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# **Virtual Material Design of PEM Fuel Cell Layers**

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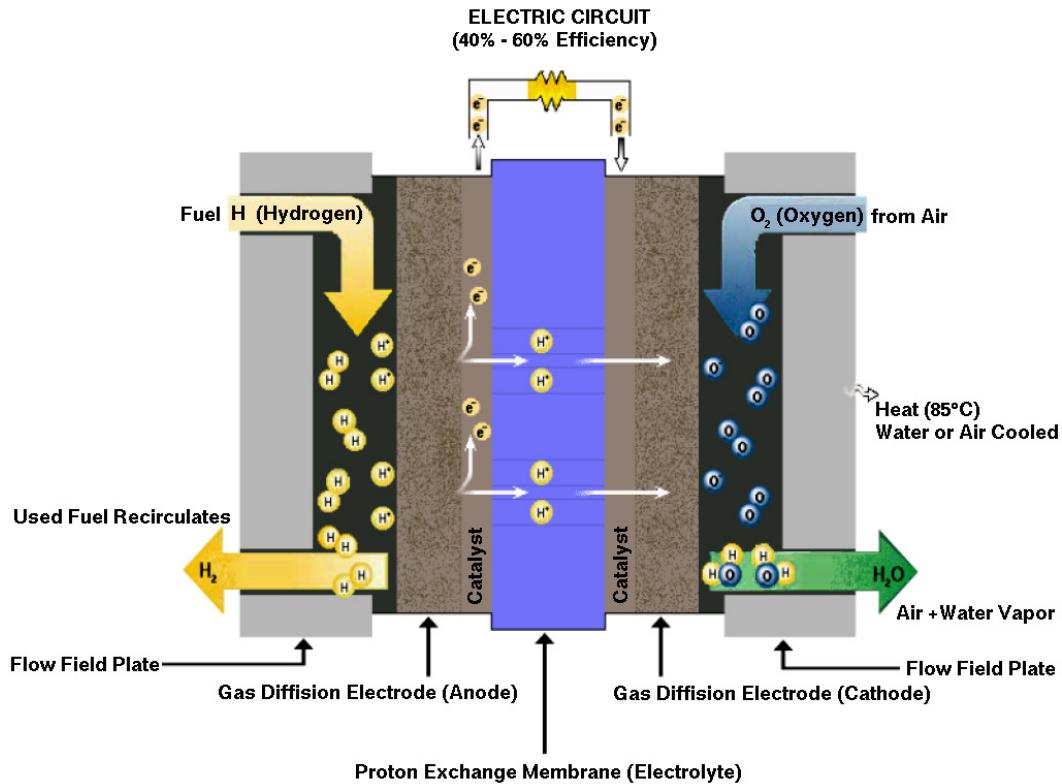
Materials for Energy, Karlsruhe, 06.07.2010

Jürgen Becker, Andreas Wiegmann

Fraunhofer Institute for Industrial Mathematics ITWM

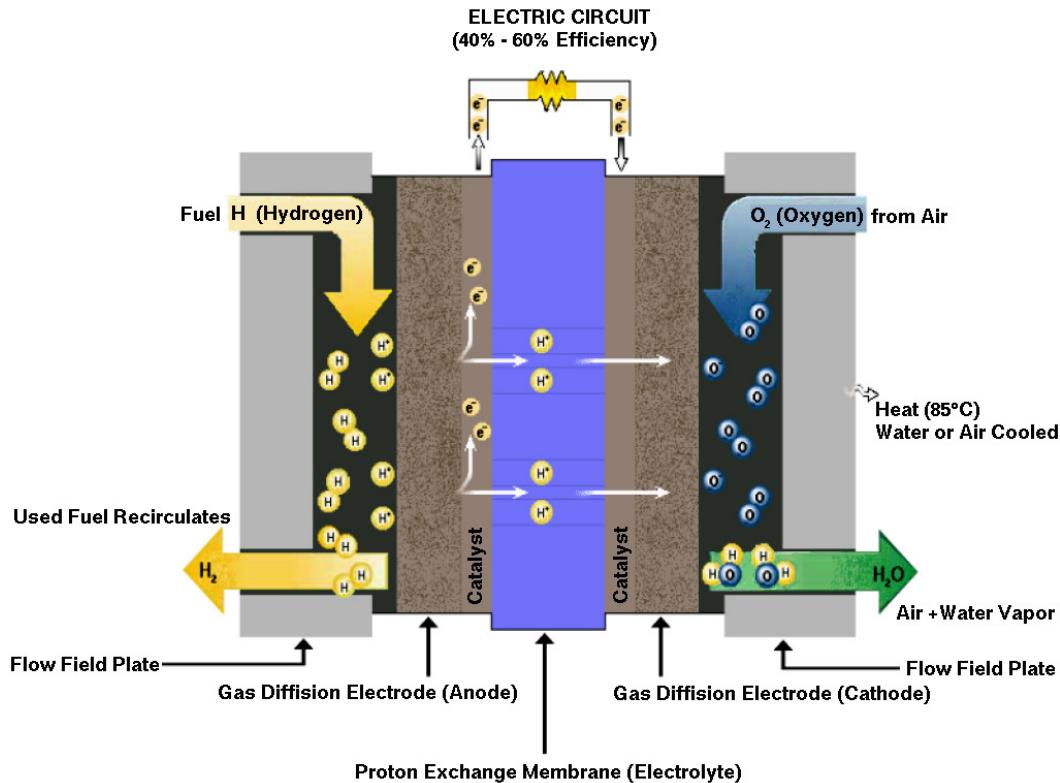
Kaiserslautern

# Porous Layers in a PEM Fuel Cell



- Gas Diffusion Layer
- Micro-porous Layer
- Catalyst Layer
- Membrane

# Porous Layers in a PEM Fuel Cell



- Gas Diffusion Layer

- Micro-porous Layer

- Catalyst Layer

- Membrane

Find layers with optimal properties!

Properties of a porous medium are influenced by

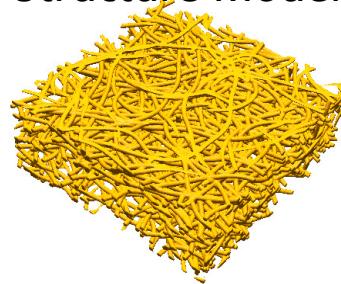
- Material

- Pore structure

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# **Virtual Material Design**

Structure Model



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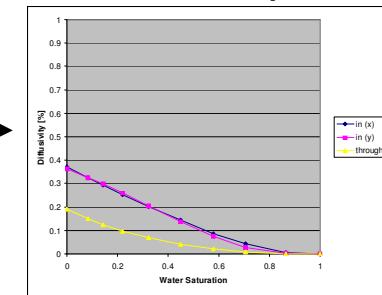
# Virtual Material Design

Structure Model



calculate

Effective Properties



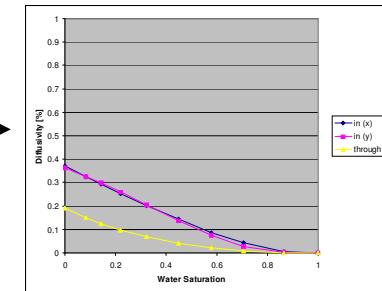
# Virtual Material Design

Structure Model



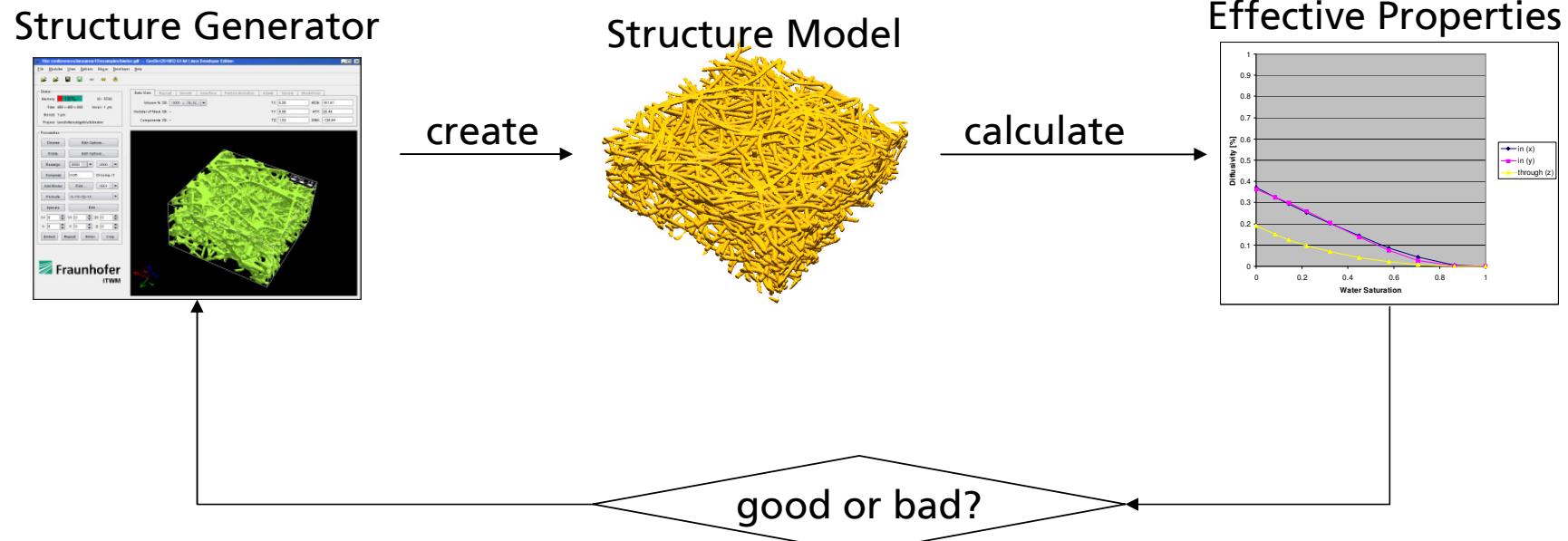
calculate

Effective Properties



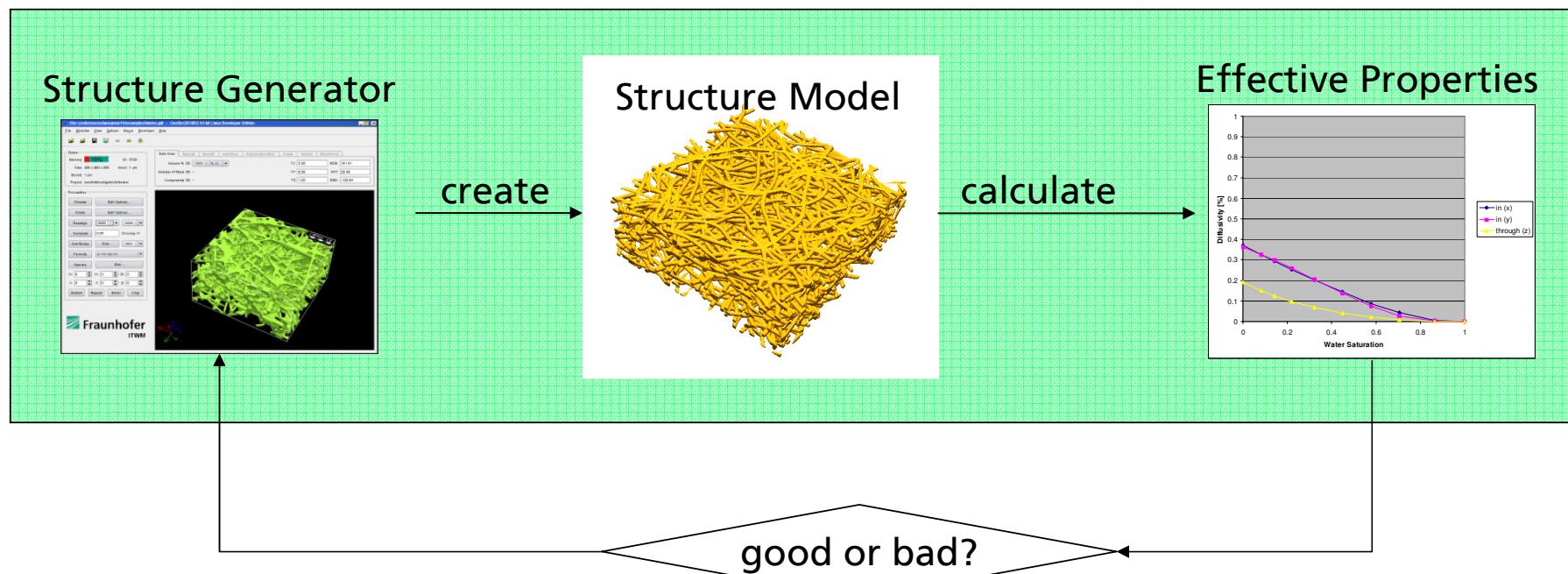
good or bad?

# Virtual Material Design



# Virtual Material Design

GEO DICT



 **Fraunhofer**  
ITWM

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# Outline

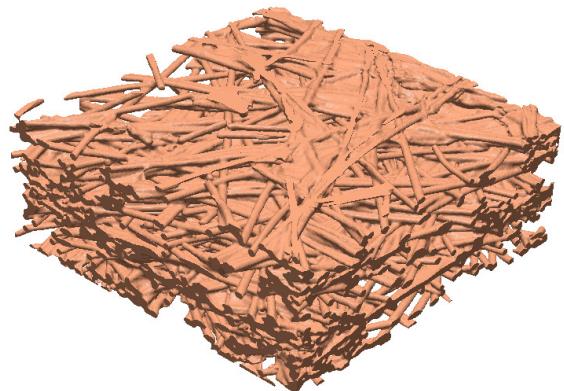
1. *Creation of 3D virtual structure models*
2. Determination of effective properties
3. Validation

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## 3D Structure Model

Two sources:

- 1) tomography image (segmentation)  
(needed for validation)



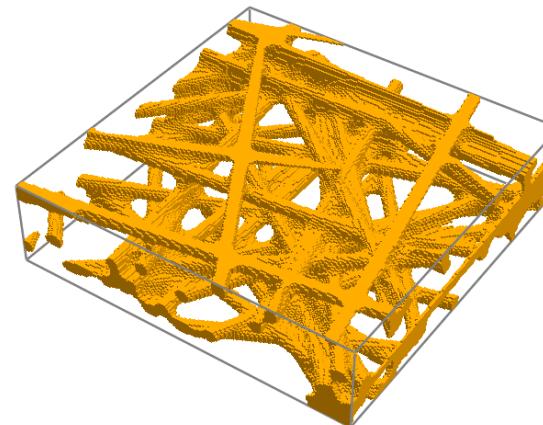
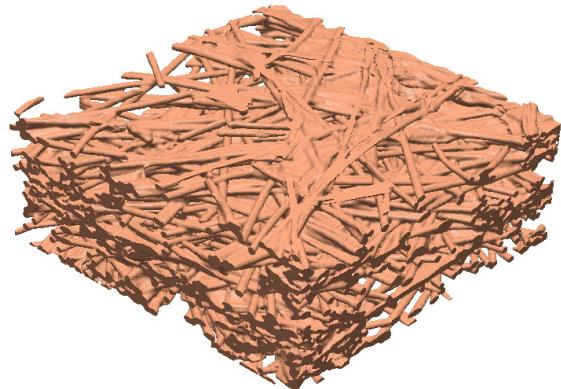
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## 3D Structure Model

Two sources:

1) tomography image (segmentation)  
(needed for validation)

2) virtually generated (stochastic geometry)  
(needed for virtual material design)



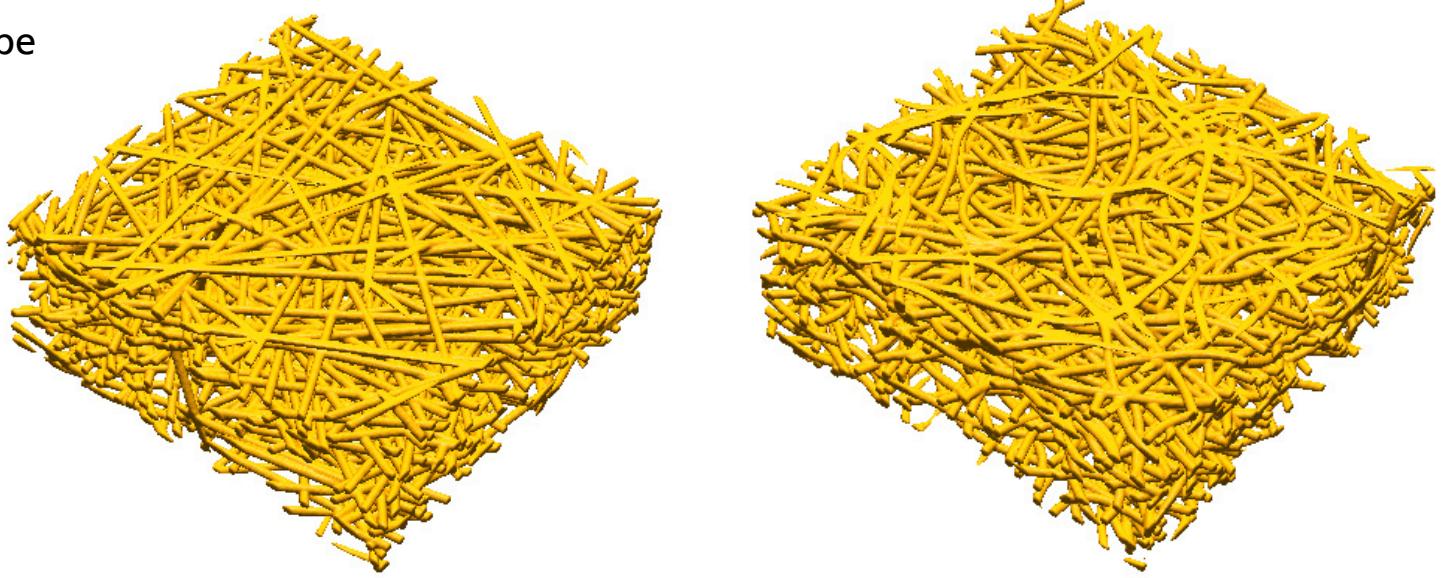
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## 3D Models: Gas Diffusion Layer (GDL)

Typically: nonwoven fibre structures plus binder

Input:

- Porosity
- Fibre diameter and type
- Anisotropy
- (Weight% binder)
- (Fibre crimp)



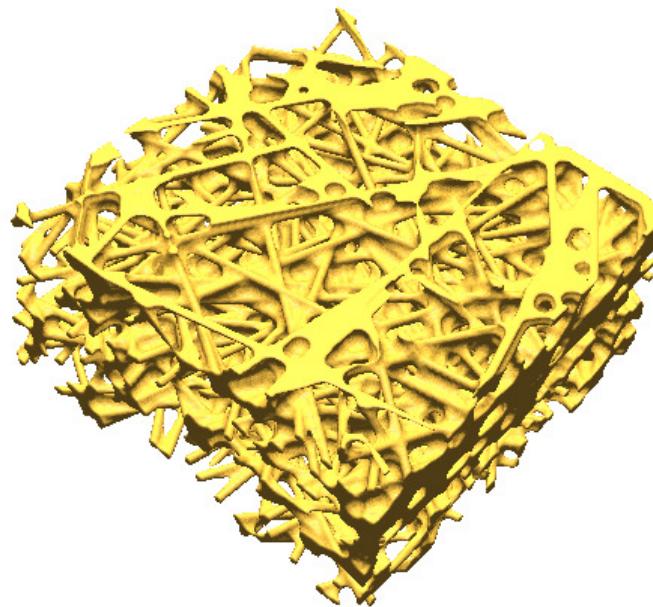
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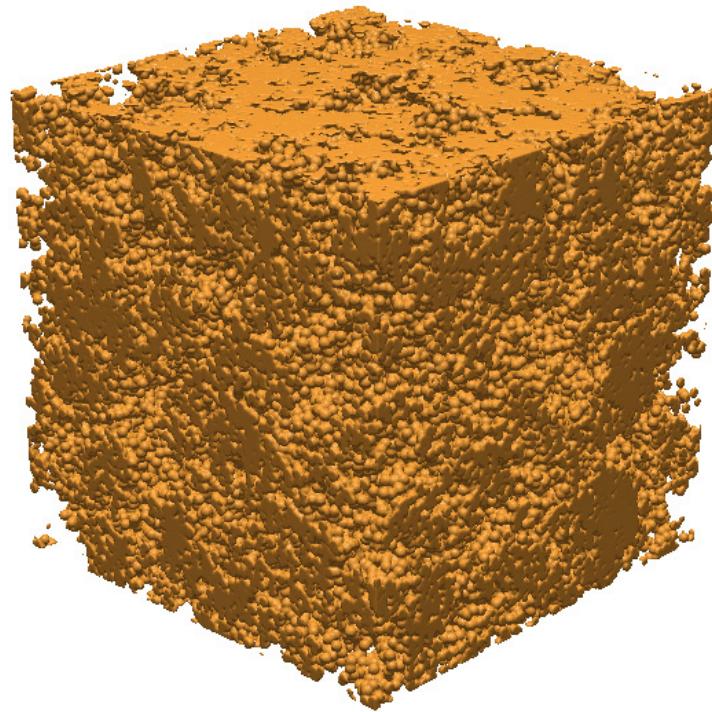
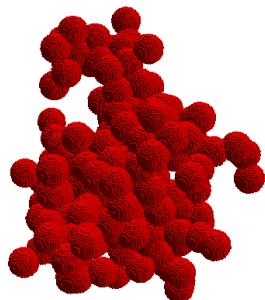
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## 3D Models: Microporous Layer (MPL)

Typically: carbon agglomerates

Input:

- Particle size
- Particles per Agglomerate
- Porosity



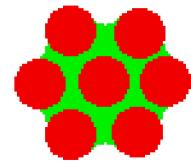
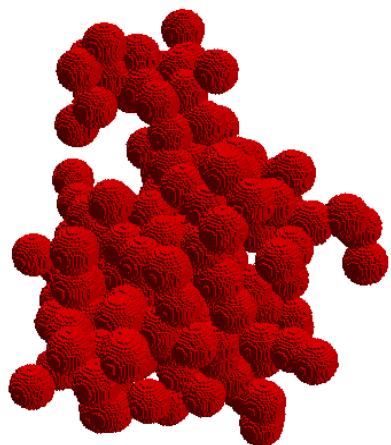
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*Becker, Wieser, Fell, Steiner, 2010, submitted*

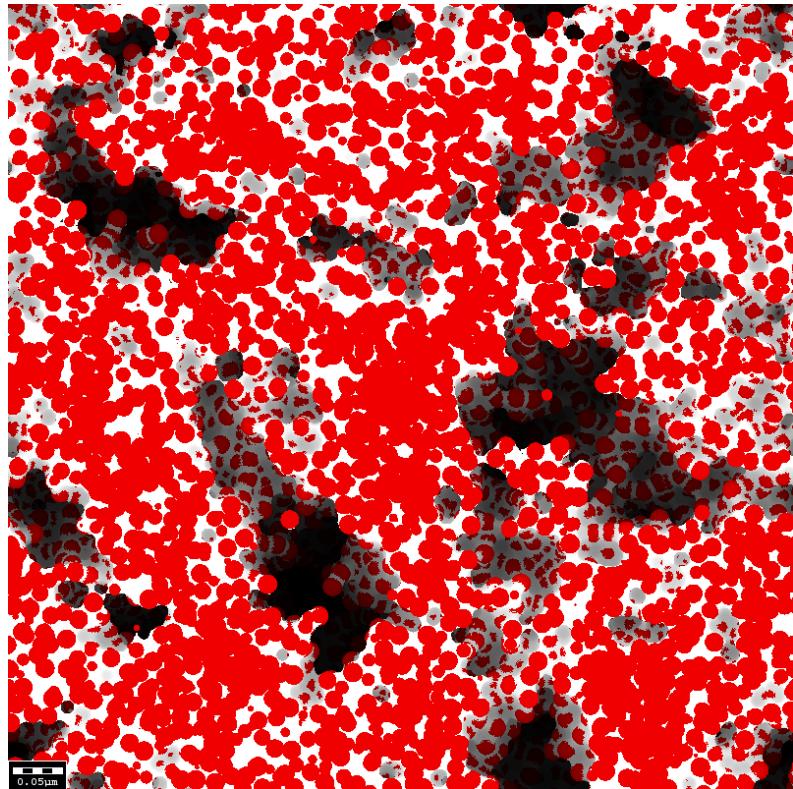
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## 3D Models: Catalyst Layer (CL)

Carbon agglomerates plus elektrolyte



Elekt. between  
C.Partikels



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# Outline

1. Creation of 3D virtual structure models
2. *Determination of effective properties*
3. Validation

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# Determination of Effective Properties

Common approach:

1. Start with a 3D voxel structure given
2. Find effective properties based on the geometrical structure
  - a) Geometrical properties:
    - pore size distribution, pore morphology, surface area
  - b) Transport properties:
    - i. Solve PDE on the voxel grid
    - ii. Find effective property by upscaling / averaging

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# Diffusivity

Macroscopic description (homogenized porous media model)

Fick's first law:  $j = -D^* \nabla c$

$D^*$  : effective diffusivity [ $\text{m}^2/\text{s}$ ] *unknown*

$j$  : diffusion flux [ $\text{mol}/\text{m}^2/\text{s}$ ]

$c$  : concentration [ $\text{mol}/\text{m}^3$ ]

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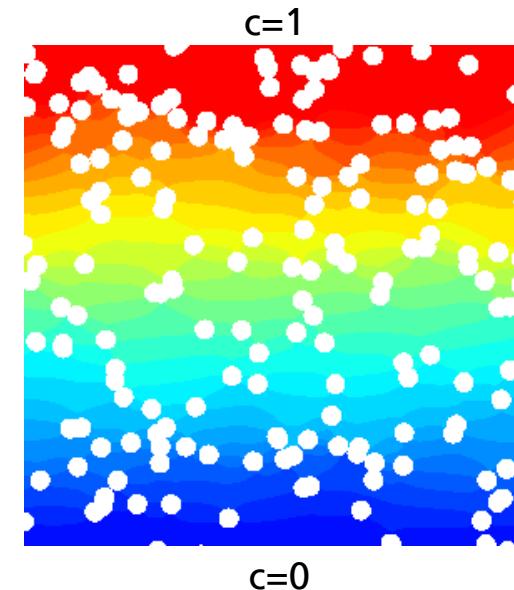
**Microscopic description (pore structure model)**

Laplace equation:

$$-\Delta c = 0$$

Boundary conditions: no-flux on fibre surface, concentration drop

$D^*$  can be determined from the solution!



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# Knudsen Diffusivity

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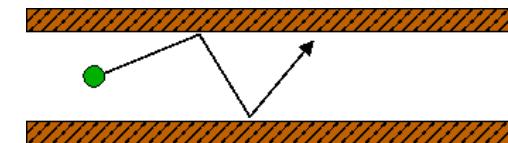
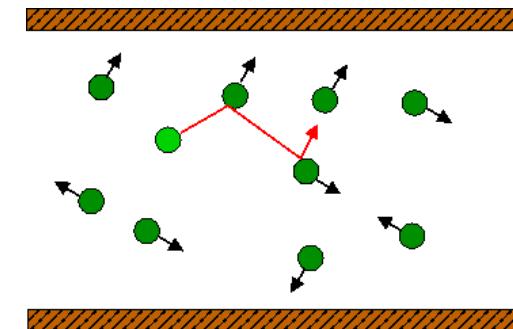
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## Diffusion mechanisms

1.  $\text{Kn} \ll 1$  (bulk diffusion)
  - Diffusion by particle-particle collisions
  - Mathematical model: Laplace equation
2.  $\text{Kn} \gg 1$  (Knudsen diffusion)
  - Diffusion by particle-wall collisions
  - Mathematical model: random walk methods
3.  $\text{Kn} \sim 1$  (transition regime diffusion)
  - Both mechanisms are present, Bosanquet:  $D = (D_{\text{bulk}}^{-1} + D_{\text{Kn}}^{-1})^{-1}$



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# Permeability

**Macroscopic description (homogenized porous media model)**

Darcy's law :

$$u = -\frac{1}{\mu} \kappa \nabla p$$

$u$  : average flow velocity

$\kappa$  : permeability tensor *unknown*

$\mu$  : viscosity

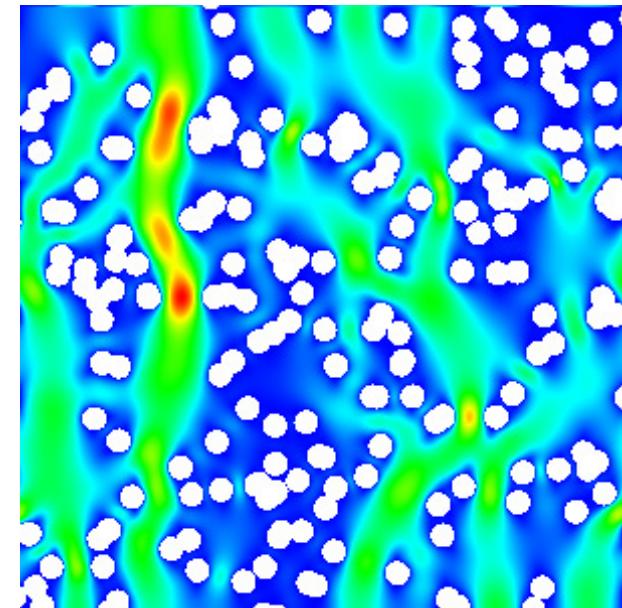
$p$  : pressure

**Microscopic description (pore structure model)**

Stokes equation:  $-\mu \Delta u + \nabla p = 0$

Boundary conditions: no-slip on fibre surface, pressure drop

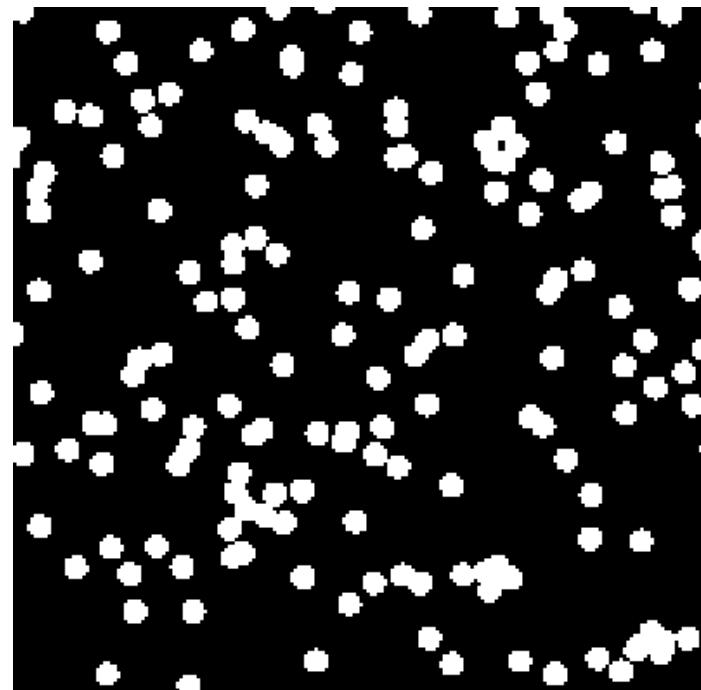
$\kappa$  can be determined from the solution!



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## Relative Permeability

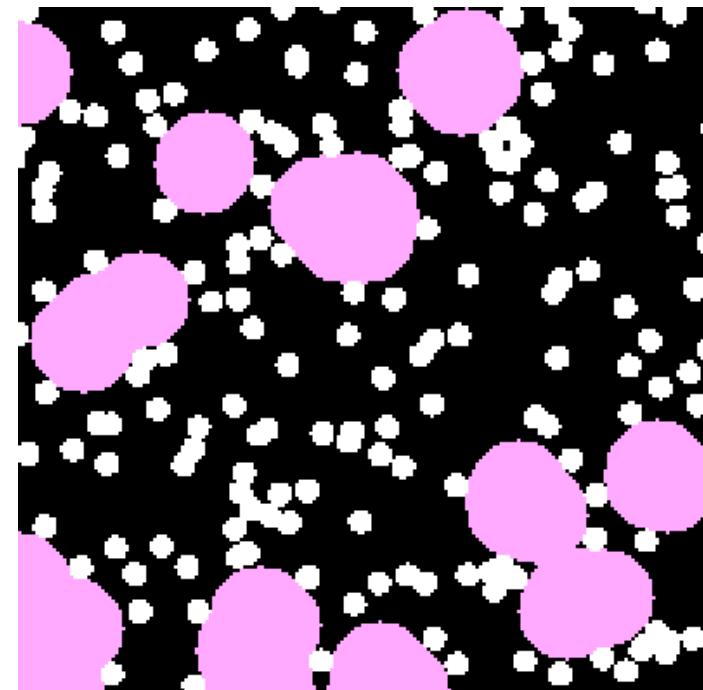
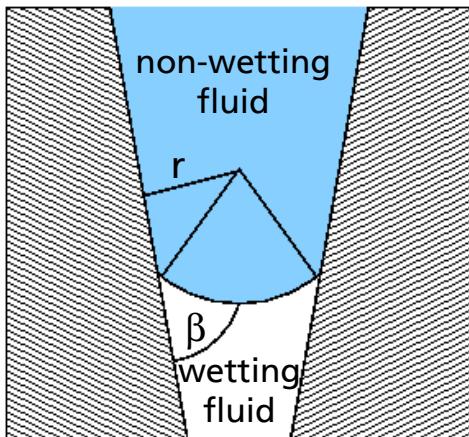
Two-step approach:



# Relative Permeability

Two-step approach:

1. Use pore morphology method (Hilpert, 2001) to determine distribution of air and water phase.
  - Idea: a pore is filled with the non-wetting fluid (=water), if  $p_c \geq \frac{2\sigma}{r} \cos \beta$

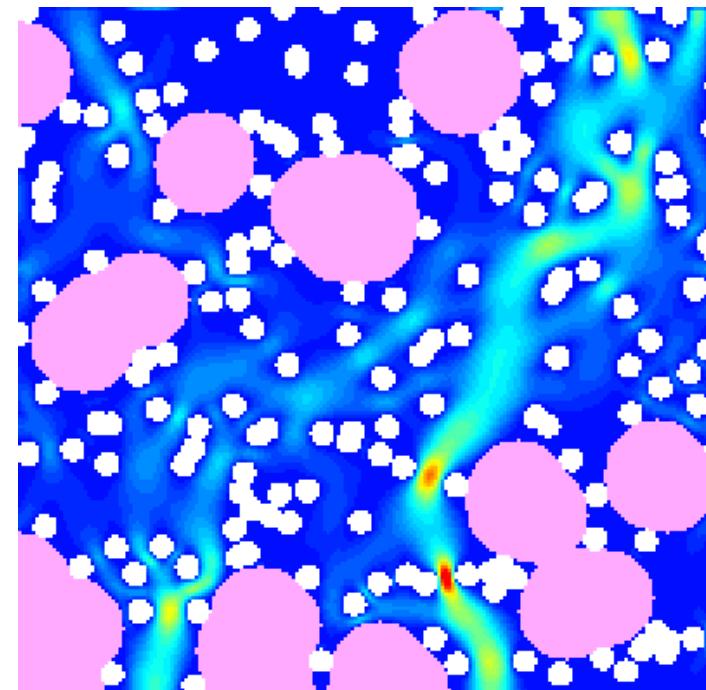


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  - Idea: a pore is filled with the non-wetting fluid (=water), if  $p_c \geq \frac{2\sigma}{r} \cos \beta$
2. Solve Stokes equation on the remaining pore space to determine wetting phase (=air) permeability



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# Properties Overview

GDL:

- (saturation dependent) diffusivity, (saturation dependent) permeability, electric conductivity, heat conductivity
- pore size distribution, capillary pressure curve

MPL

- (Knudsen) diffusivity, electric conductivity, heat conductivity
- pore size distribution

CL

- pore size distribution, surface or contact areas, contact lines
- protonic conductivity, electronic conductivity, (Knudsen) diffusivity

Results cannot be better than the 3D structure model permits.

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# Outline

1. Creation of 3D virtual structure models
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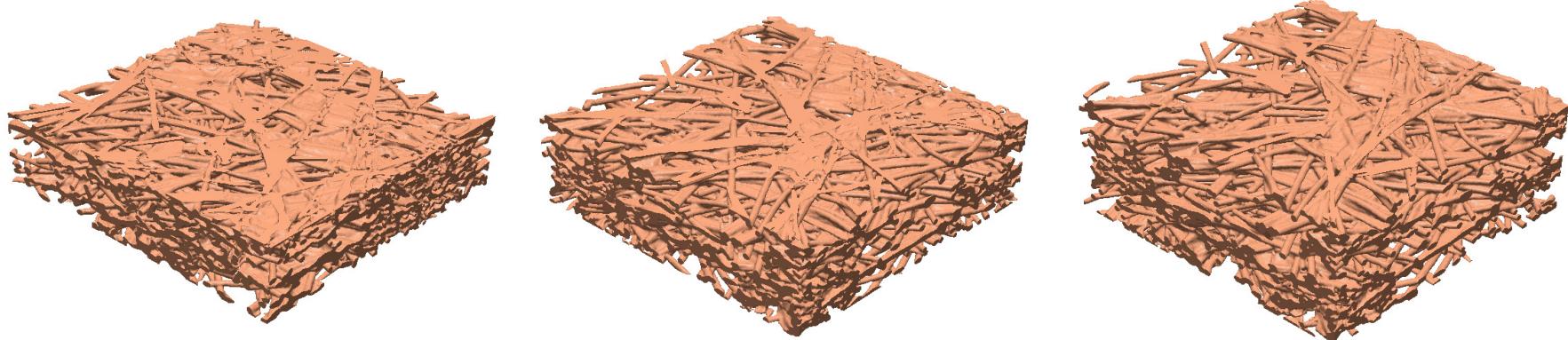
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## Validation: Toray TGP H 060 Gas Diffusion Layer

Data from PSI:

- Tomography images of Toray TGP H 060 at different compression levels
- Diffusivity, permeability and conductivity were measured at different compression levels experimentally

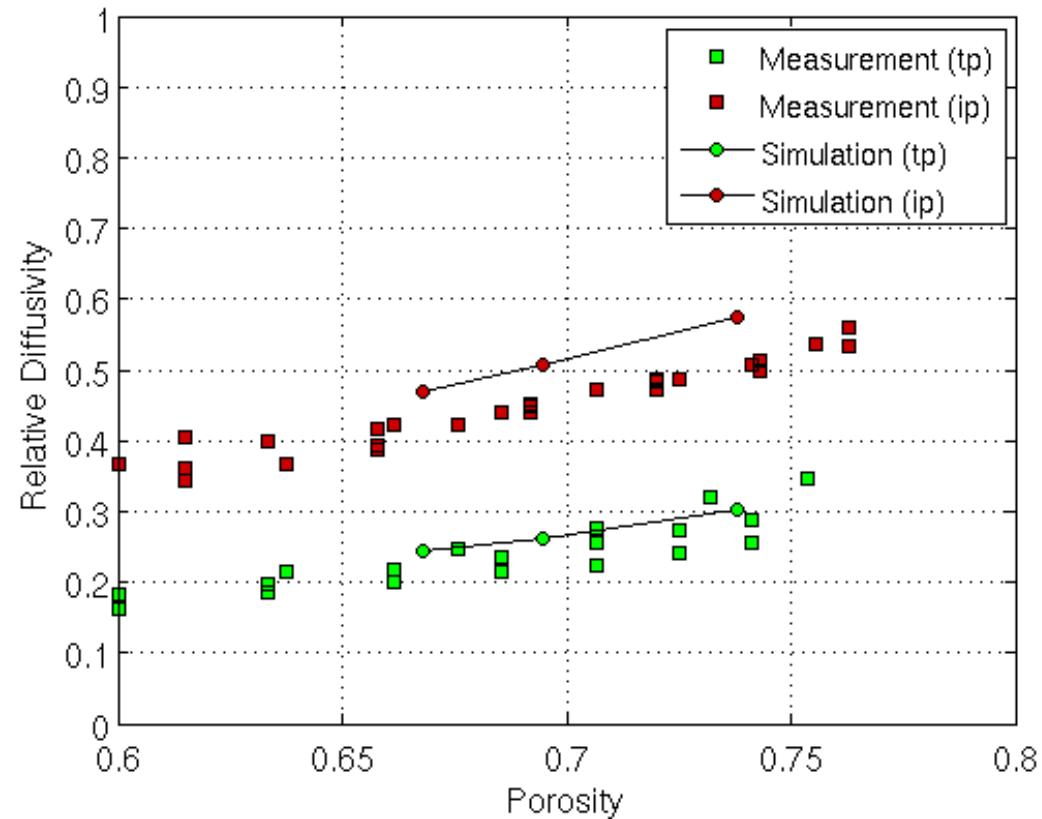
Now: compute diffusivity, permeability and conductivity numerically and compare results



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Becker, Flückiger, Reum, Büchi, Marone, Stampanoni, 2009, J. Electrochem. Soc. 156

# Diffusivity

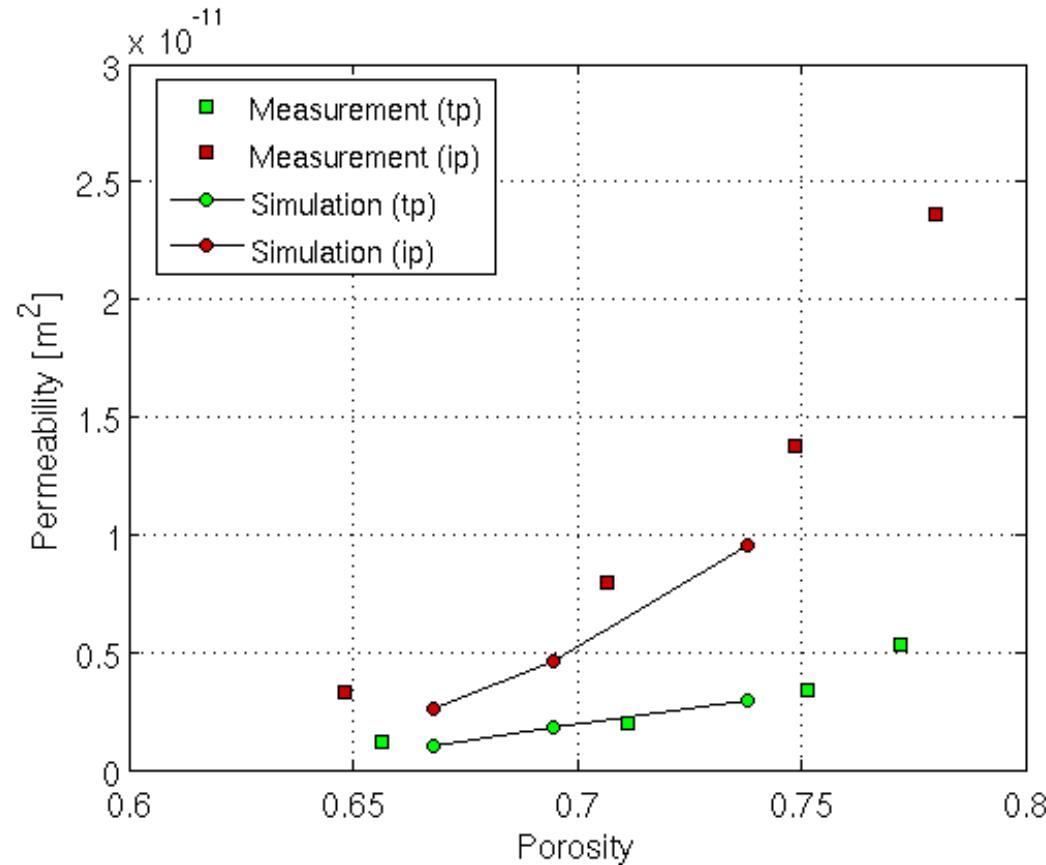


Perfect in tp-direction

Small differences in ip-direction

- ip-measurememts performed on a stack of GDLs
- tomography image shows single layer between sample holder

# Permeability



Perfect in tp-direction

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- ip-measurements performed on a stack of GDLs
- tomography image shows single layer between sample holder

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Thank You !



Geometry generator,  
property predictor and  
virtual material designer

[www.geodict.com](http://www.geodict.com)

BMBF project PemCaD

