
Pore Scale Modelling of Porous Layers in a PEFC

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Jürgen Becker

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Motivation

- MEA is an assembly of porous layers: GDL, MPL, CL, membrane
- Each layer needs to have optimal properties
- Properties of a porous medium are influenced by
 - Material
 - Pore structure

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Our goal: enable virtual material design!

Outline

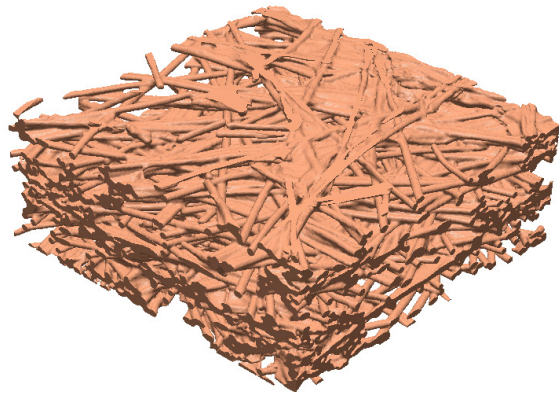
1. *Creation of 3D virtual structure models*
2. Determination of effective properties
3. Validation



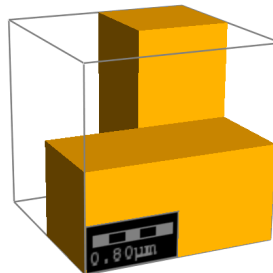
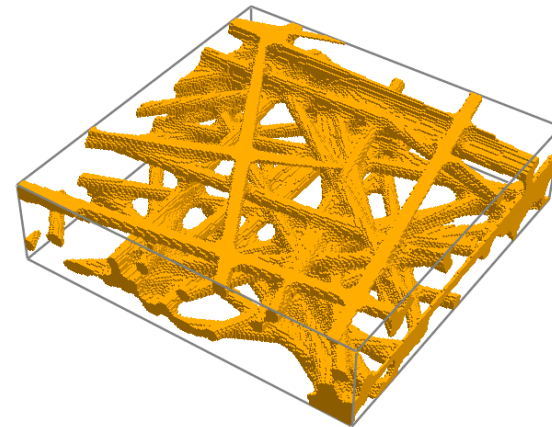
3D Structure Model

Two sources:

1) tomography image (segmentation)



2) virtually generated (stochastic geometry)



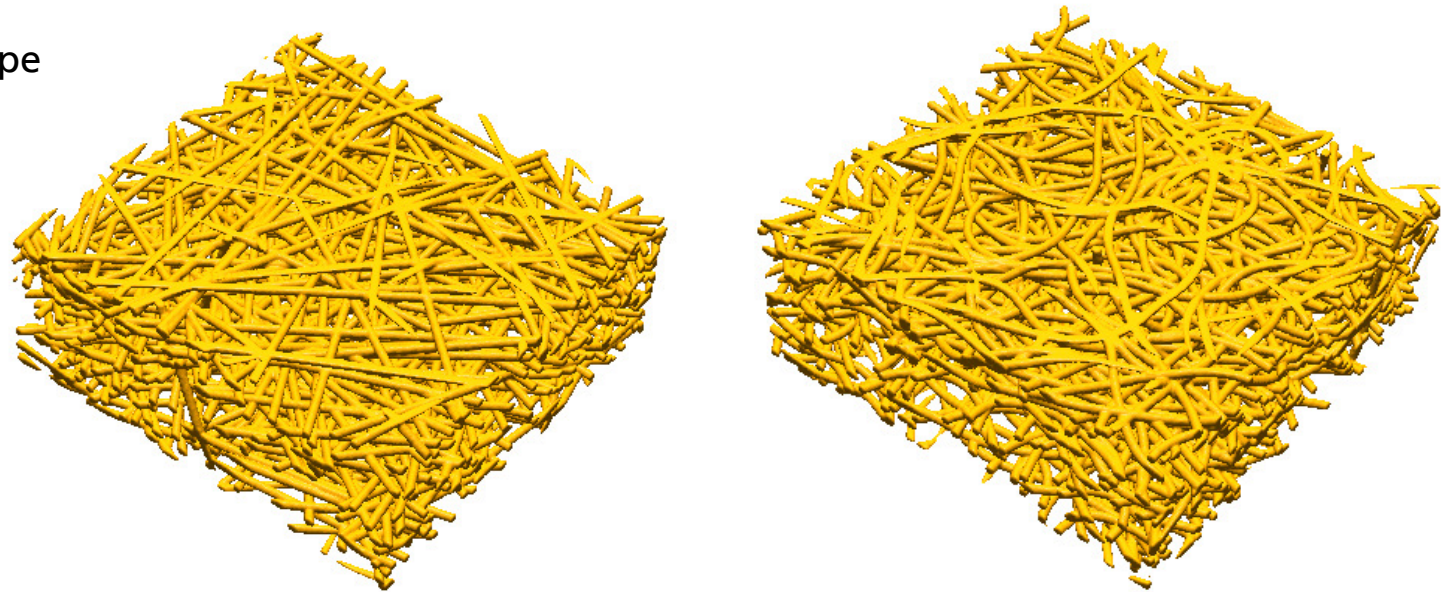
all structure models:
cubic voxels (voxel = volume pixel)

3D Models: Gas Diffusion Layer (GDL)

Typically: nonwoven fibre structures plus binder

Input:

- Porosity
- Fibre diameter and type
- Anisotropy
- (Weight% binder)
- (Fibre crimp)

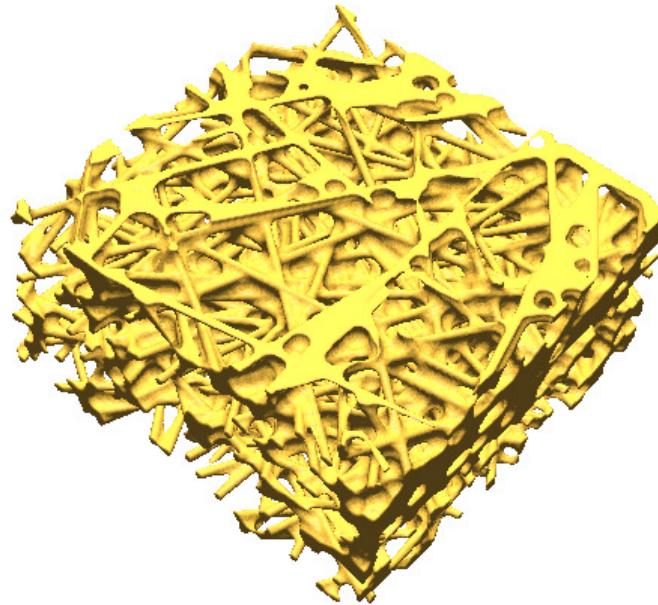


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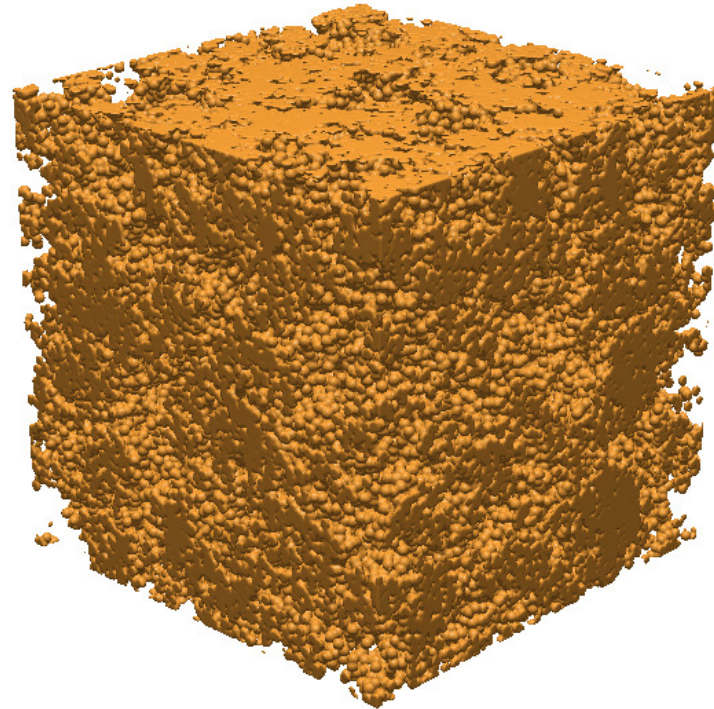
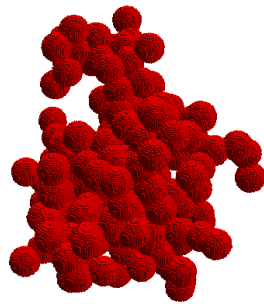


3D Models: Microporous Layer (MPL)

Typically: carbon agglomerates

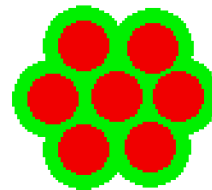
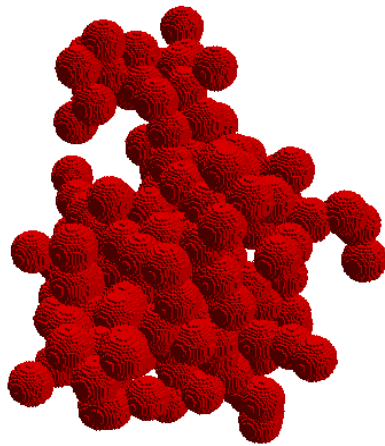
Input:

- Particle size
- Particles per Agglomerate
- Porosity

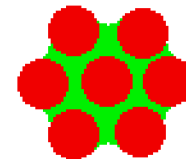


3D Models: Catalyst Layer (CL)

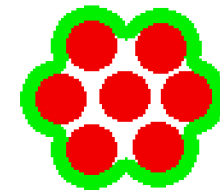
Carbon agglomerates plus electrolyte



Elekt. surrounds
C.Partikels



Elekt. between
C.Partikels



Elekt. surrounds
C.Partikels but
not in between

3D Models: Catalyst Layer (CL)

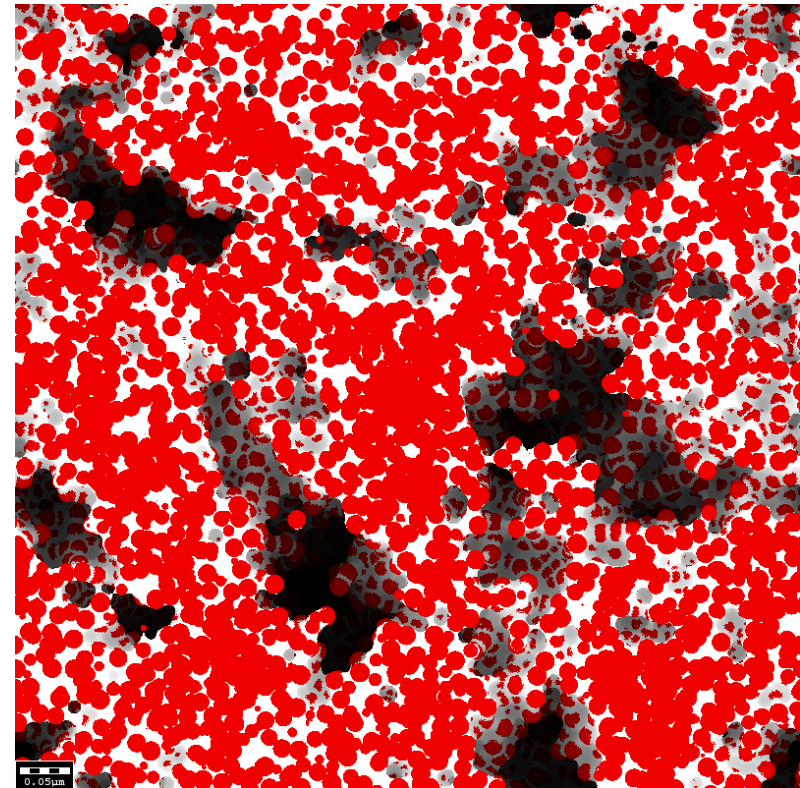
Model example:

Porosity 33.3 %

Carbon/Pt 50.1 vol%

Elektrolyte 16.6 vol%

Size: (800 nm)³, voxel length 1 nm



Outline

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Determination of Effective Properties

Common approach:

1. Start with a 3D voxel structure given
2. Find effective properties based on the geometrical structure
 - a) Geometrical properties:
 - pore size distribution, pore morphology, surface area
 - b) Transport properties:
 - i. Solve PDE on the voxel grid
 - ii. Find effective property by upscaling / averaging

Diffusivity

Macroscopic description (homogenized porous media model)

Fick's first law: $j = -D^* \nabla c$

D^* : effective diffusivity [m²/s] *unknown*

j : diffusion flux [mol/m²/s]

c : concentration [mol/m³]

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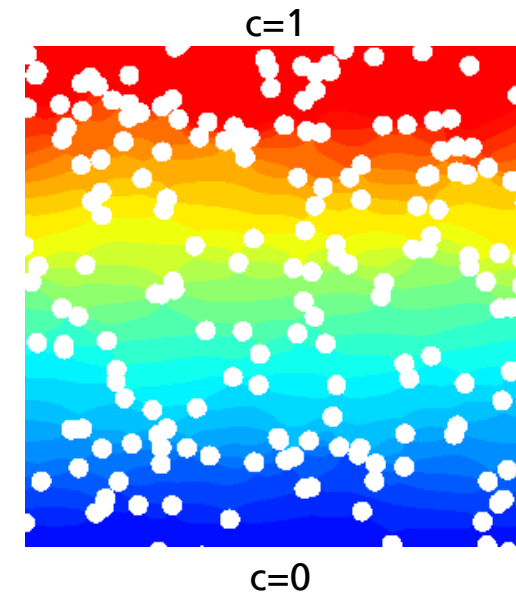
c : concentration [mol/m^3]

Microscopic description (pore structure model)

Laplace equation: $-\Delta c = 0$

Boundary conditions: no-flux on fibre surface, concentration drop

D^* can be determined from the solution!



Knudsen Diffusivity

Macroscopic description (homogenized porous media model)

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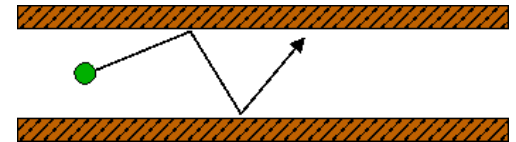
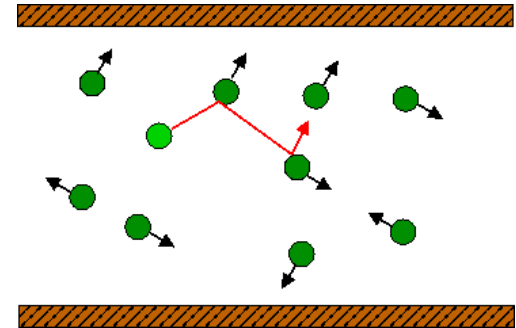
c : concentration [mol/m^3]

Diffusion mechanisms

1. $\text{Kn} \ll 1$ (bulk diffusion)
 - Diffusion by particle-particle collisions
 - Mathematical model: Laplace equation
2. $\text{Kn} \gg 1$ (Knudsen diffusion)
 - Diffusion by particle-wall collisions
 - Mathematical model: random walk methods

3. $\text{Kn} \sim 1$ (transition regime diffusion)

- Both mechanisms are present, Bosanquet: $D = \left(D_{bulk}^{-1} + D_{Kn}^{-1} \right)^{-1}$



Permeability

Macroscopic description (homogenized porous media model)

Darcy's law :
$$u = -\frac{1}{\mu}\kappa\nabla p$$

u : average flow velocity

κ : permeability tensor *unknown*

μ : viscosity

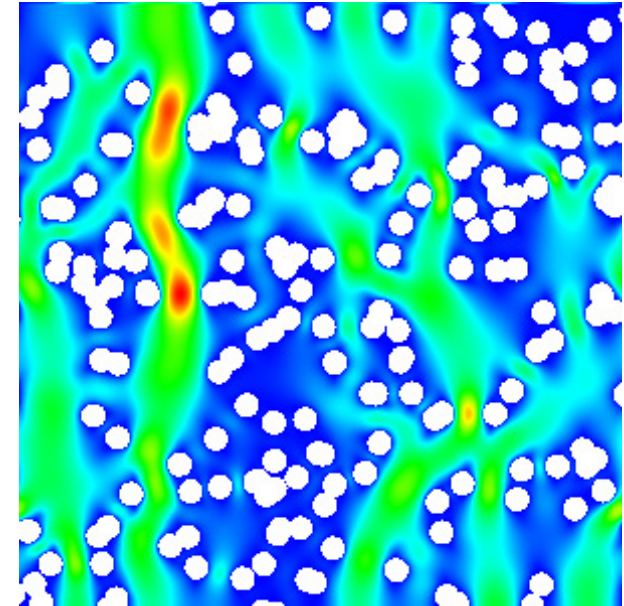
p : pressure

Microscopic description (pore structure model)

Stokes equation: $-\mu\Delta u + \nabla p = 0$

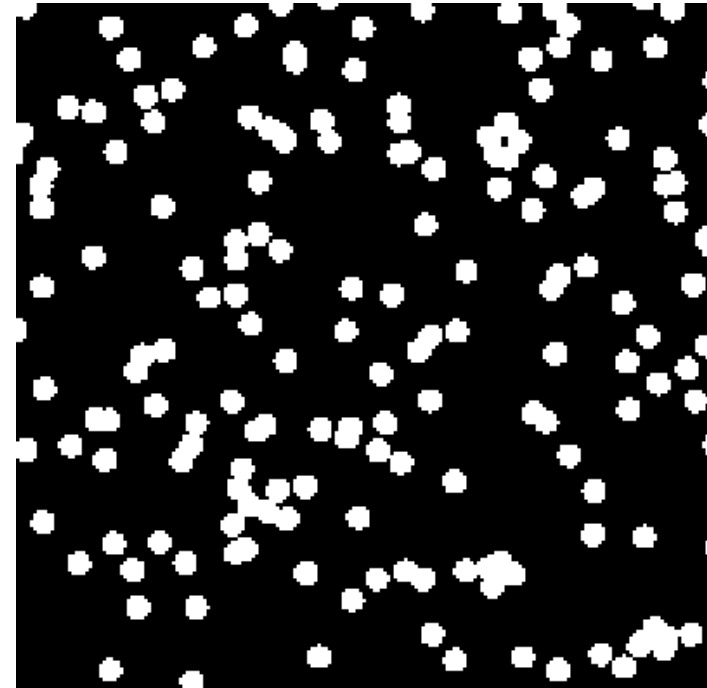
Boundary conditions: no-slip on fibre surface, pressure drop

κ can be determined from the solution!



Relative Permeability

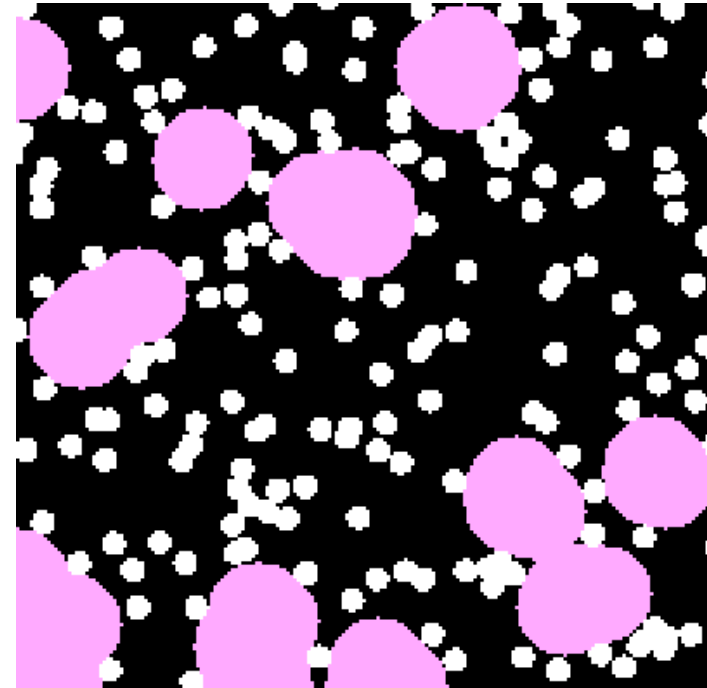
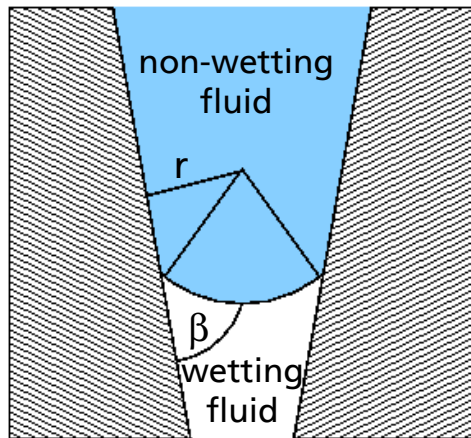
Two-step approach:



Relative Permeability

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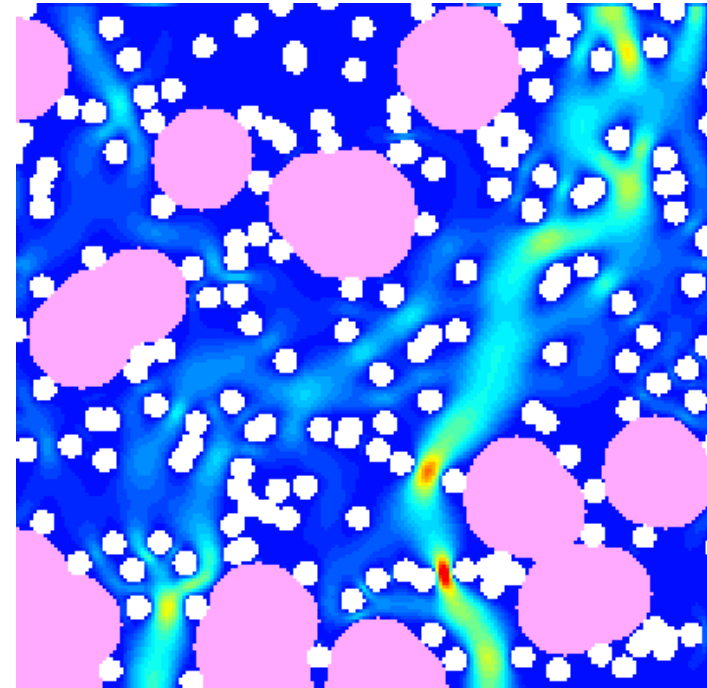
1. Use pore morphology method (Hilpert, 2001) to determine distribution of air and water phase.
 - Idea: a pore is filled with the non-wetting fluid (=water), if $p_c \geq \frac{2\sigma}{r} \cos \beta$



Relative Permeability

Two-step approach:

1. Use pore morphology method (Hilpert, 2001) to determine distribution of air and water phase.
 - Idea: a pore is filled with the non-wetting fluid (=water), if $p_c \geq \frac{2\sigma}{r} \cos \beta$
2. Solve Stokes equation on the remaining pore space to determine wetting phase (=air) permeability



Properties Overview

GDL:

- (saturation dependent) diffusivity, (saturation dependent) permeability, electric conductivity, heat conductivity
- pore size distribution

MPL

- (Knudsen) diffusivity, electric conductivity, heat conductivity
- pore size distribution

CL

- pore size distribution, surface or contact areas, contact lines
- protonic conductivity, electronic conductivity, (Knudsen) diffusivity

Results cannot be better than the 3D structure model permits.

Outline

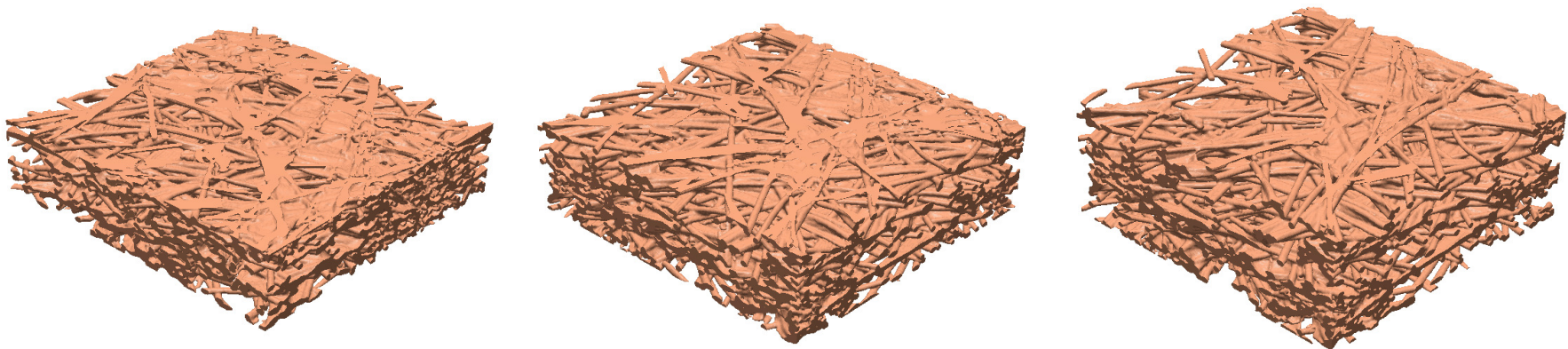
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Validation: Toray TGP H 060 Gas Diffusion Layer

Data from PSI:

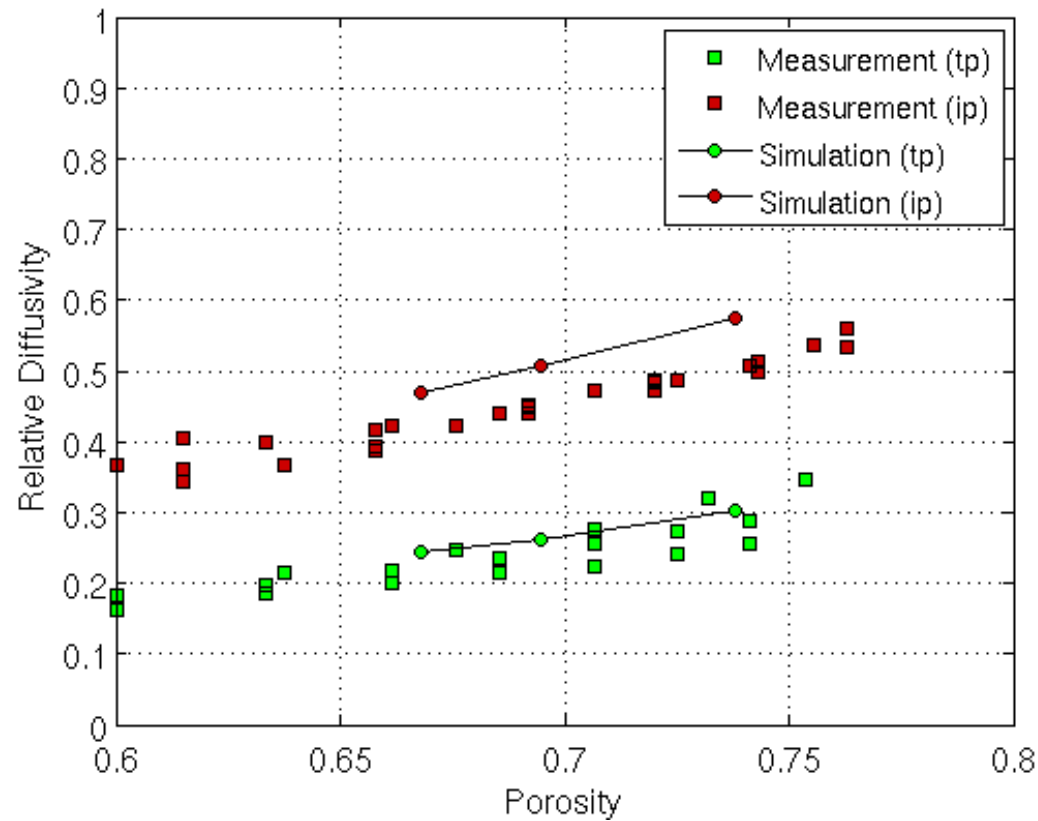
- Tomography images of Toray TGP H 060 at different compression levels
- Diffusivity, permeability and conductivity were measured at different compression levels experimentally

Now: compute diffusivity, permeability and conductivity numerically and compare results



Becker, Flückiger, Reum, Büchi, Marone, Stampanoni, 2009, J. Electrochem. Soc. 156

Diffusivity

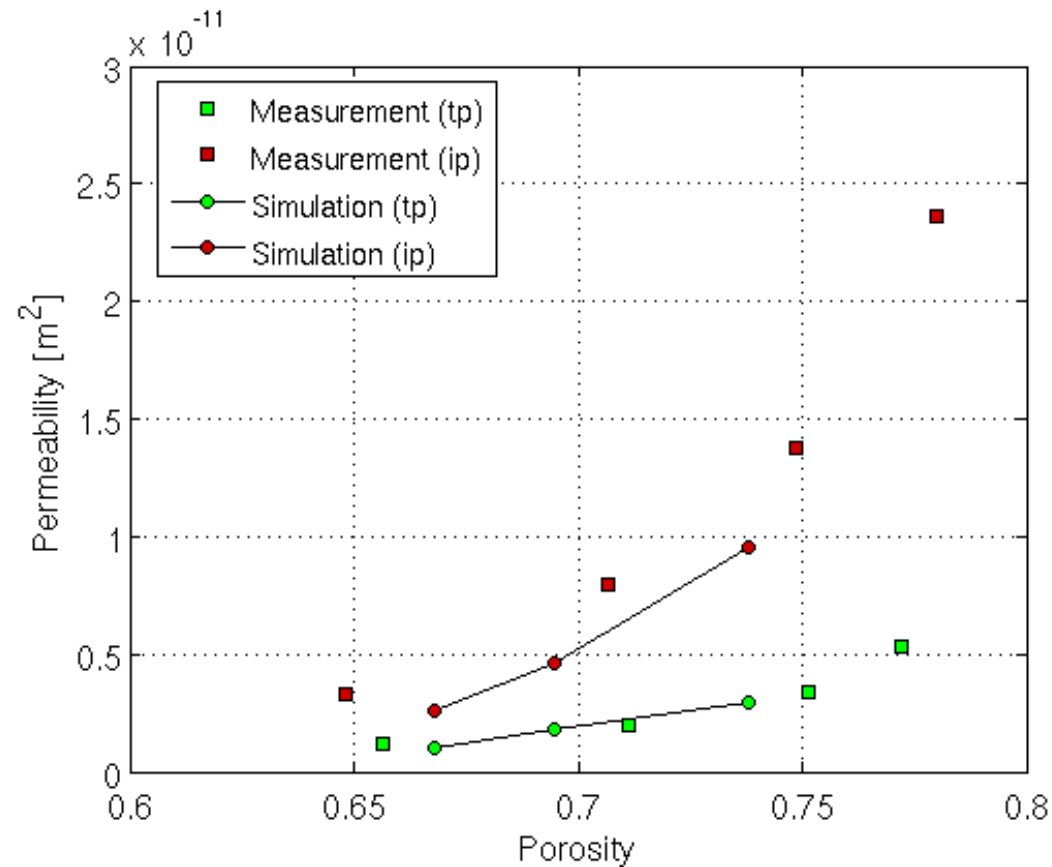


Perfect in tp-direction

Small differences in ip-direction

- ip-measurements performed on a stack of GDLs
- tomography image shows single layer between sample holder

Permeability



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Small differences in ip-direction

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- tomography image shows single layer between sample holder

Thank You !



Geometry generator,
property predictor and
virtual material designer

www.geodict.com

BMBF project PemCaD

