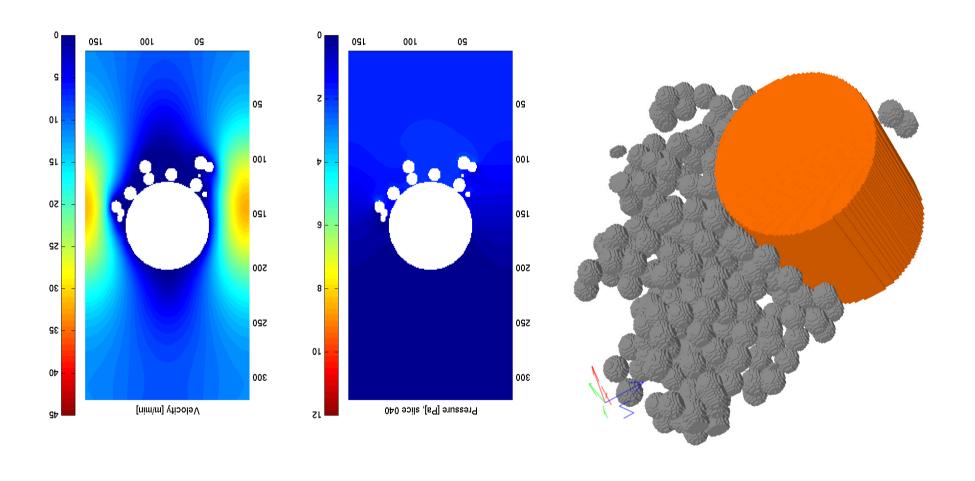




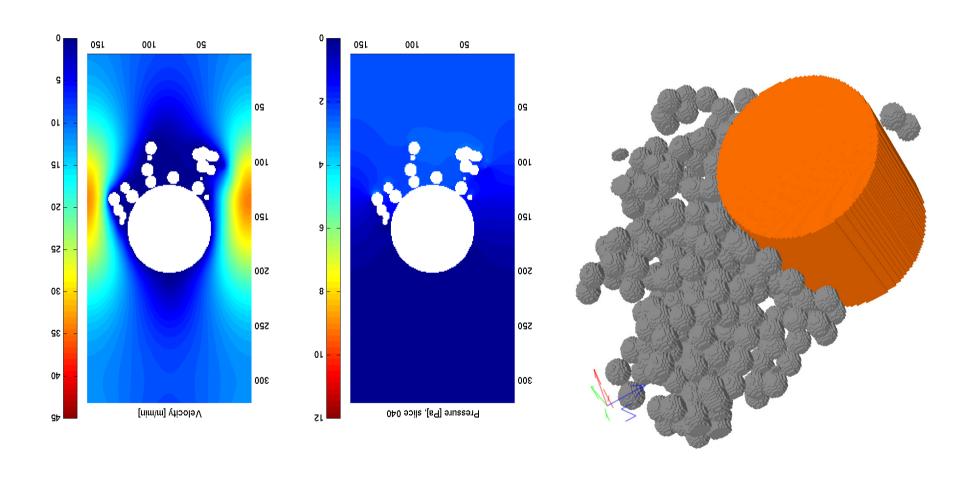




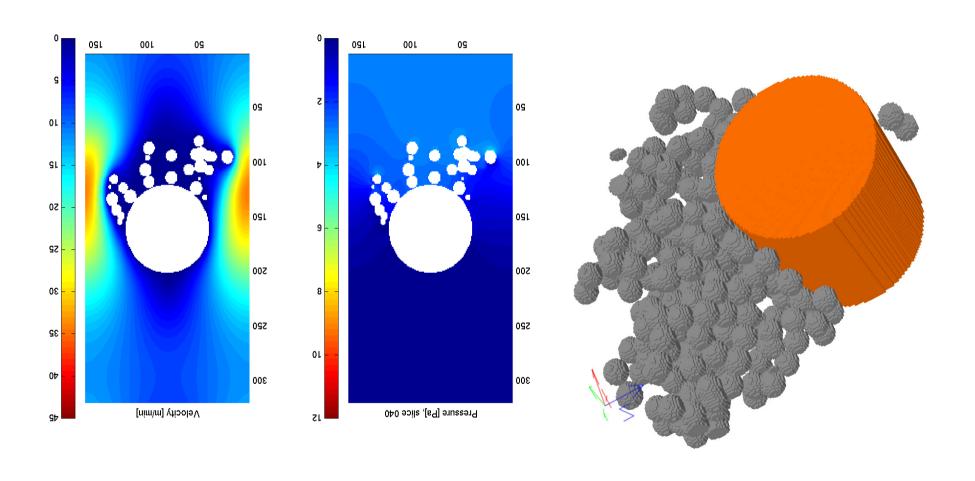




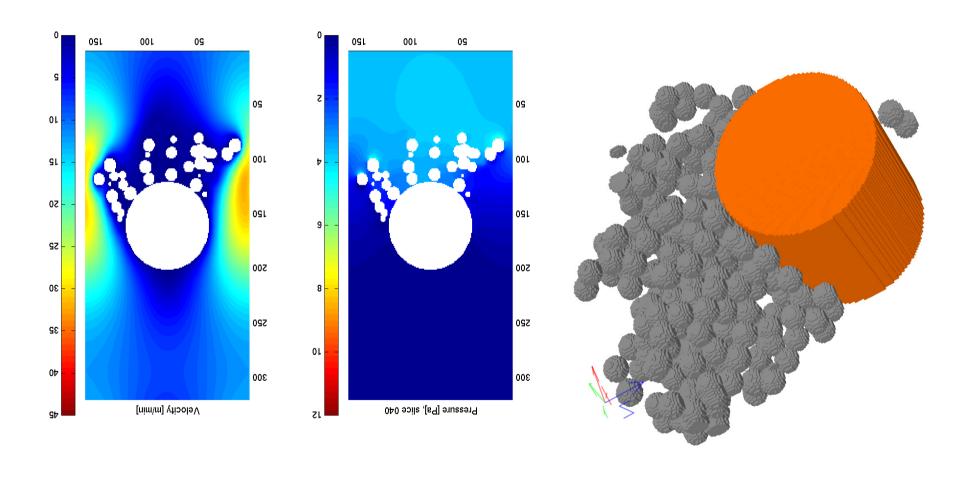




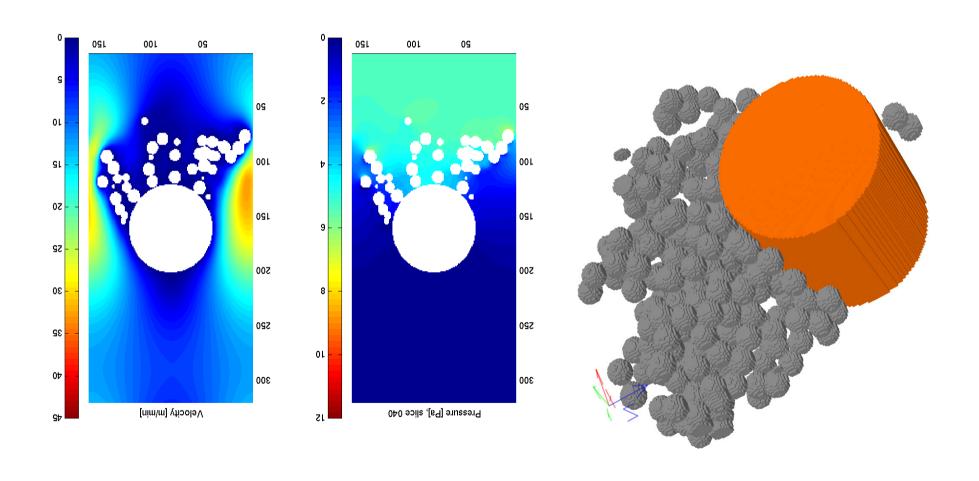




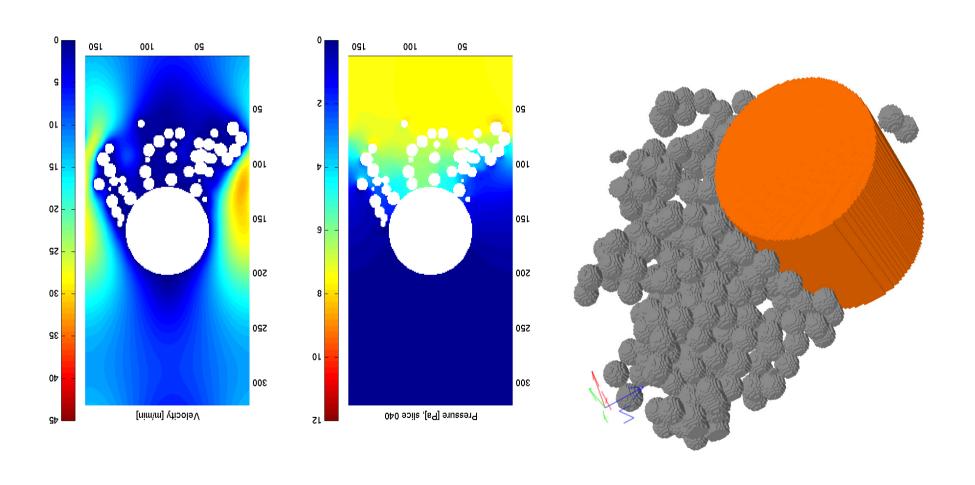




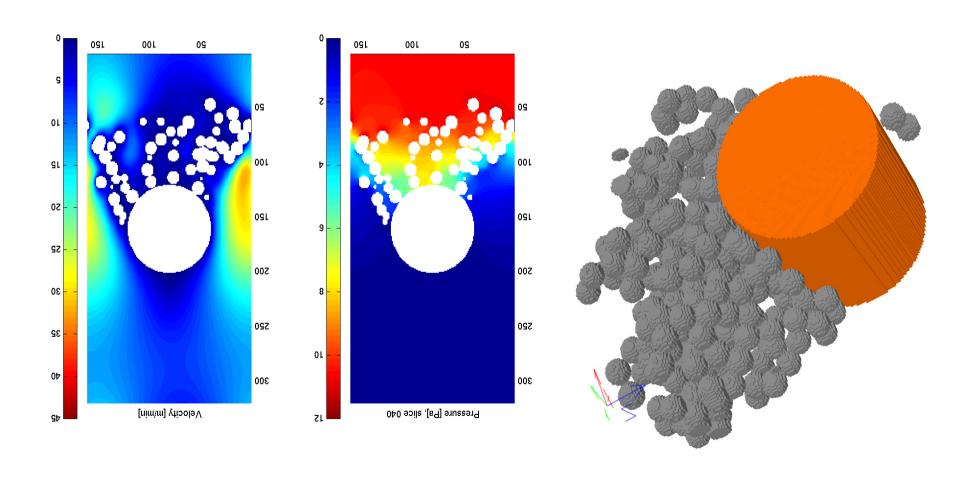




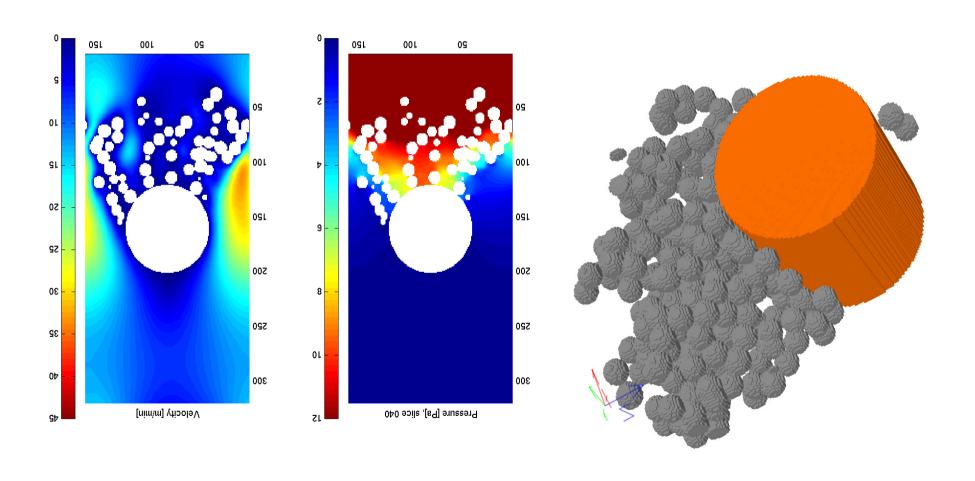
















Geometry and property predictor

Thank You!

www.geodict.com

