
Predicting Transport Properties of Porous Layers Based on Pore-Scale Models

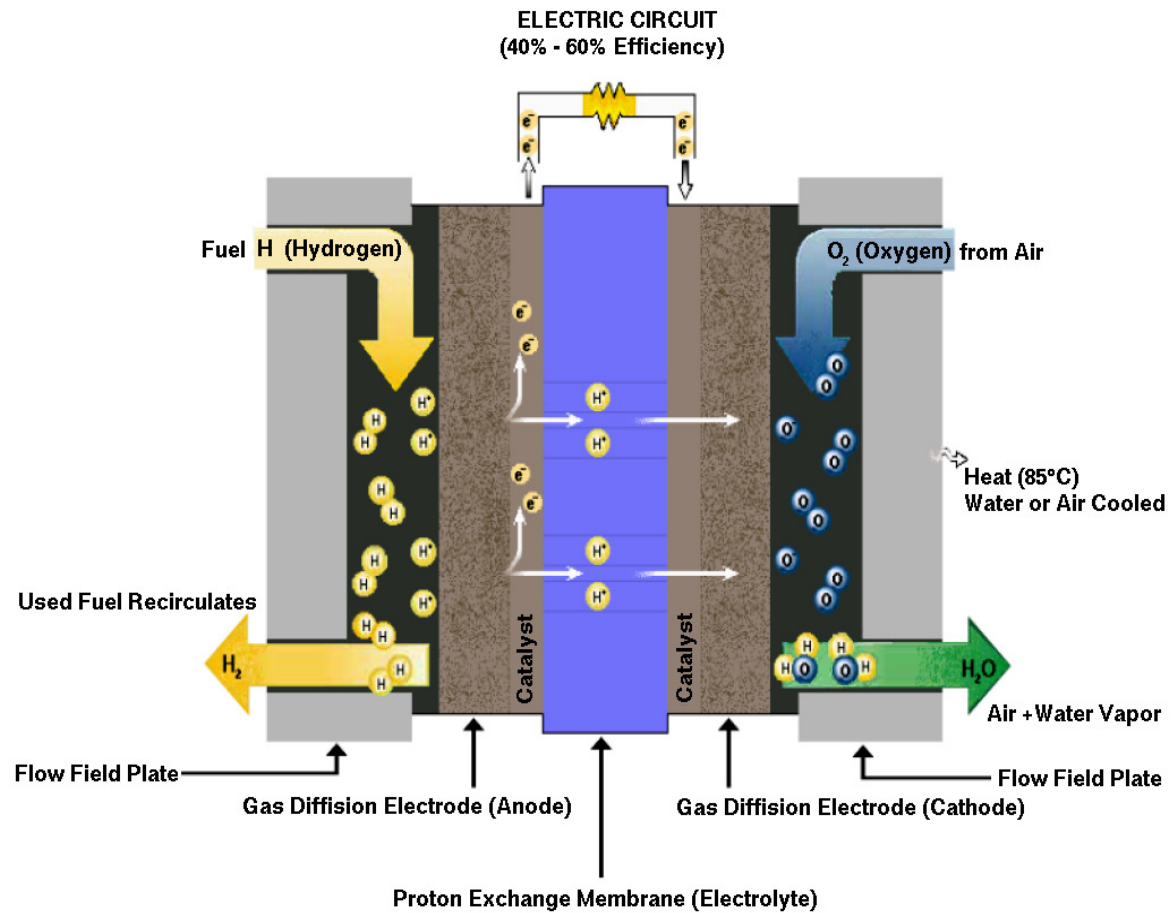
Transpore, Villigen, 19.08.2010

Jürgen Becker, Andreas Wiegmann

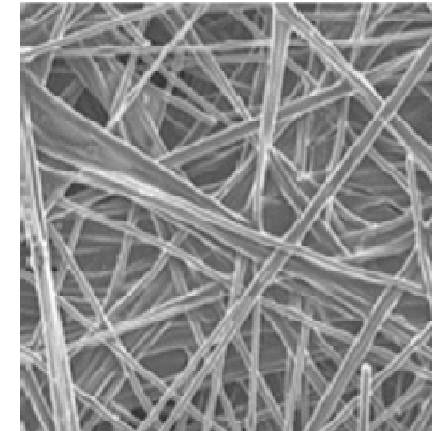
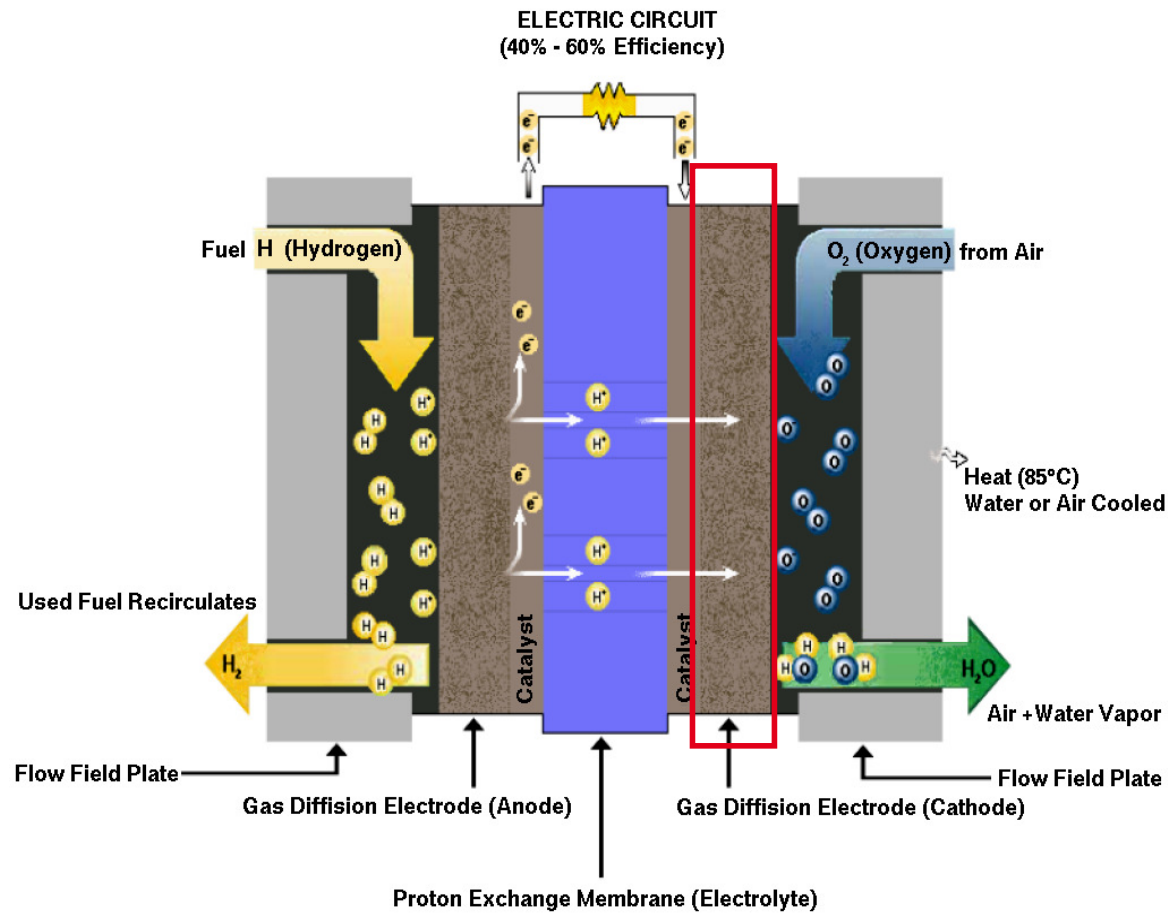
Fraunhofer Institute for Industrial Mathematics ITWM

Kaiserslautern, Germany

PEM Fuel Cell

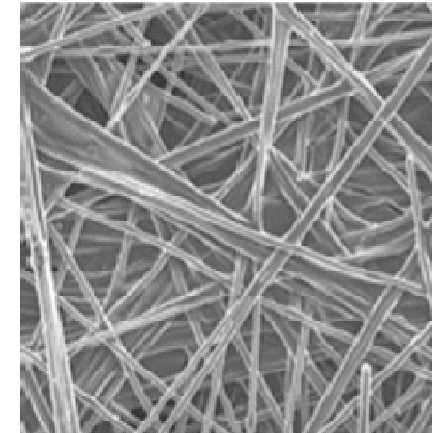
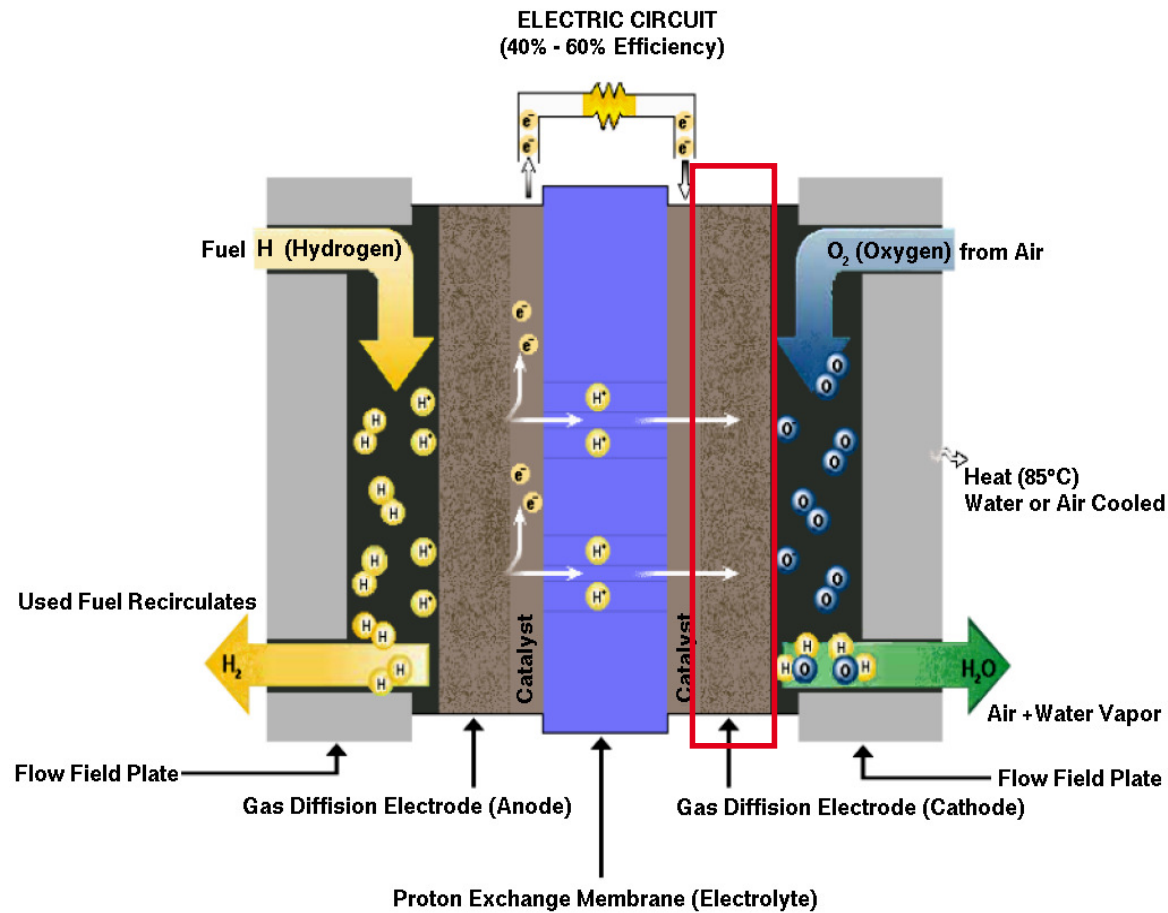


PEM Fuel Cell



Gas Diffusion layer

PEM Fuel Cell



Gas Diffusion layer

Aim: engineer a better GDL !

Better ?

- higher conductivity
- higher diffusivity
- higher stability
- ??

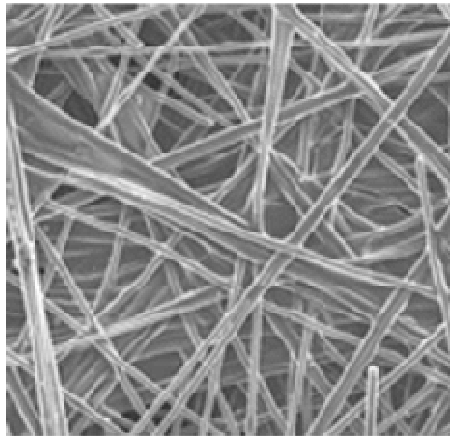
Predicting Transport Properties of Porous Layers Based on Pore-Scale Models

1. General Approach
2. Application to PEM fuel cells
 - Gas Diffusion Layer
 - Catalyst Layer

Aim: Virtual Material Design

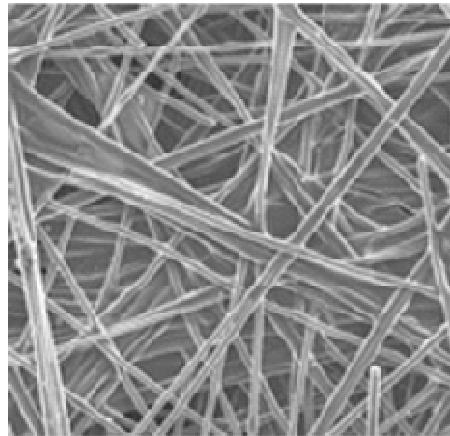
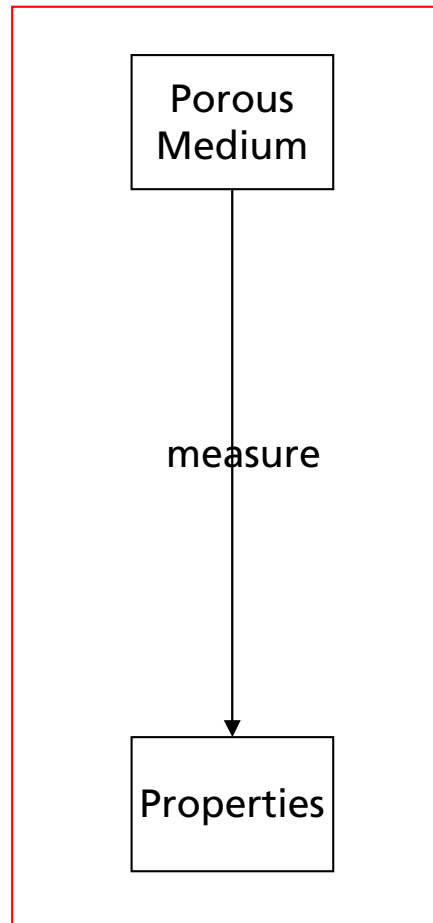
Lab

Porous
Medium



Aim: Virtual Material Design

Lab

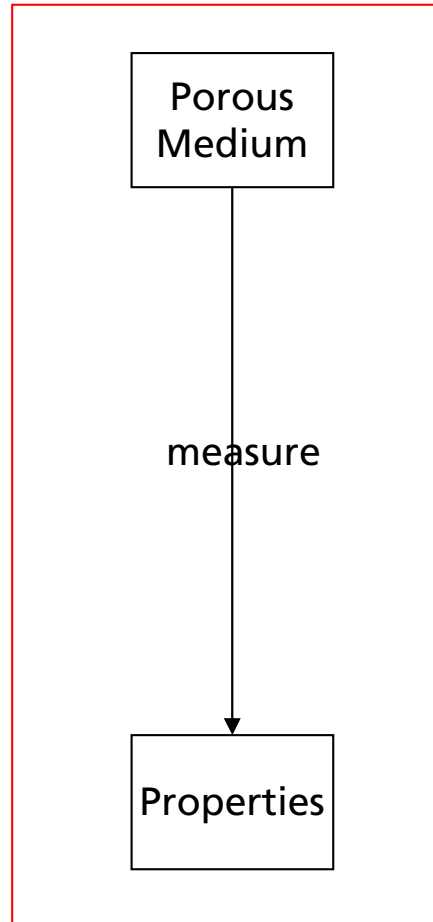


Properties are:

- pore size distribution
- permeability
- diffusivity
- cap. pressure curve
- ...

Aim: Virtual Material Design

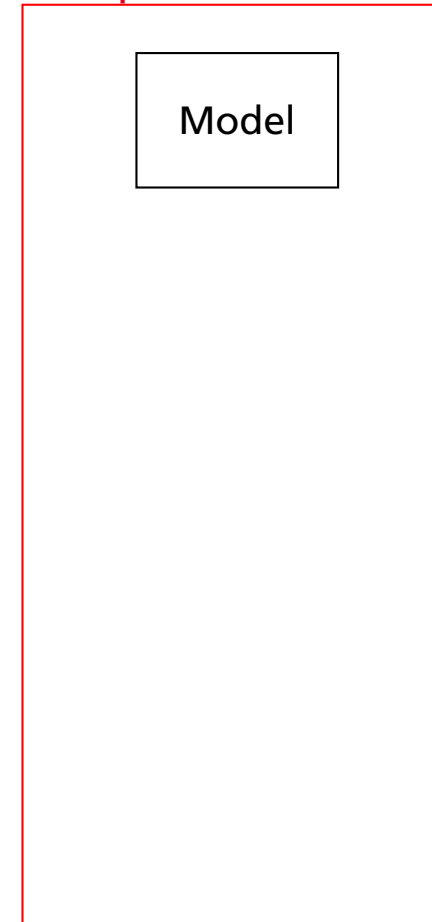
Lab



Properties are:

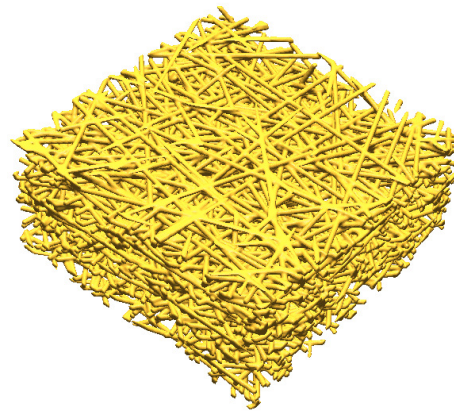
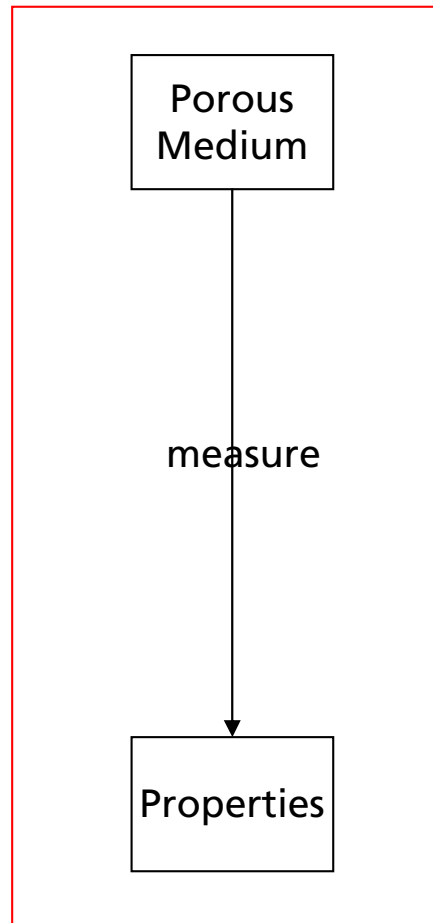
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Computer



Aim: Virtual Material Design

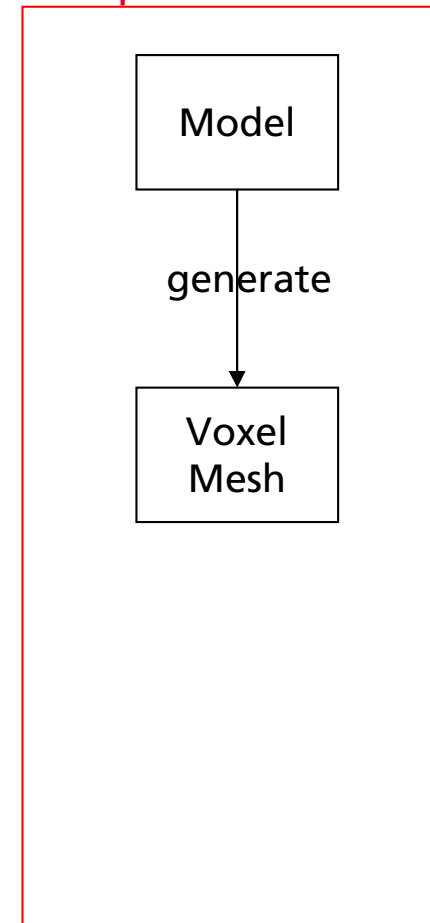
Lab



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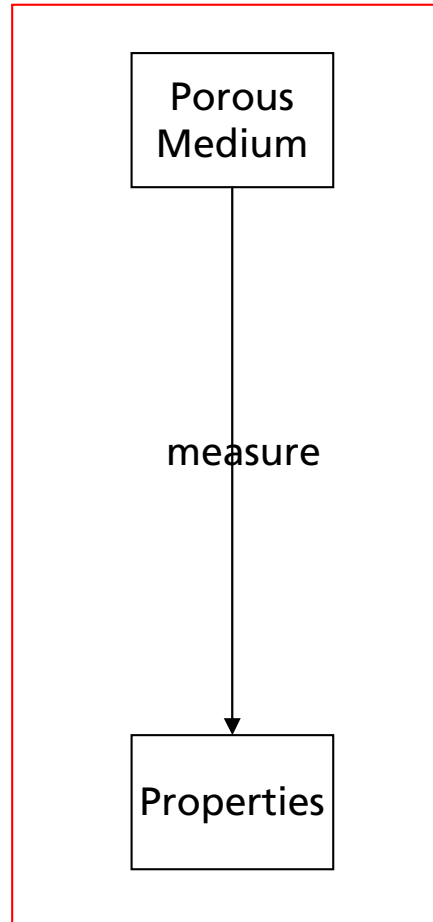
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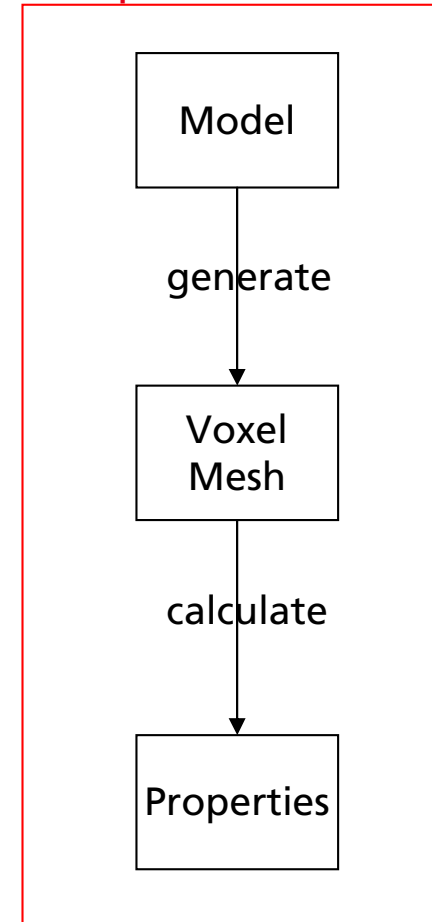
Lab



Properties are:

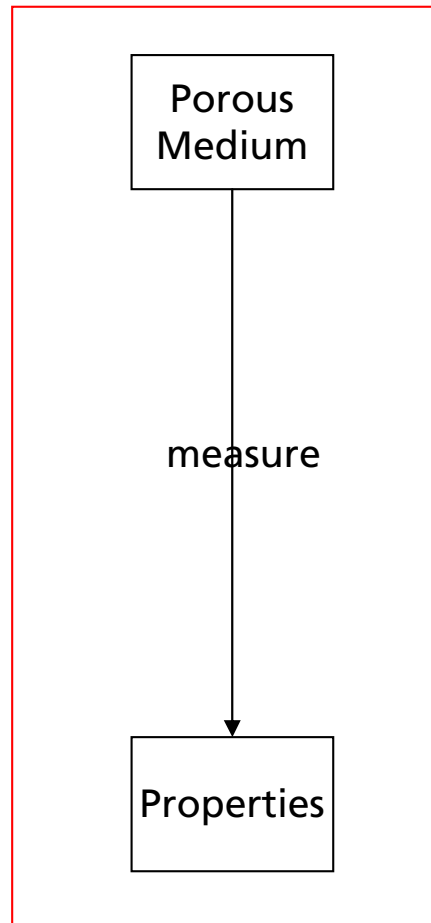
- pore size distribution
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Computer



Aim: Virtual Material Design

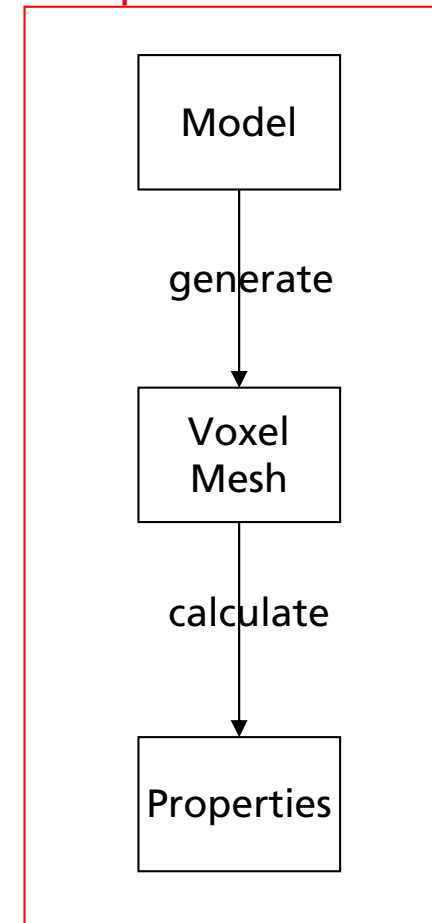
Lab



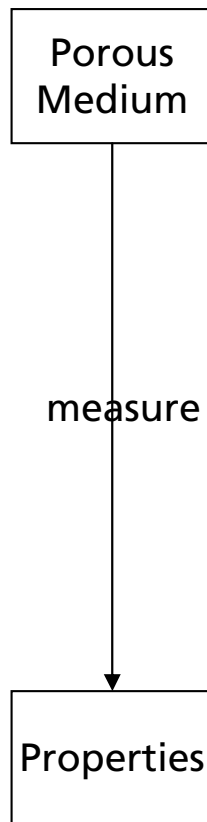
?

- Properties are:
- pore size distribution
 - permeability
 - diffusivity
 - cap. pressure curve
 - ...

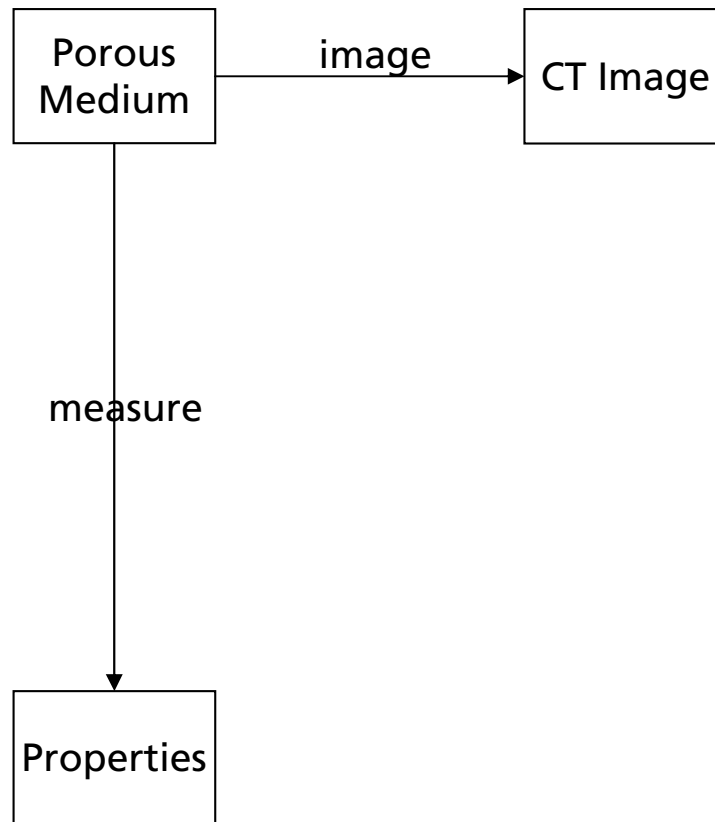
Computer



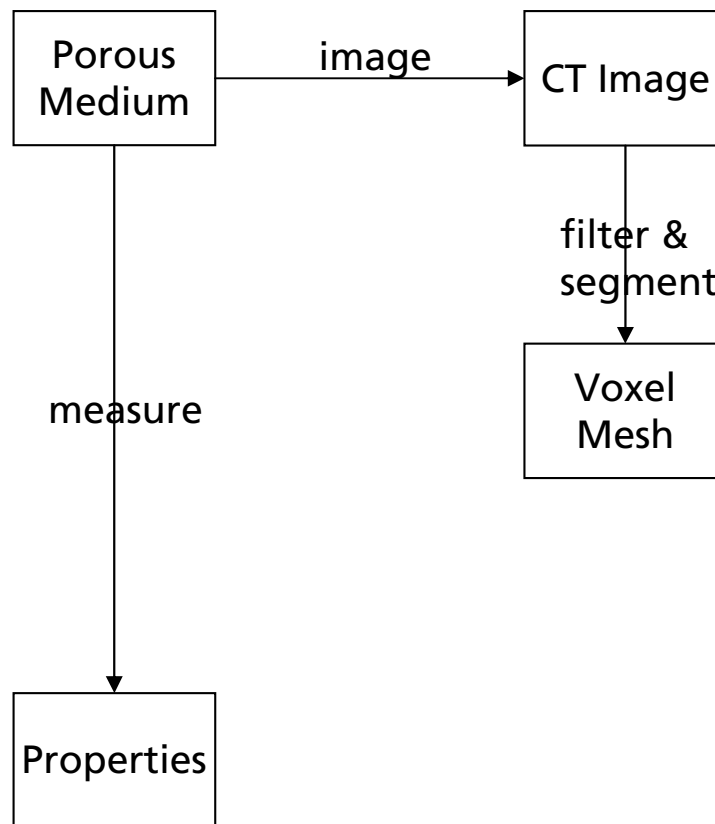
Bridge the Gap - Step 1: Validate Calculations



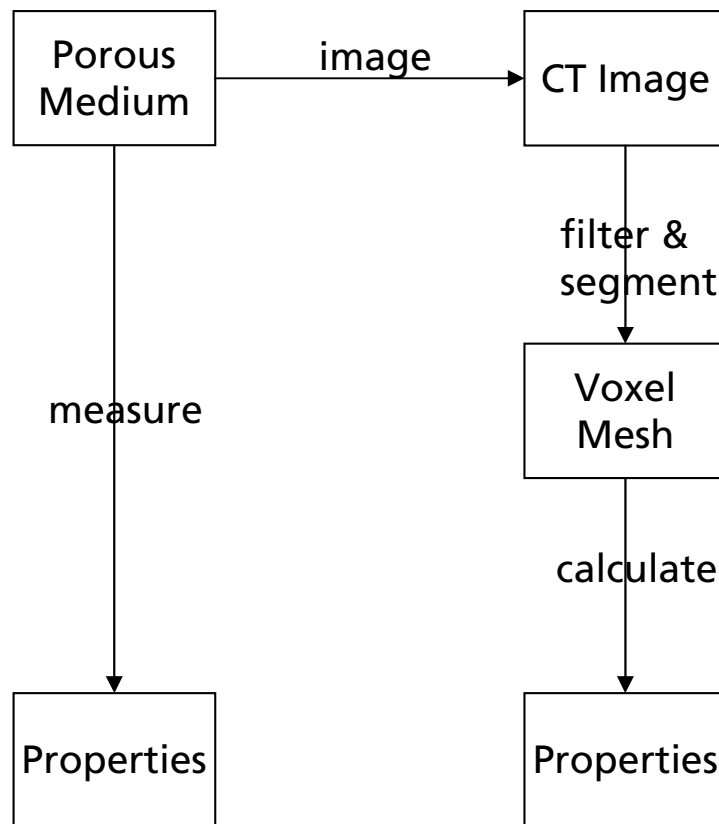
Bridge the Gap - Step 1: Validate Calculations



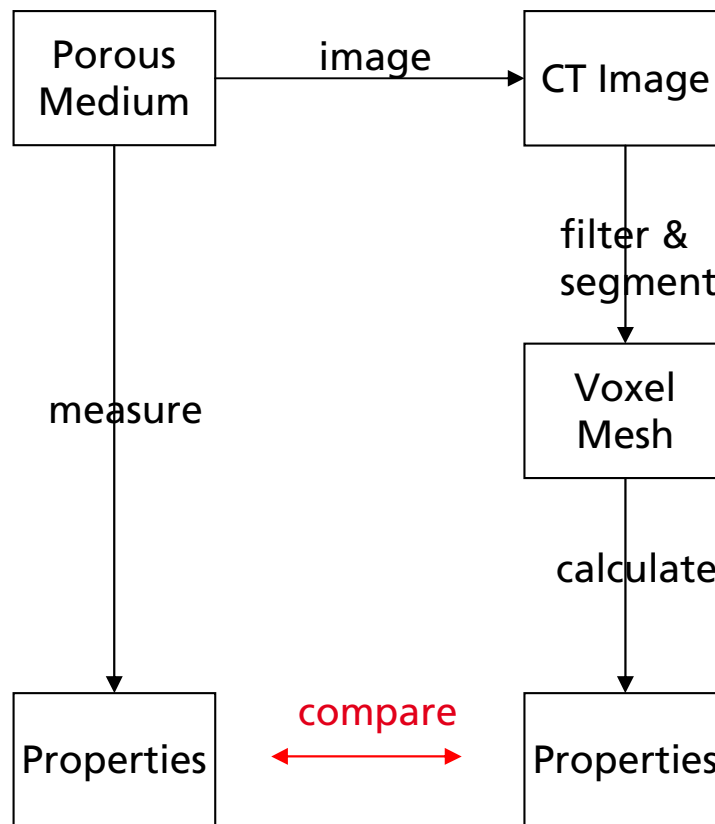
Bridge the Gap - Step 1: Validate Calculations



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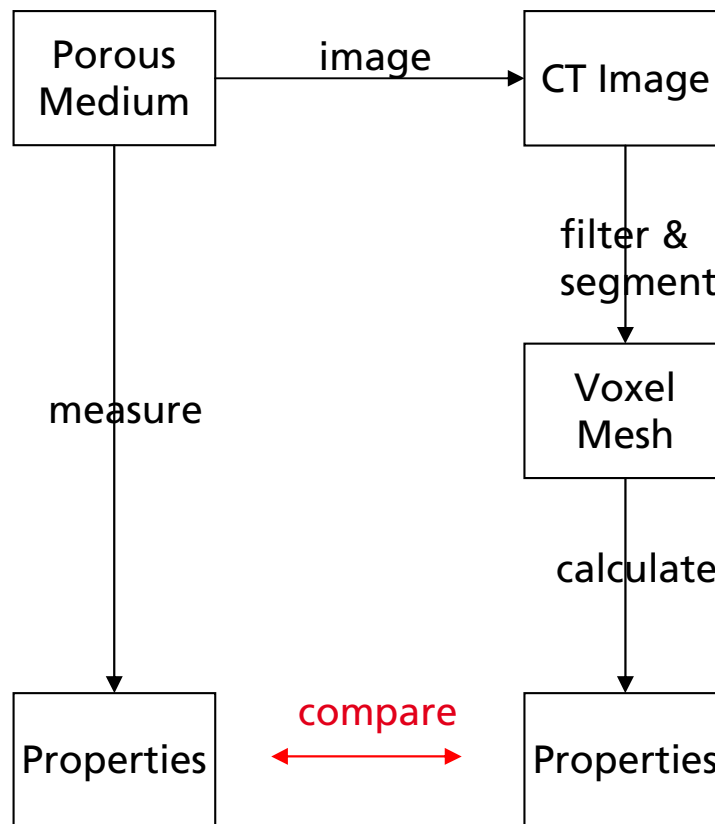
Bridge the Gap - Step 1: Validate Calculations



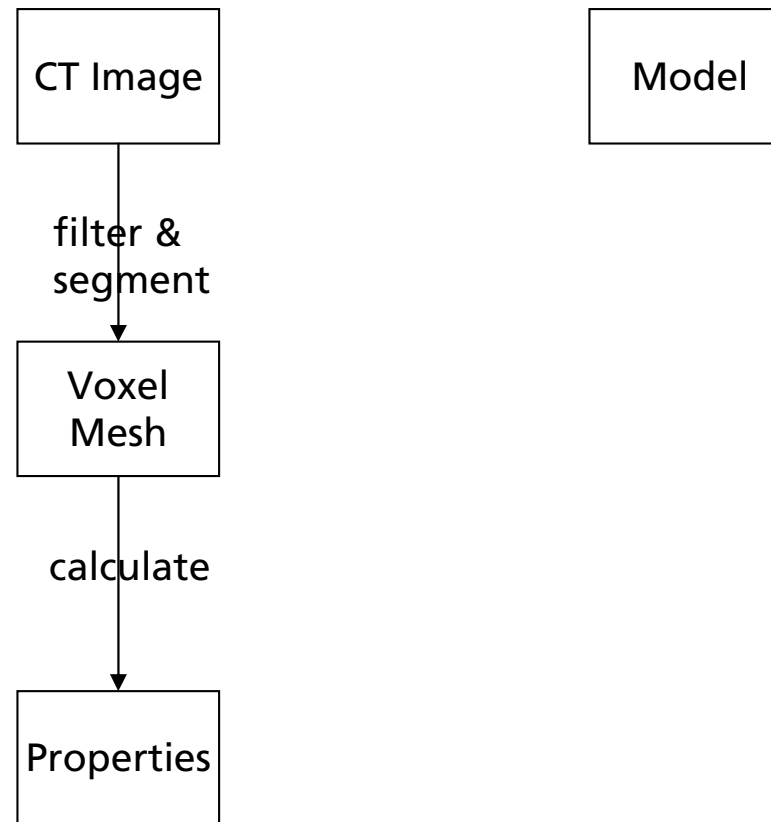
Bridge the Gap - Step 1: Validate Calculations

... and Measurements

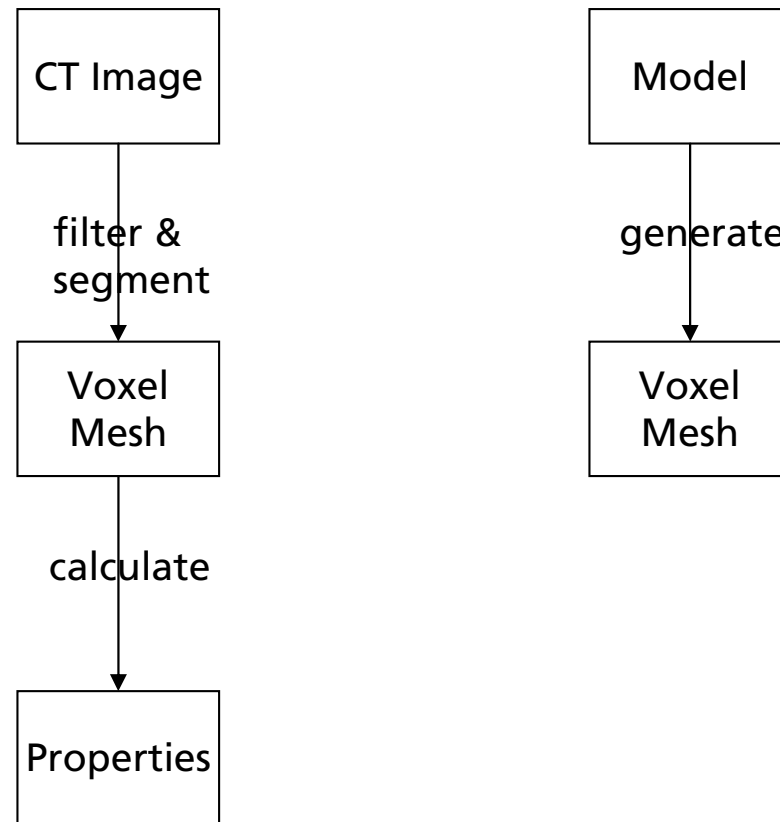
... and Imaging



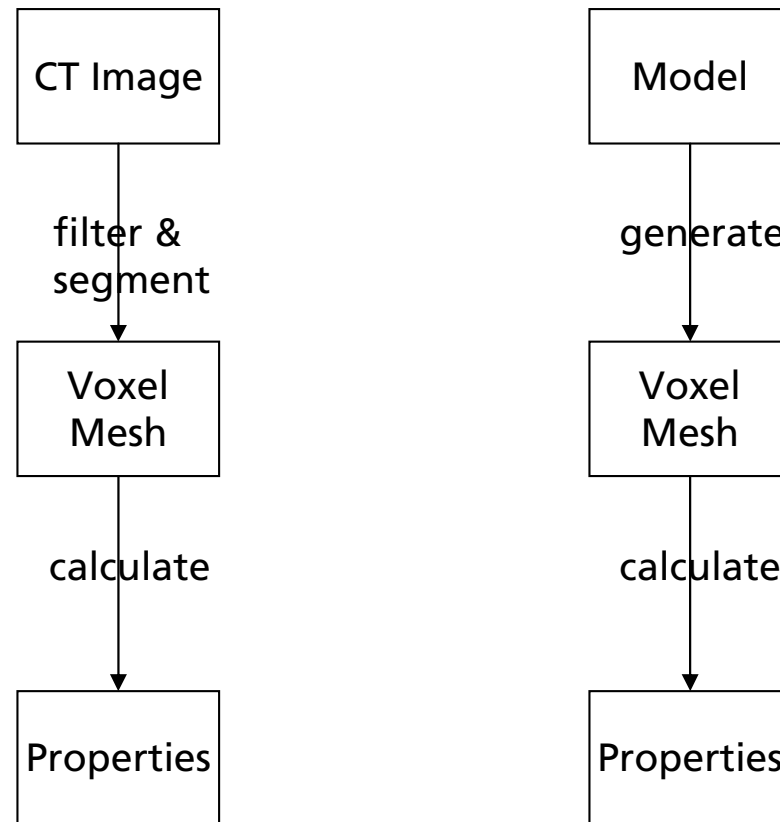
Bridge the Gap - Step 2: Validate Modeling



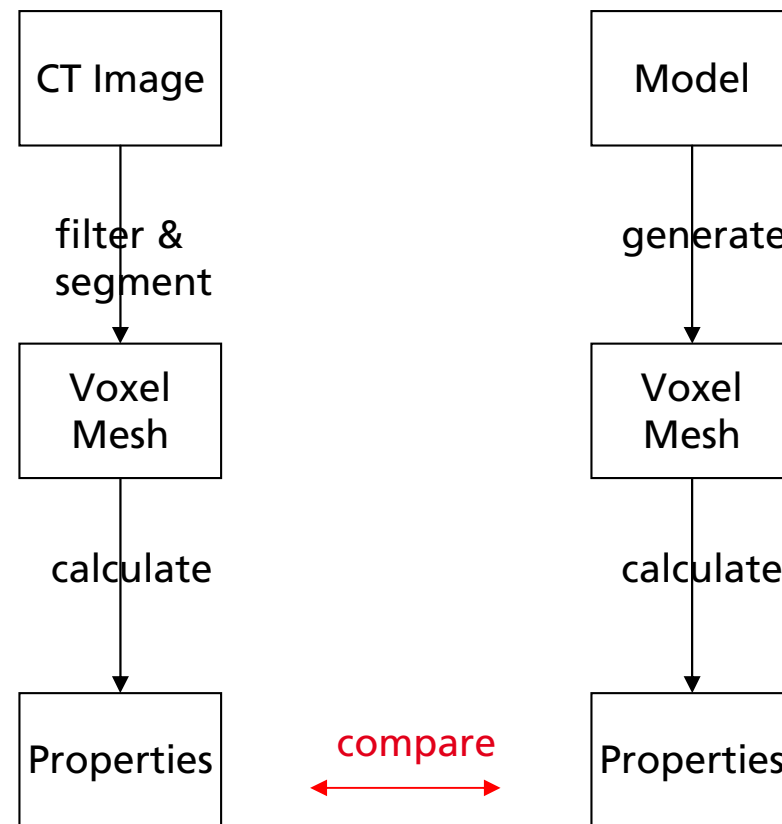
Bridge the Gap - Step 2: Validate Modeling



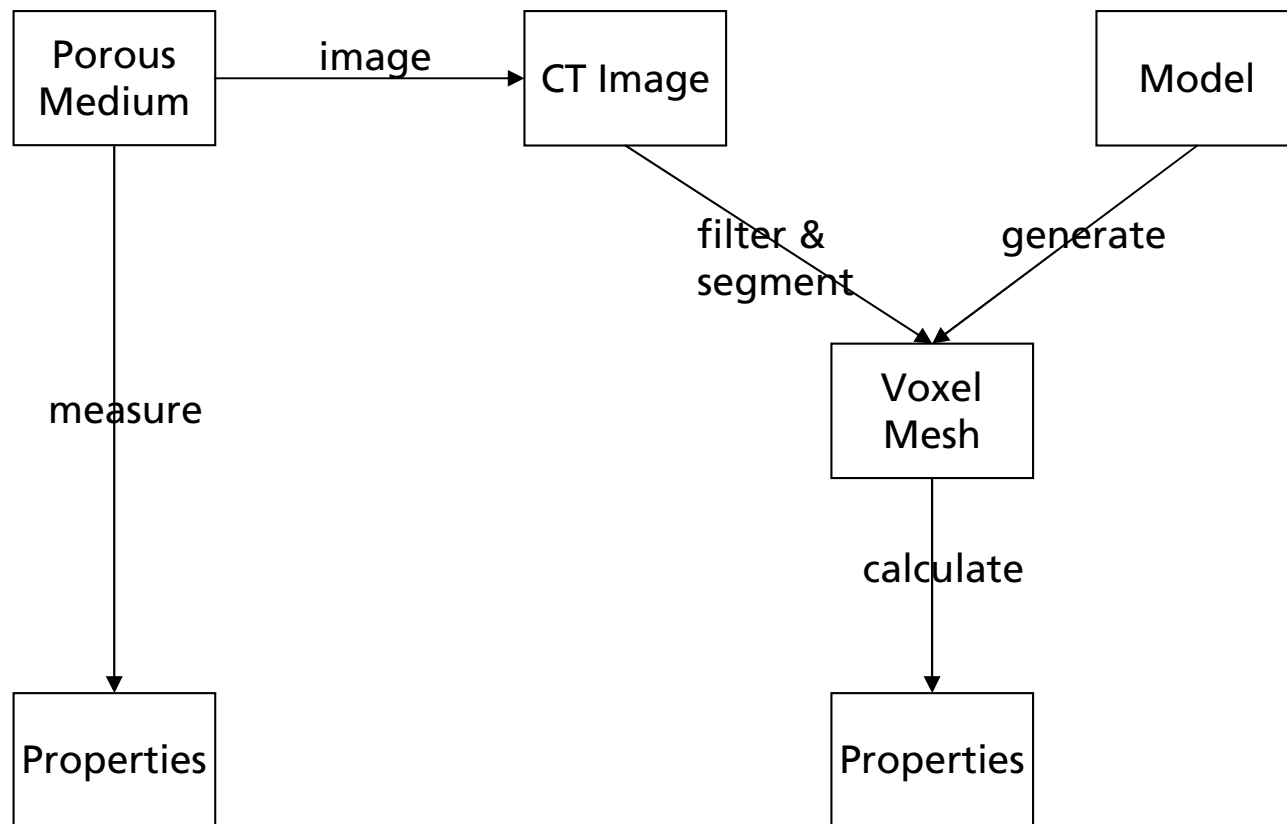
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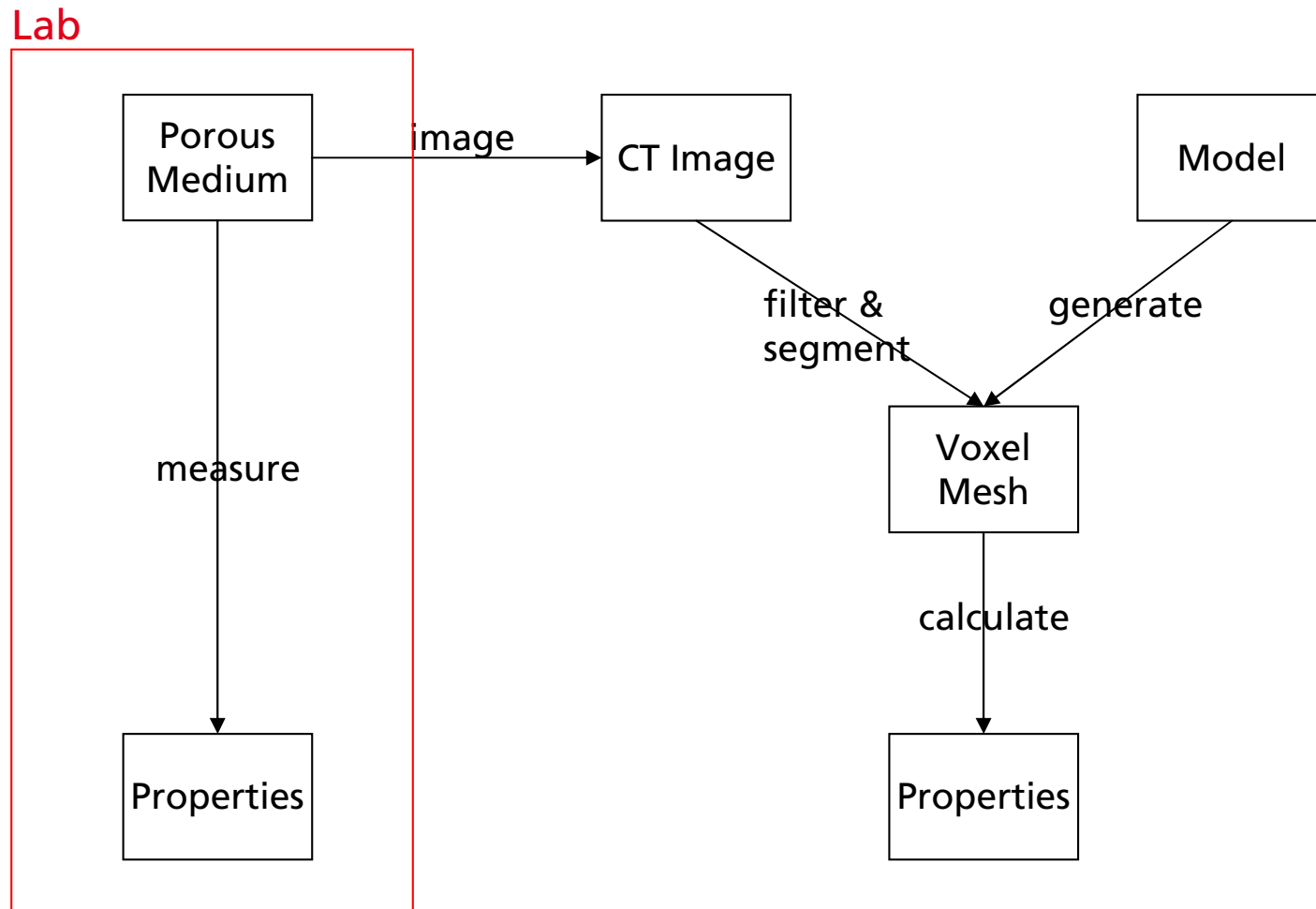
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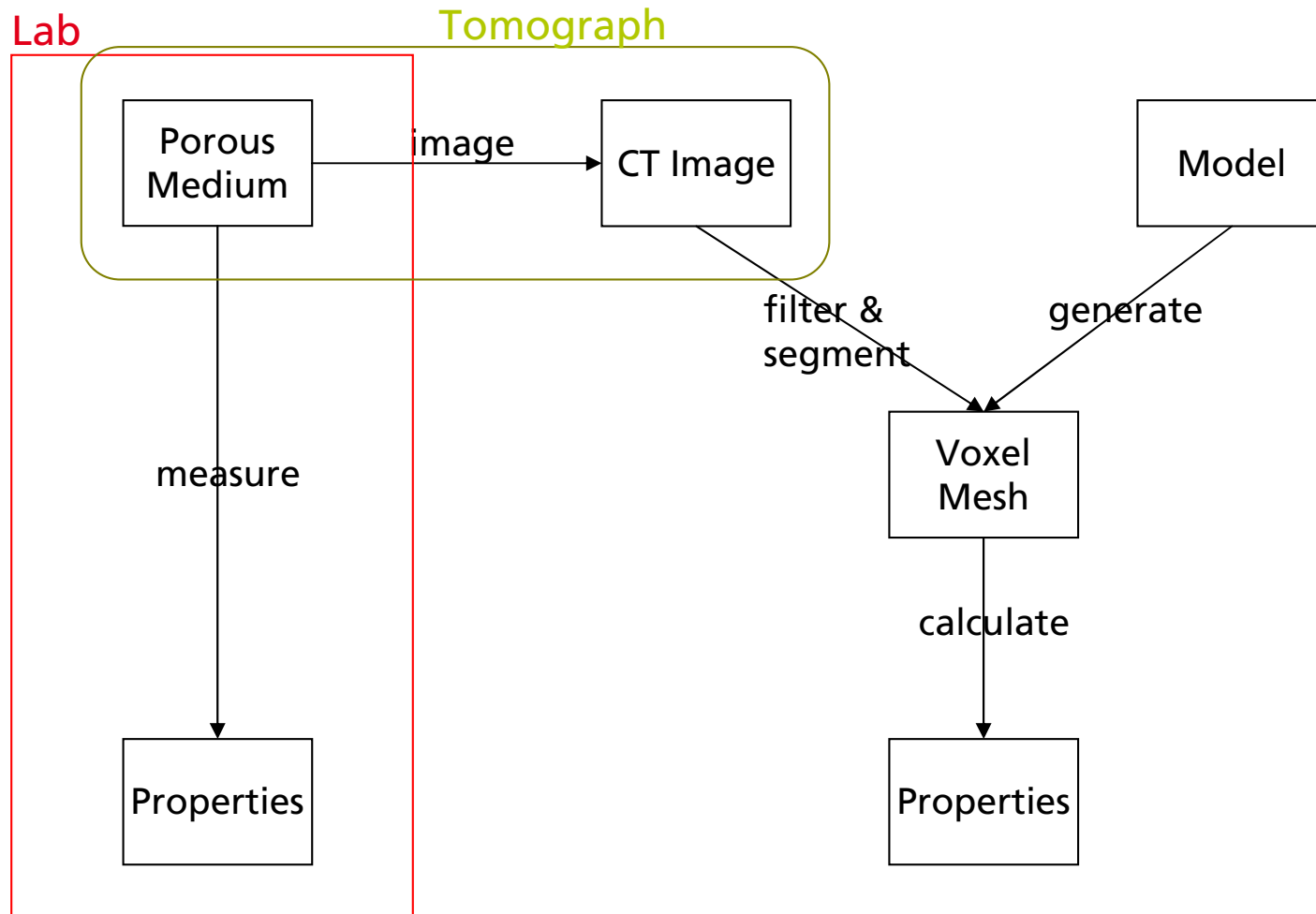
The GeoDict Idea



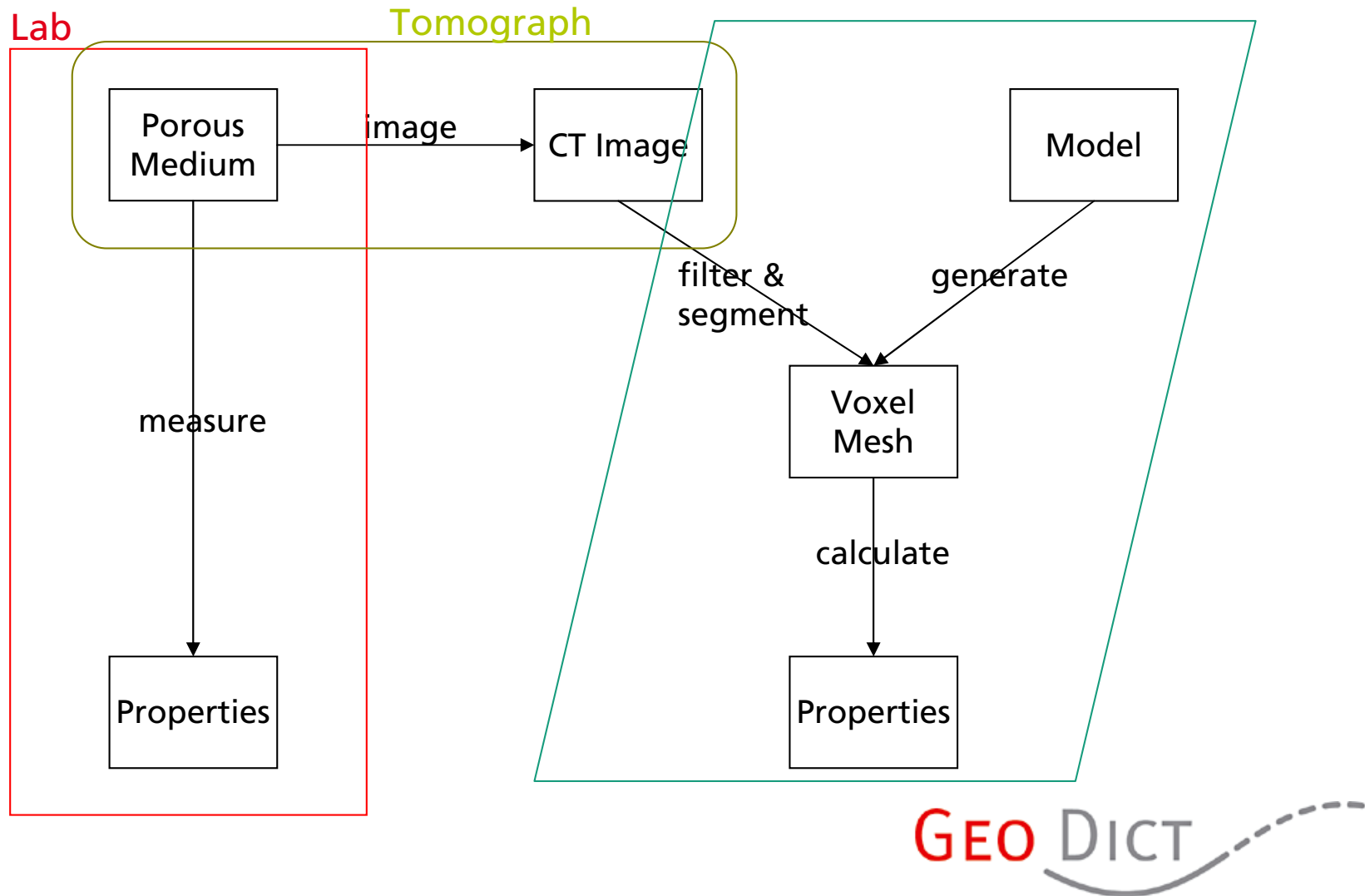
The GeoDict Idea



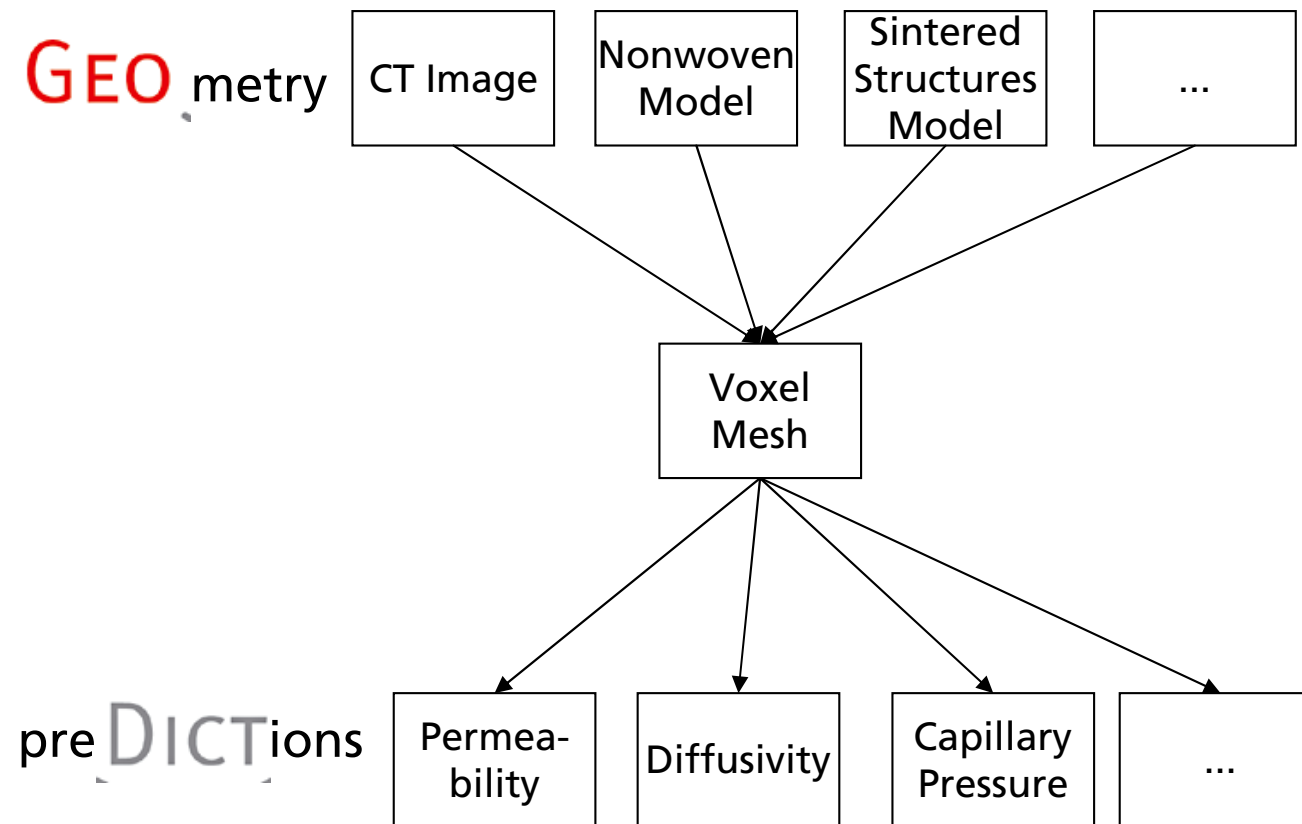
The GeoDict Idea



The GeoDict Idea



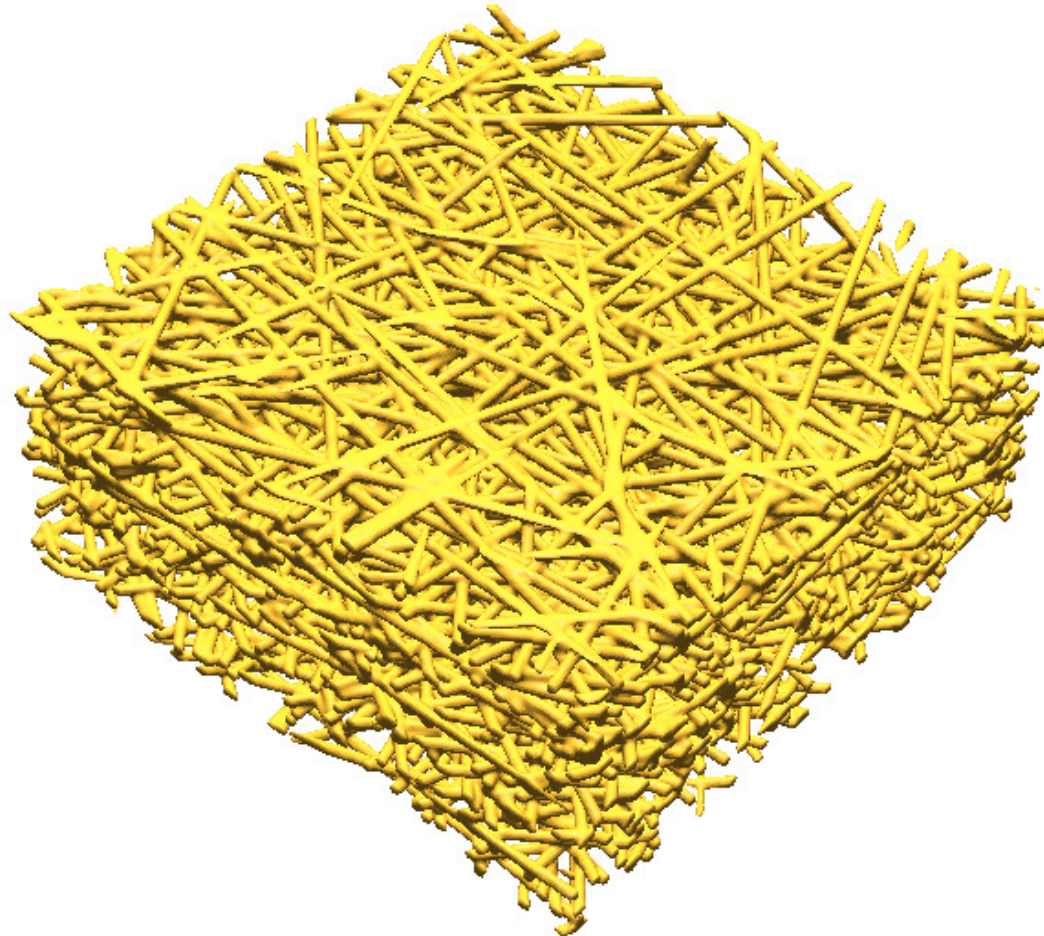
The GeoDict Software



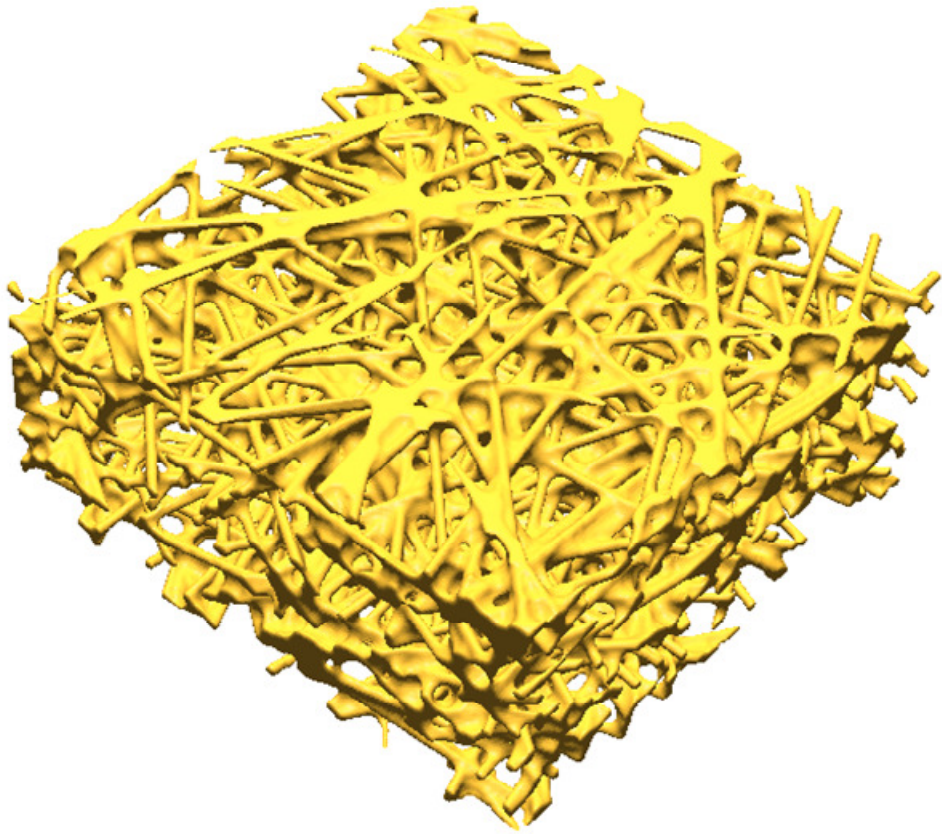
Model: Nonwovens - Straight Fibres

Poisson line process using:

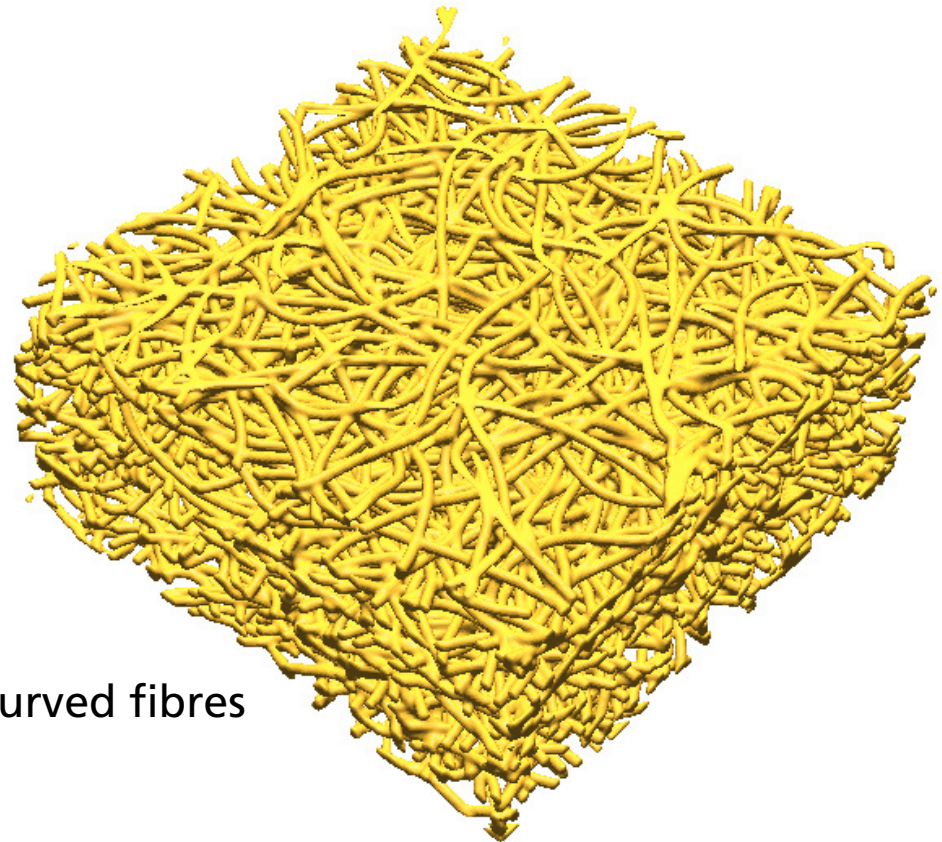
- fibre diameter
- fibre cross sectional shape
- anisotropy
- porosity



Model: Nonwovens - Some Variants

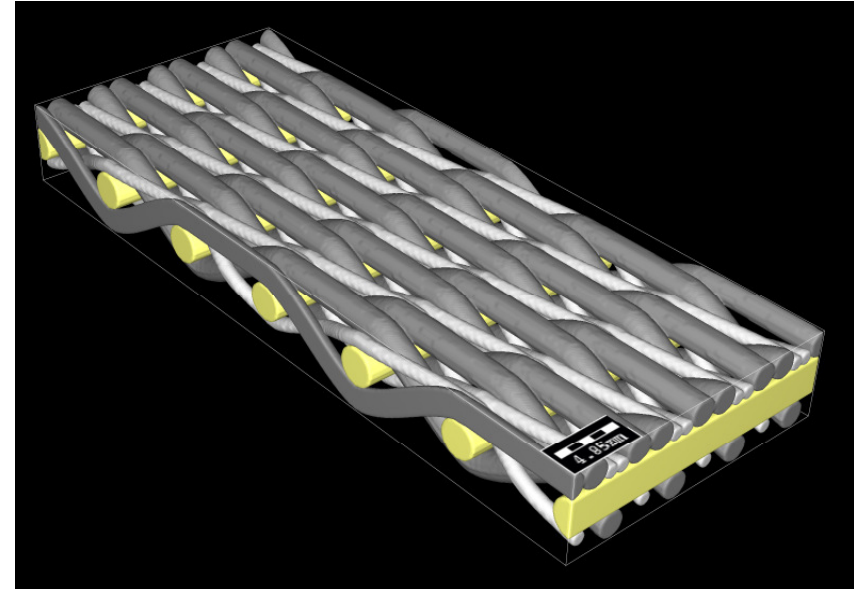
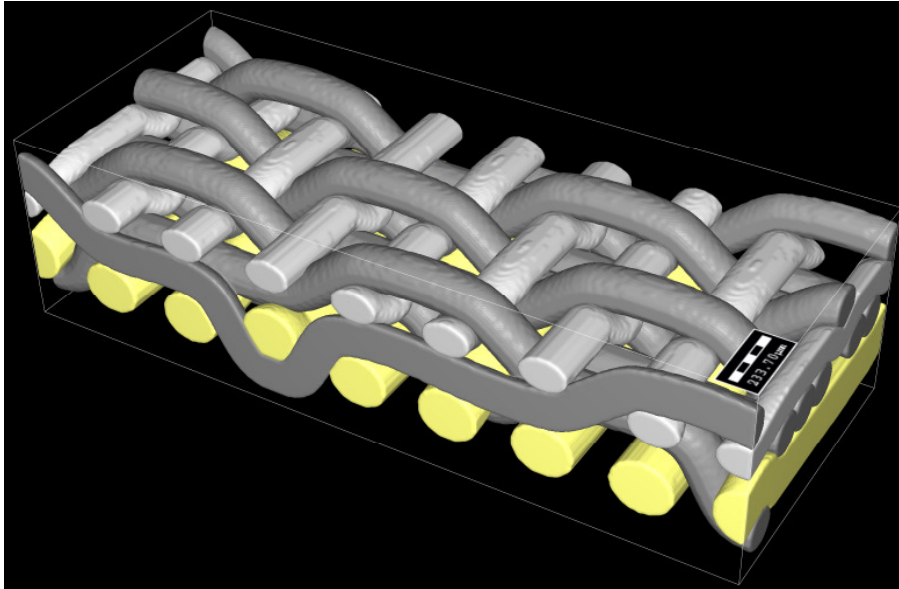


Straight fibres plus binder



Curved fibres

Model: Woven Fabric



Property: Permeability

Macroscopic description (homogenized porous media model)

$$\text{Darcy's law : } u = -\frac{1}{\mu} \kappa \nabla p$$

u : average flow velocity

κ : permeability tensor *unknown*

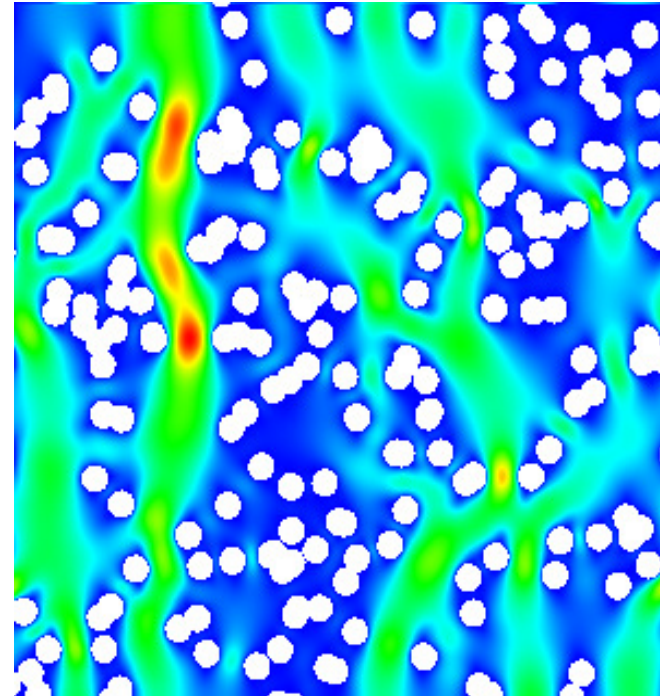
μ : viscosity

p : pressure

Microscopic description (pore structure model)

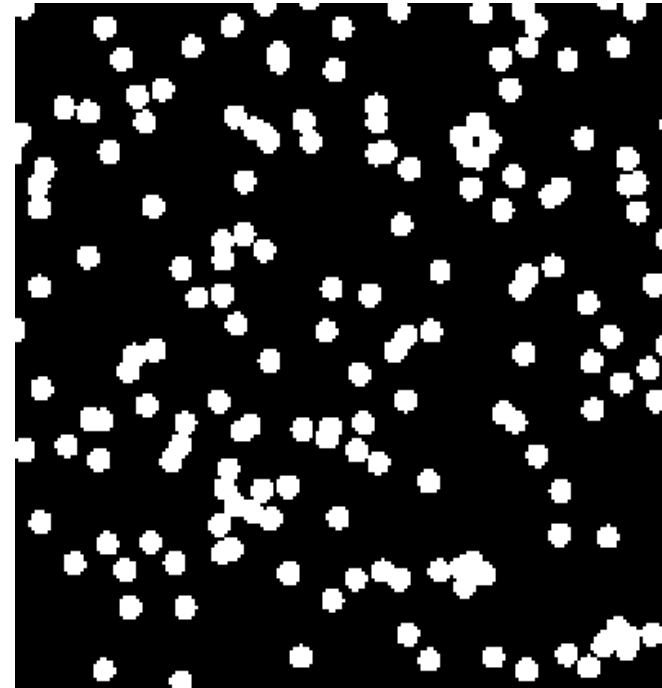
$$\text{Stokes equation: } -\mu \Delta u + \nabla p = 0$$

Boundary conditions: no-slip on fibre surface, pressure drop
 κ can be determined from the solution!



Property: Relative Permeability

Two-step approach:

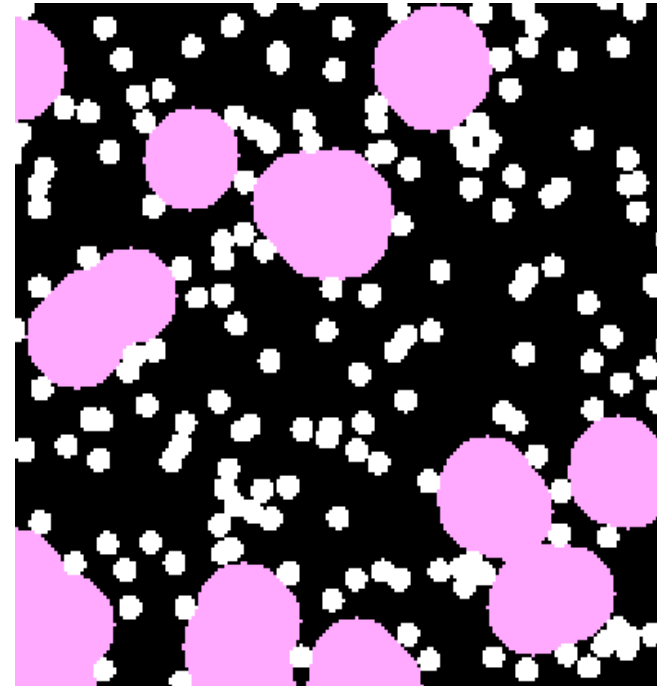
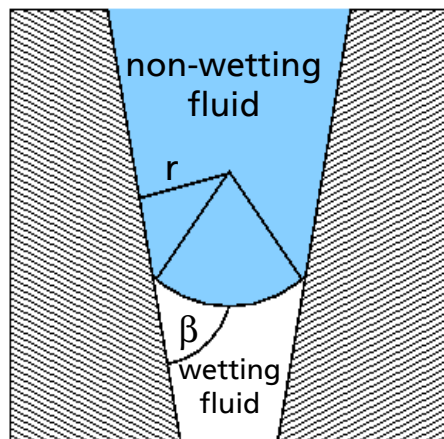


Property: Relative Permeability

Two-step approach:

1. Use pore morphology method (Hilpert, 2001) to determine distribution of air and water phase.
- Idea: a pore is filled with the non-wetting fluid (=water), if

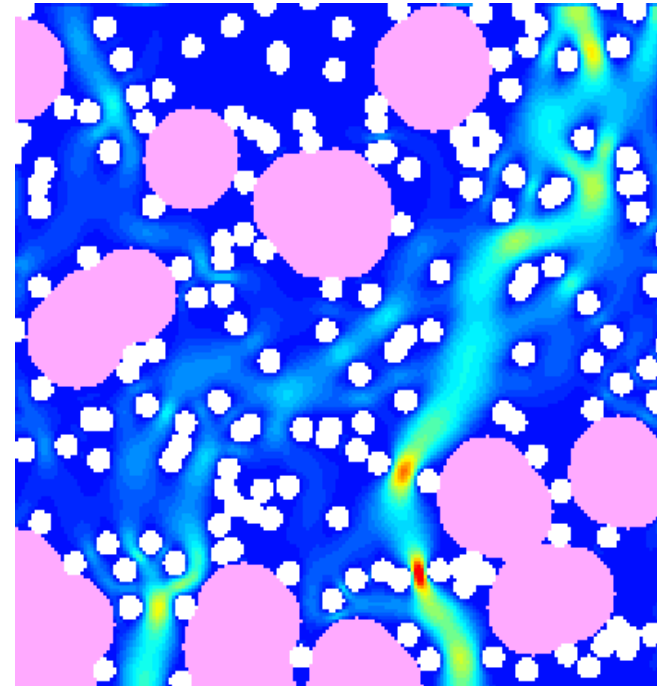
$$p_c \geq \frac{2\sigma}{r} \cos \beta$$



Property: Relative Permeability

Two-step approach:

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 - Idea: a pore is filled with the non-wetting fluid (=water), if
$$p_c \geq \frac{2\sigma}{r} \cos \beta$$
2. Solve Stokes equation on the remaining pore space to determine wetting phase (=air) permeability



Property: Diffusivity

Macroscopic description (homogenized porous media model)

Fick's first law: $j = -D^* \nabla c$

D^* : effective diffusivity [m^2/s] *unknown*

j : diffusion flux [$\text{mol}/\text{m}^2/\text{s}$]

c : concentration [mol/m^3]

Property: Diffusivity

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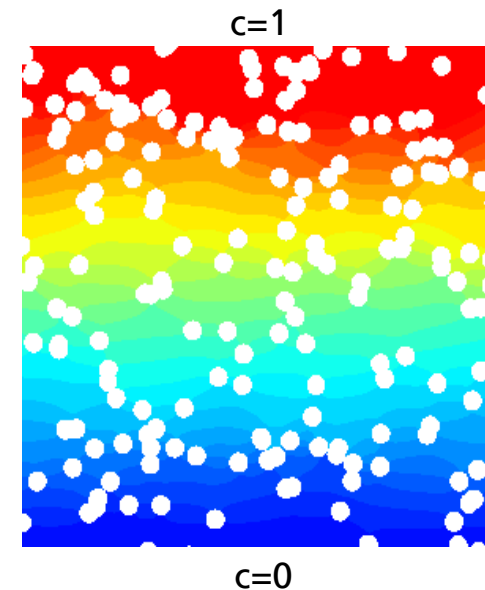
c : concentration [mol/m^3]

Microscopic description (pore structure model)

Laplace equation: $-\Delta c = 0$

Boundary conditions: no-flux on fibre surface,
concentration drop

D^* can be determined from the solution!



Summary Part I

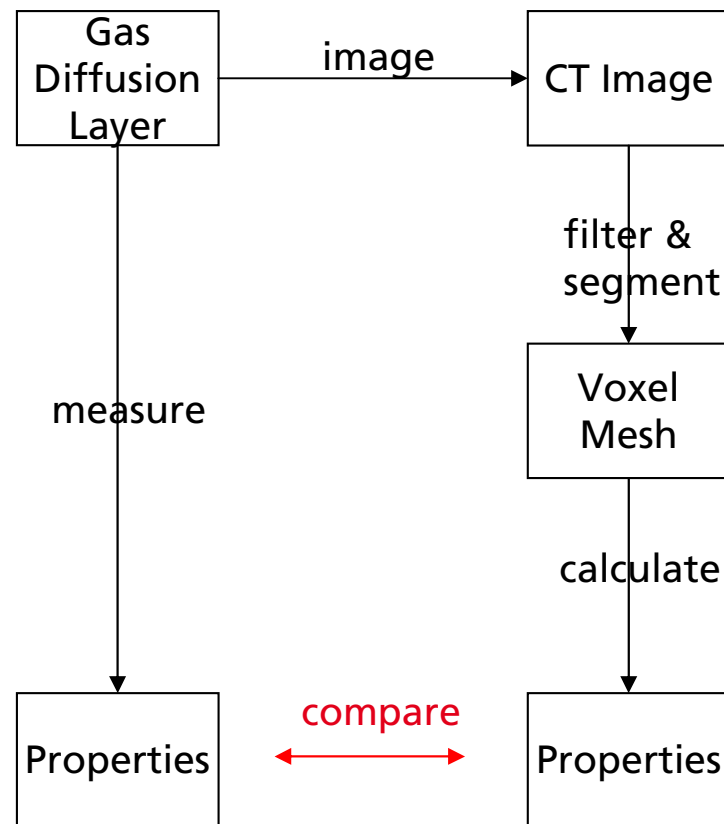
Models:

- CT Images
- Fibrous nonwovens
- Woven structures
- Sintered structures
- Sphere packings
- Layered structures

Properties:

- Pore size distribution
- Surface area
- (Knudsen) Diffusivity
- Permeability
- Electric conductivity
- Heat conductivity
- Capillary pressure curve
- Bubble point
- Relative (= saturation dependent) permeability
- Relative (= saturation dependent) diffusivity
- Filter efficiency and life time

Application: Gas Diffusion Layer of PEM Fuel Cell



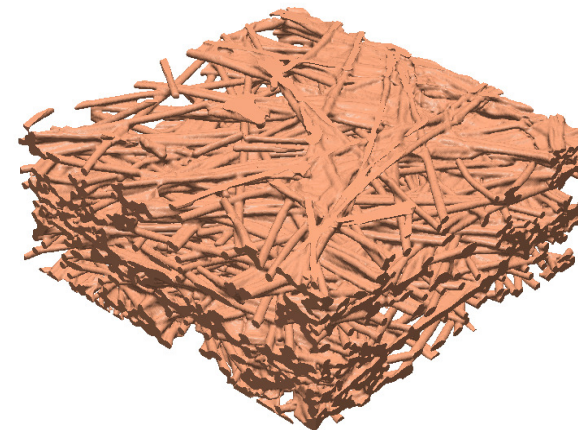
Joint work

PSI:

- CT Images of Toray paper at different compression levels
- Diffusivity and permeability measurements at different compression levels

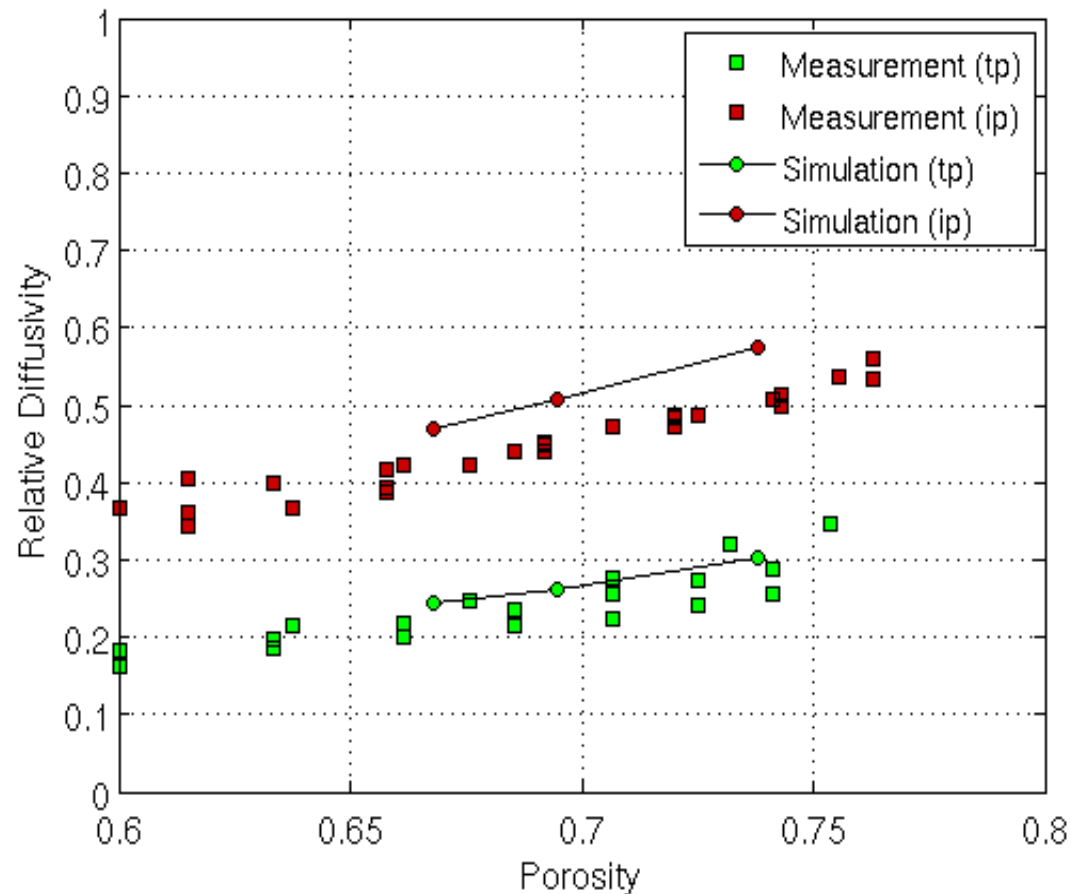
ITWM:

- Compute diffusivity and permeability



Becker, Flückiger, Reum, Büchi, Marone, Stampanoni, 2009, J. Electrochem. Soc. 156

Diffusivity

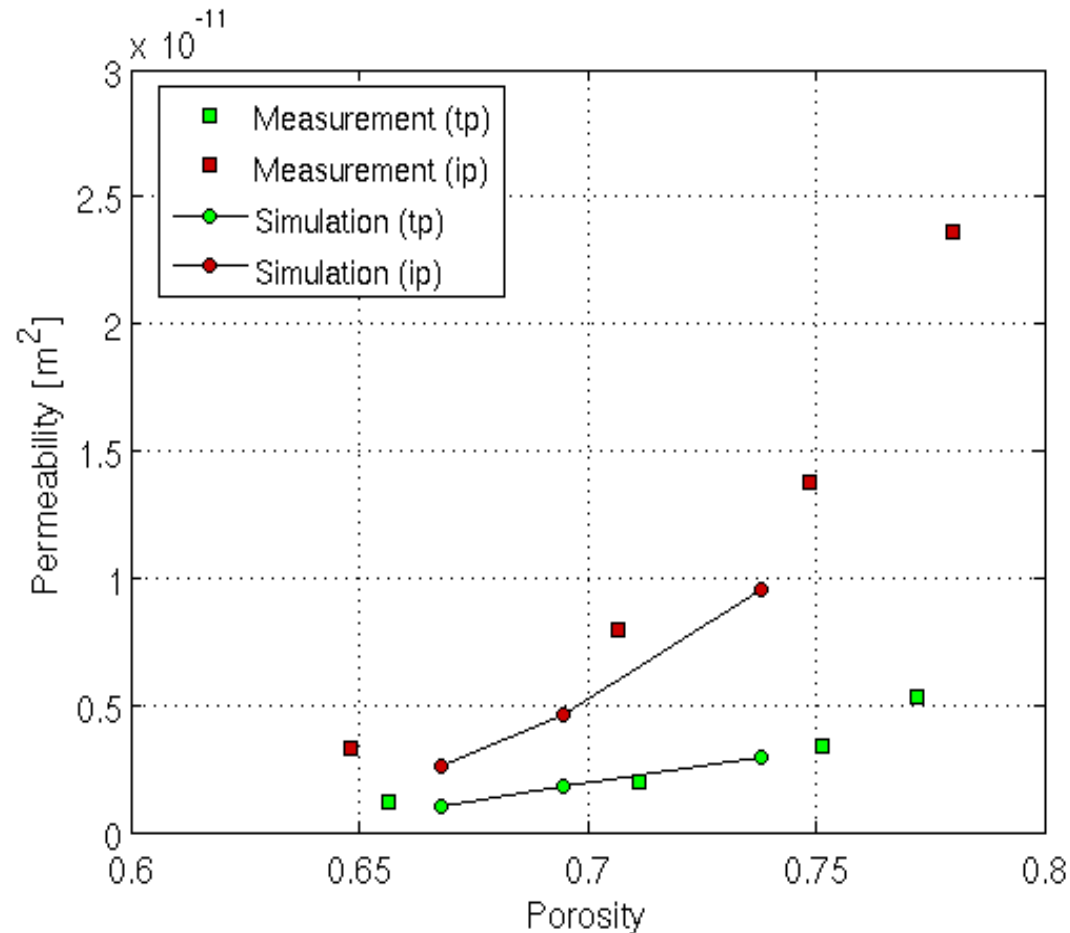


Perfect in tp-direction

Small differences in ip-direction

- ip-measurements performed on a stack of GDLs
- tomography image shows single layer between sample holder

Permeability

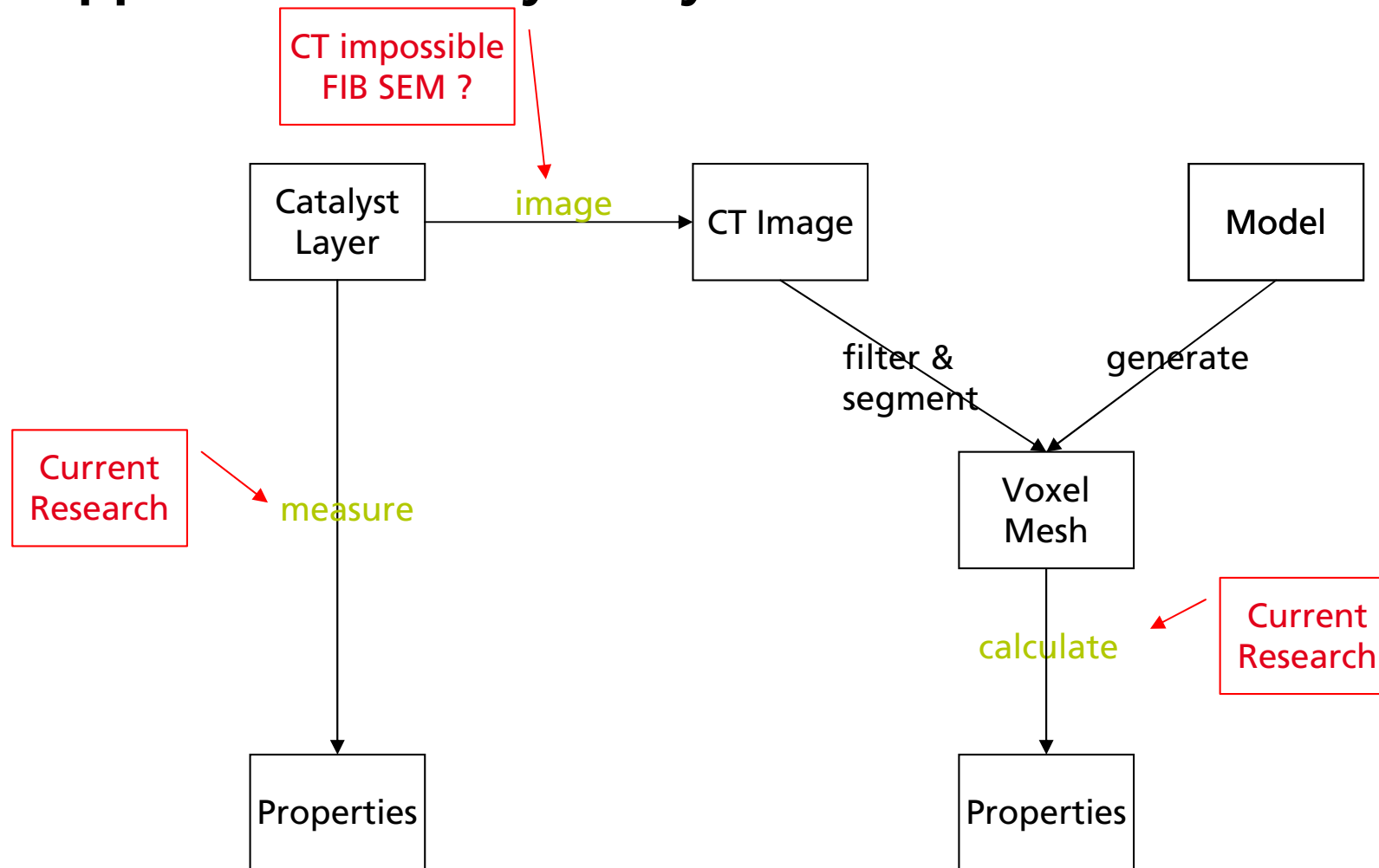


Perfect in tp-direction

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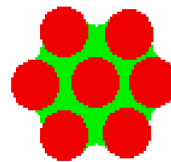
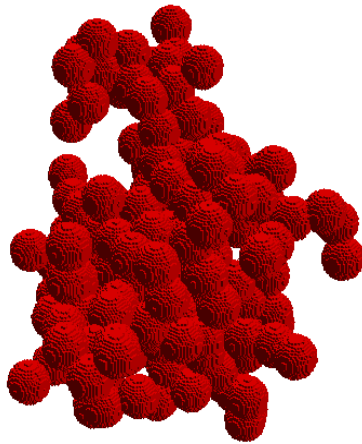
Application: Catalyst Layer of PEM Fuel Cell



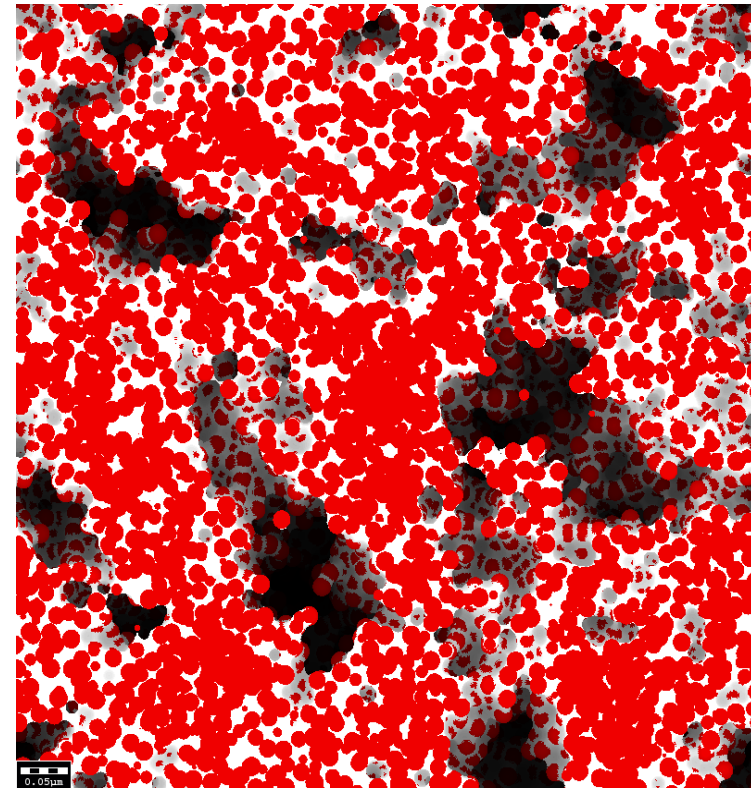
Problem: pore sizes < 100 nm

Catalyst Layer Model

Carbon agglomerates plus electrolyte



Elect. between
Carbon Partikels



Conductivity

Compare models with varying carbon and electrolyte volume fractions

| Vol% Carbon | Vol% Electrolyte | Porosity | Electronic Conductivity | Protonic Conductivity |
|-------------|------------------|----------|-------------------------|-----------------------|
| 35.4 | 12.2 | 52.4 | 6.6 % | 1.1 % |
| 40.9 | 5.2 | 53.9 | 9.7 % | none |
| 40.9 | 13.8 | 45.3 | 9.7 % | 1.6 % |
| 40.9 | 20.7 | 38.3 | 9.7 % | 4.9 % |
| 40.9 | 26.3 | 32.8 | 9.7 % | 8.2 % |
| 45.1 | 15.2 | 39.8 | 13.4 % | 1.9 % |
| 50.1 | 16.6 | 33.3 | 17.6 % | 2.2 % |

Summary Part II

Gas diffusion layer:

- validated method to determine diffusivity and permeability

Catalyst layer:

- no validation possible until 3D images are available

Thank You !



Geometry generator,
property predictor and
virtual material designer

www.geodict.com

BMBF project PemCaD

