
Simulation of Particle Filtration Using

GEO DICT

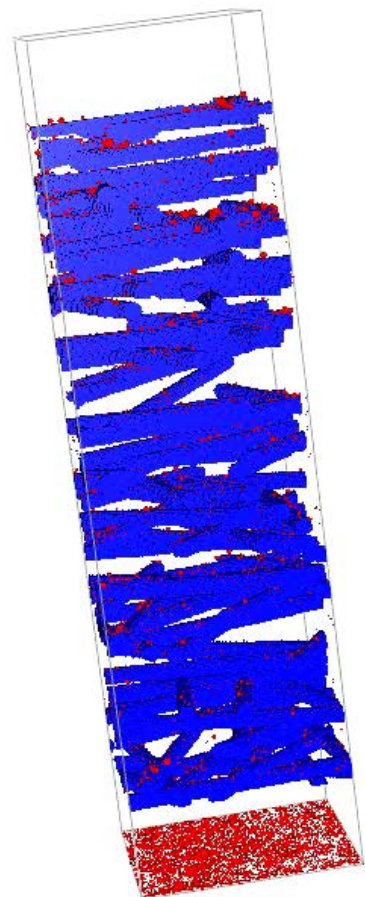


Fraunhofer

ITWM

MATH
2 MARKET

Simulation of Particle Filtration Using **GEO** **DICT**



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Dr. Stefan Rief

Dr. Jürgen Becker

Dr. Liping Cheng

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Math2Market GmbH,
Kaiserslautern

11th Symposium *Textile Filters*

Sächsisches Textilforschungsinstitut e.V.

March 6th & 7th 2012, Chemnitz

What about Math2Market & Fraunhofer ITWM / SMS?

Math2Market GmbH is a spin-off that markets and further develops the GeoDict software

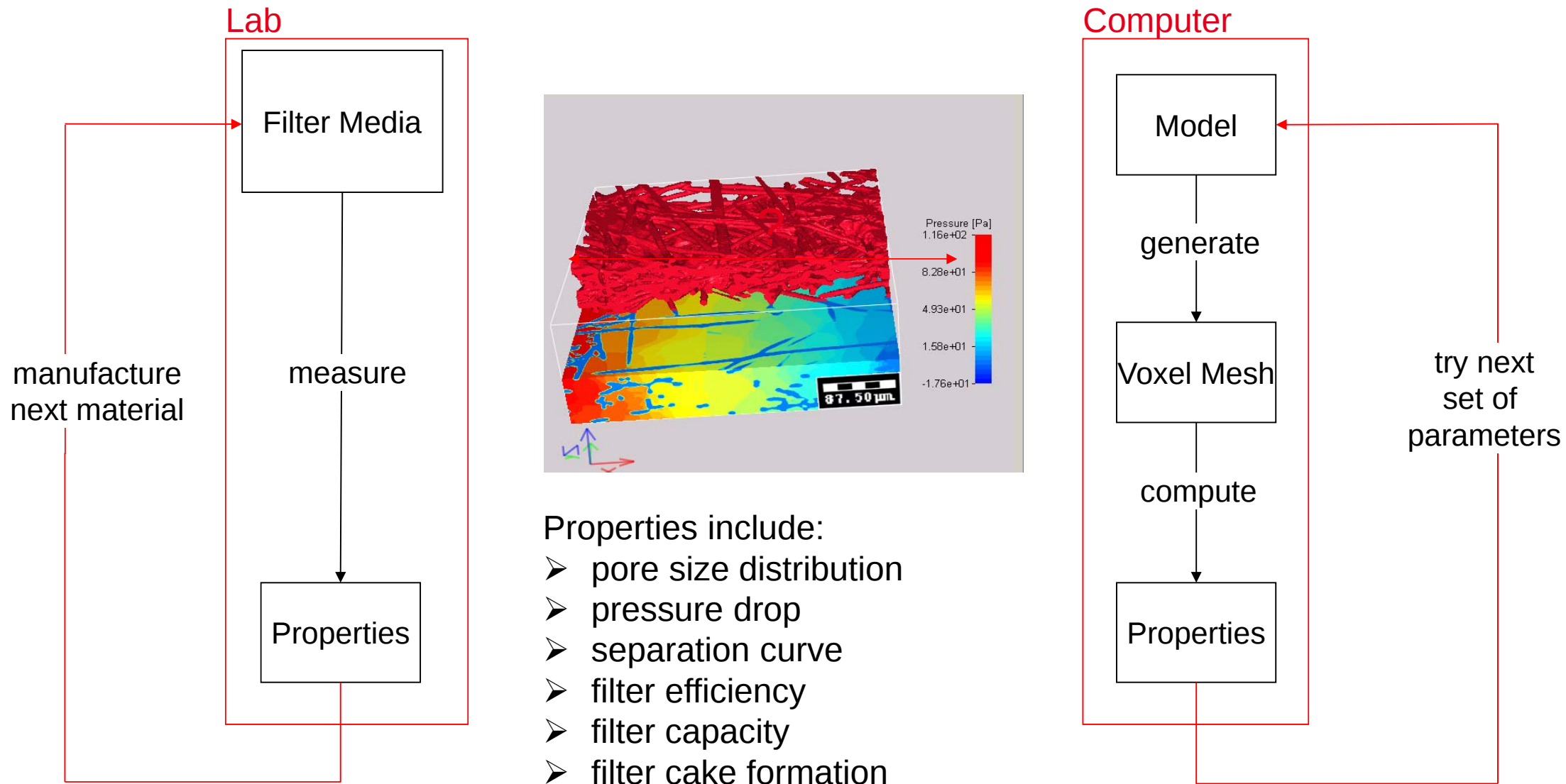
M2M incorporated 9/2011, the 4 core team members phase from SMS to M2M in 2012.

Andreas Wiegmann, PhD, until June 30th, 2012 is

- Chief Executive Officer at Math2Market GmbH (50% -> 100%)
- Deputy head of department SMS at Fraunhofer ITWM (50% -> 0%)

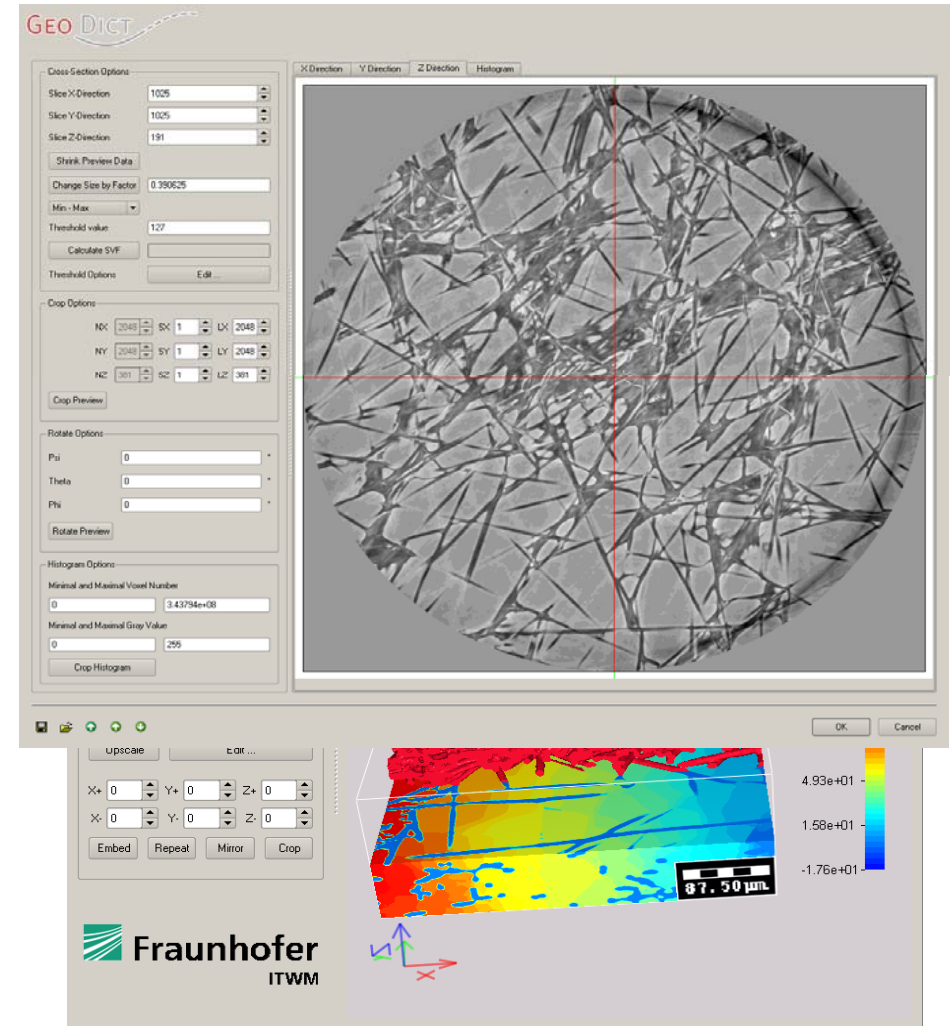
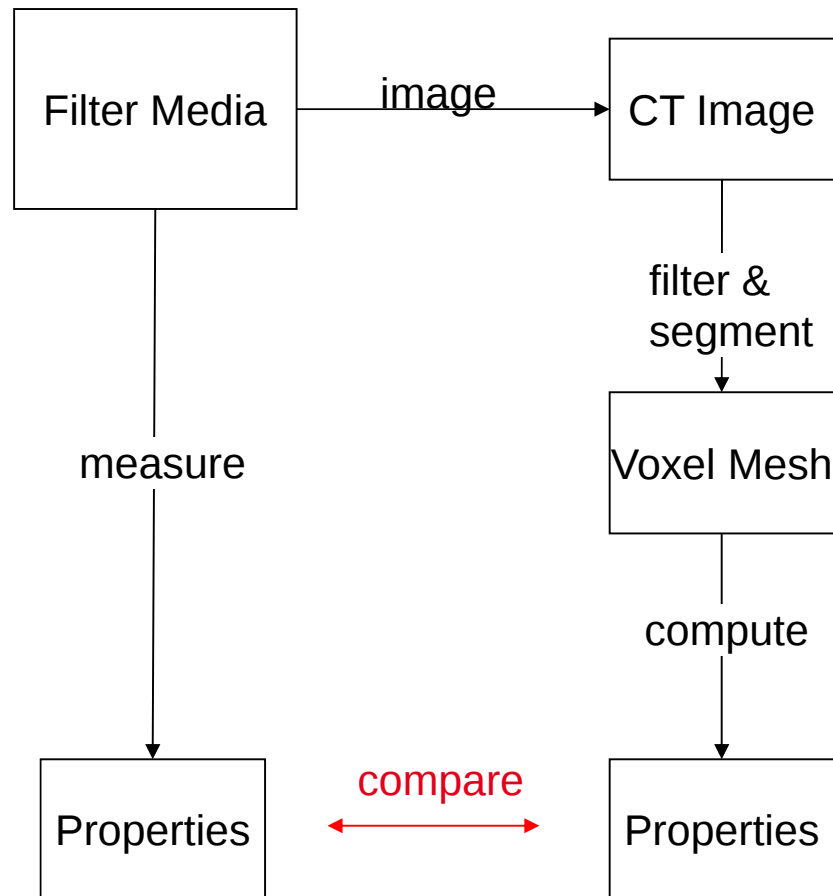
M2M provides

- licenses,
- software support,
- consulting regarding modelling,
- simulation-based engineering services ,
- commercial-strength software engineering &
- close ties to Fraunhofer ITWM when mathematical research is required



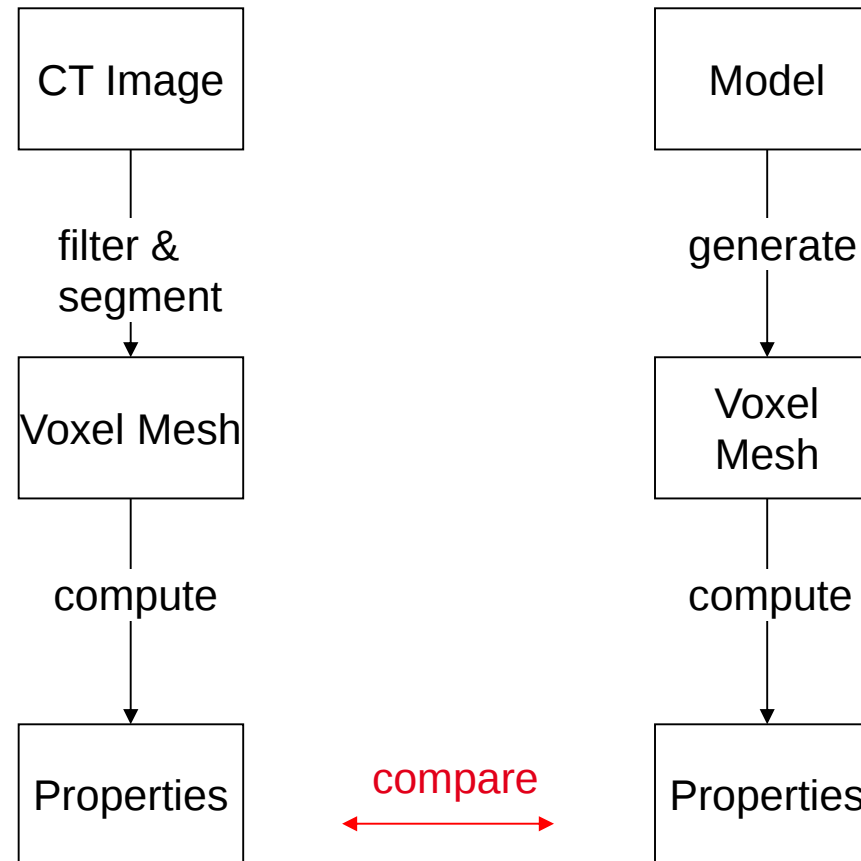
Validation - Step 1:

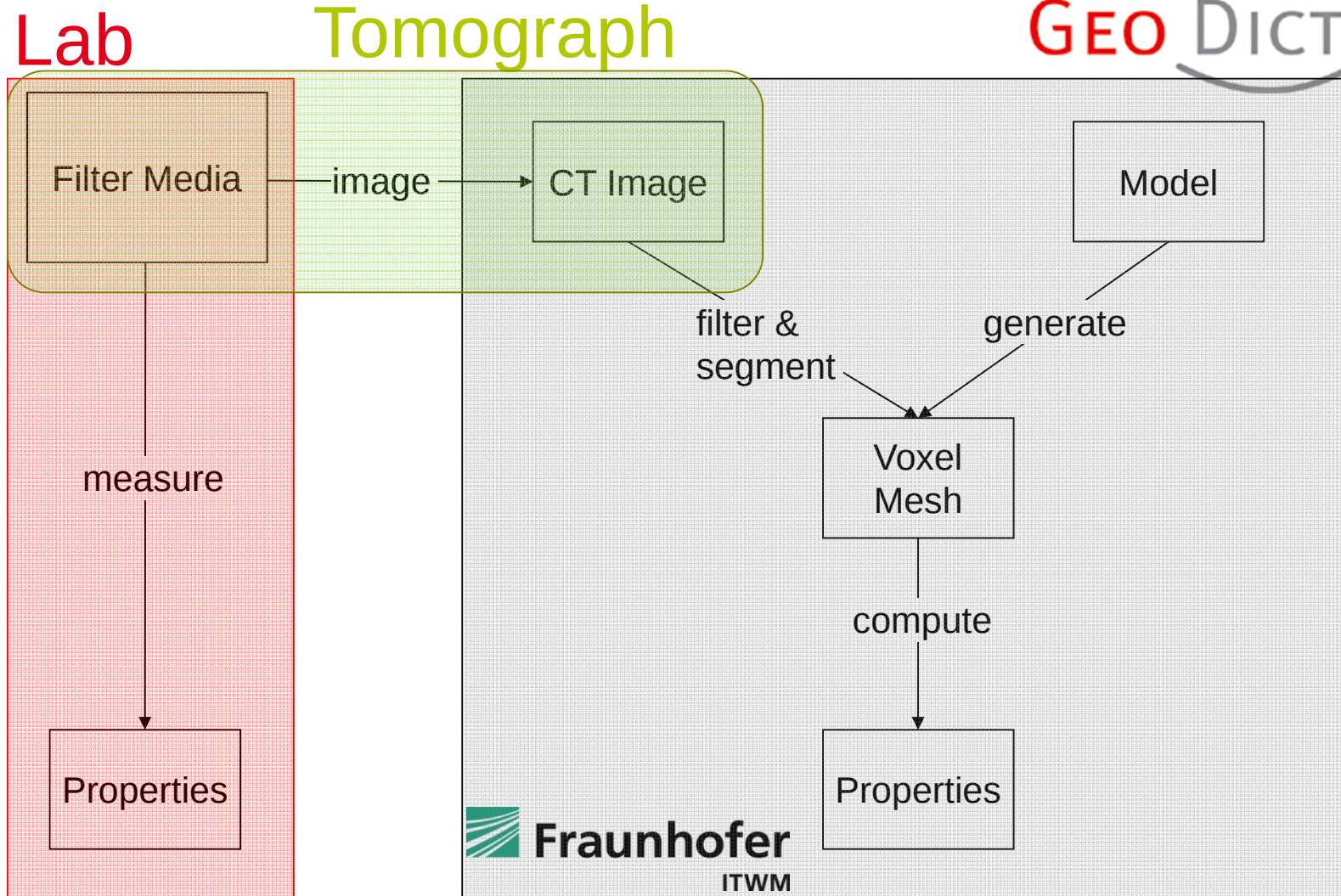
Property Computations



Validation - Step 2:

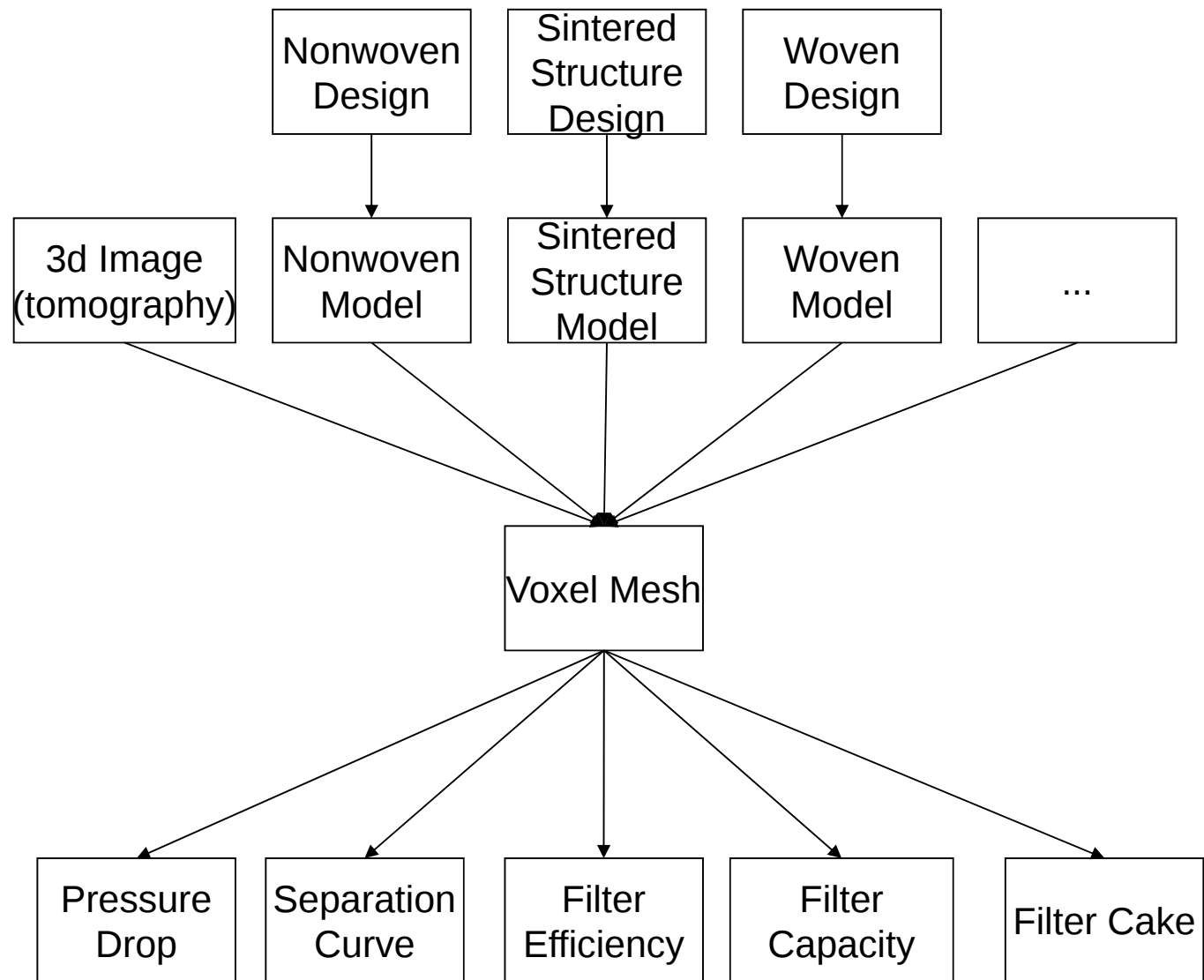
Material Models



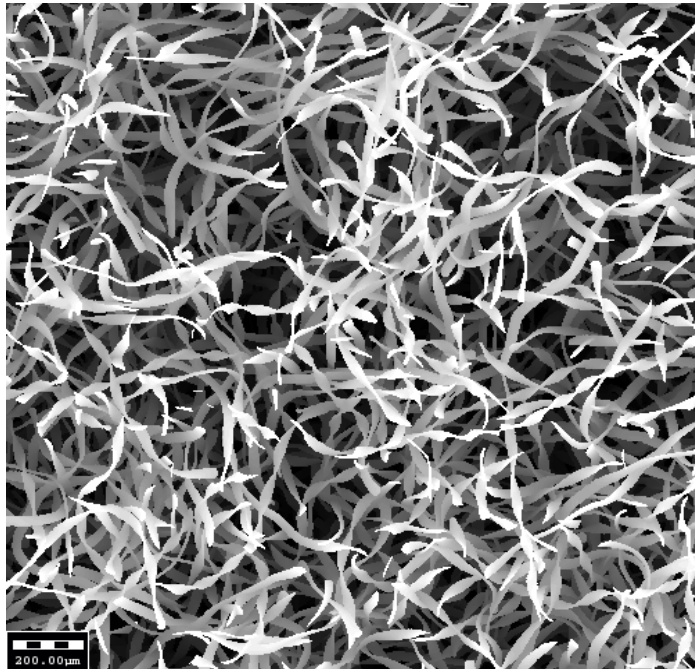


GEOmetry

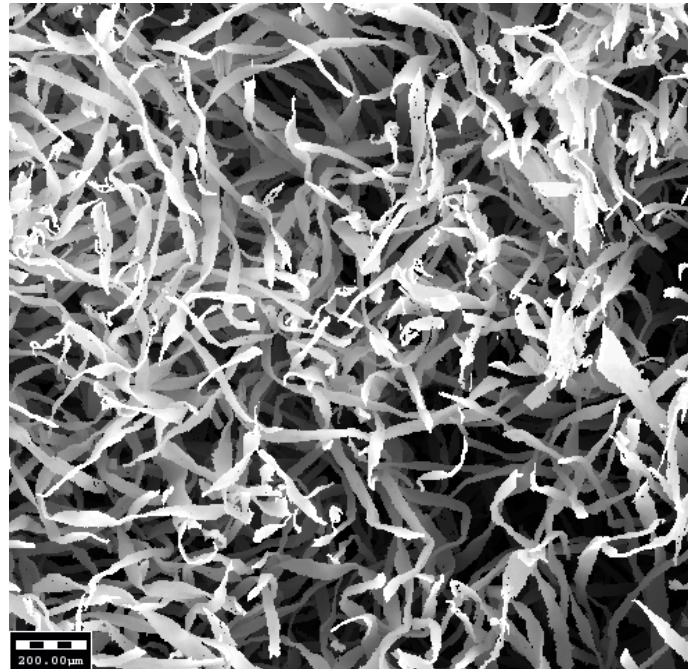
preDICTions



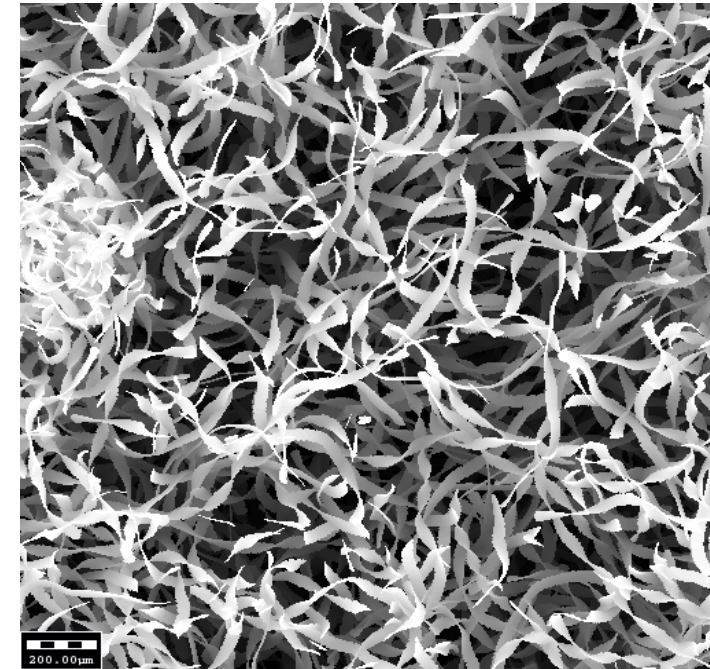
Modell of a nonwoven



homogeneous



tomogram



inhomogeneous

GeoDict's four representation languages of (textile) filter media

- **Design:**
Fiber orientation, porosity / base weight, fiber diameter / dtex,
fiber cross-section, fiber curvature etc.
- **Objects:**
ns (number of segments),
Point(1), Point(2), ..., Point(ns), diameter
- **Image:**
nx, ny, nz, (numbers of voxels in the three directions),
dx, dy, dz, (lengths of voxels in the three directions),
c(1,1,1), c(1,1,2), c(1,1,3), ... c(nx, ny, nz)
- **Surface:**
nt (number of triangles),
P(1,1),P(1,2),P(1,3),P(2,1),P(2,2),P(2,3),P(3,1),P(3,2),P(3,3),...,P(nt,1),P(nt,2),P(nt,3)

Virtual paper: cellulose fibers & fines



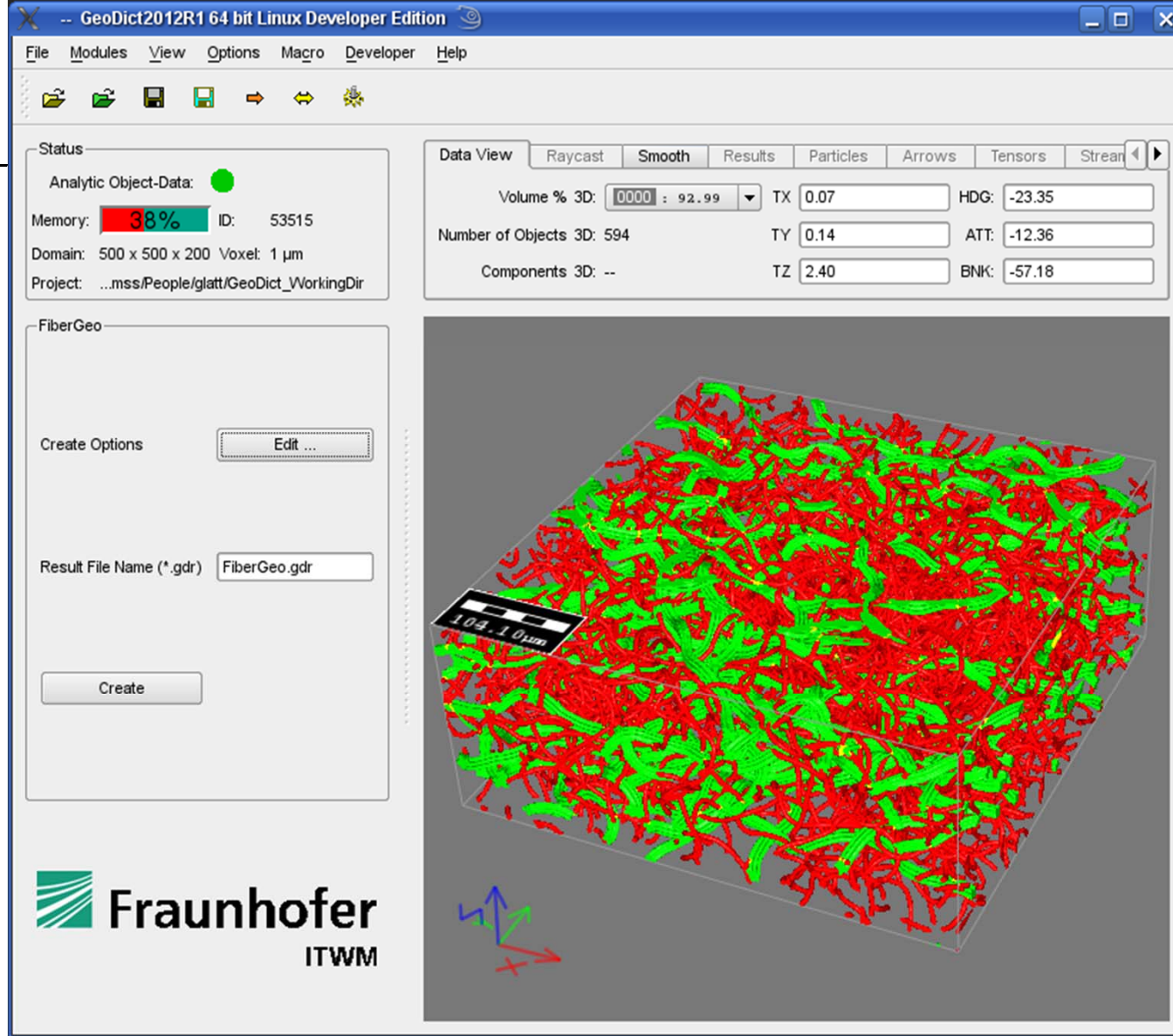
paper.gmc



paper.gad



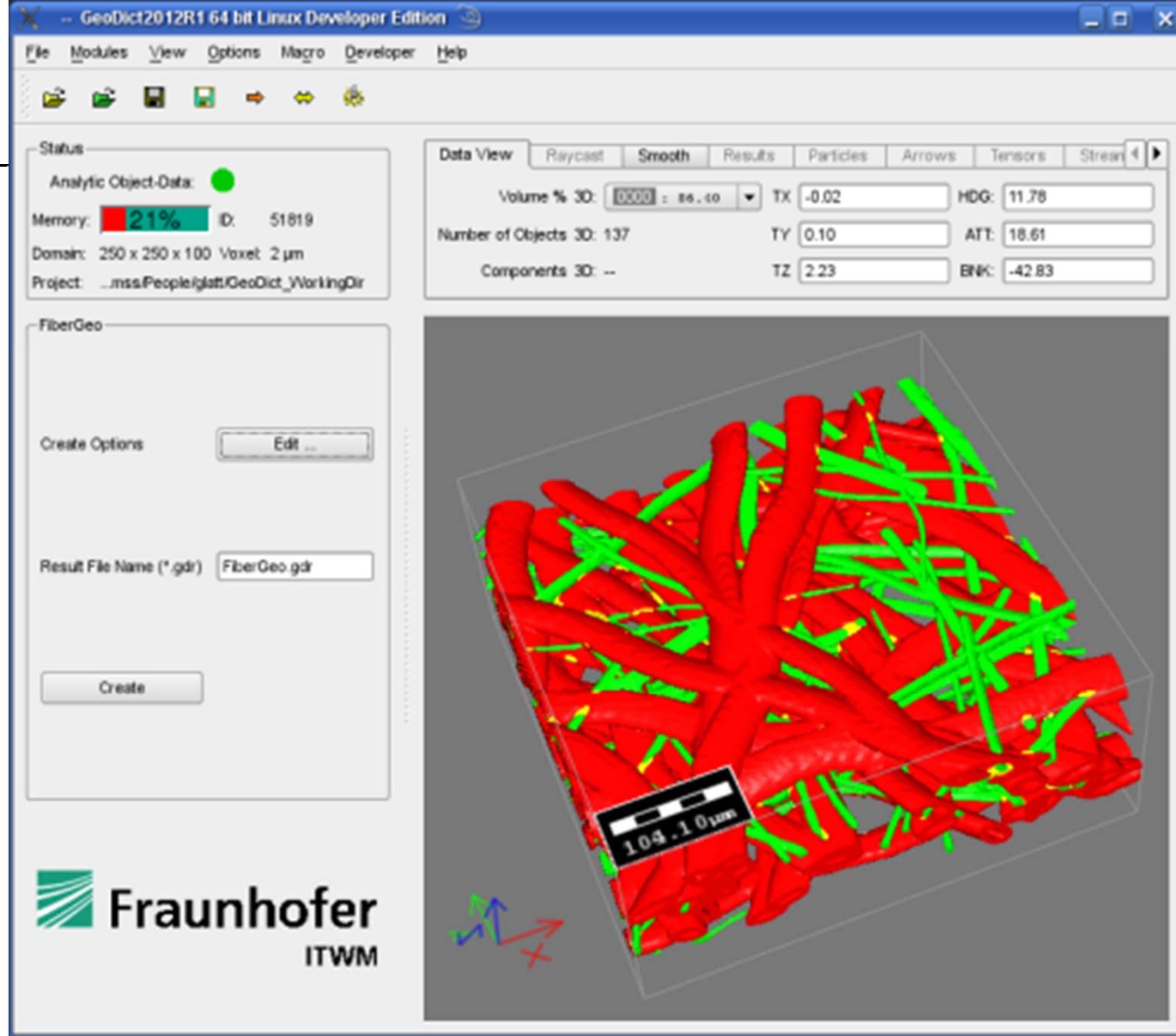
paper.leS



Virtual meltblown: curved fibers



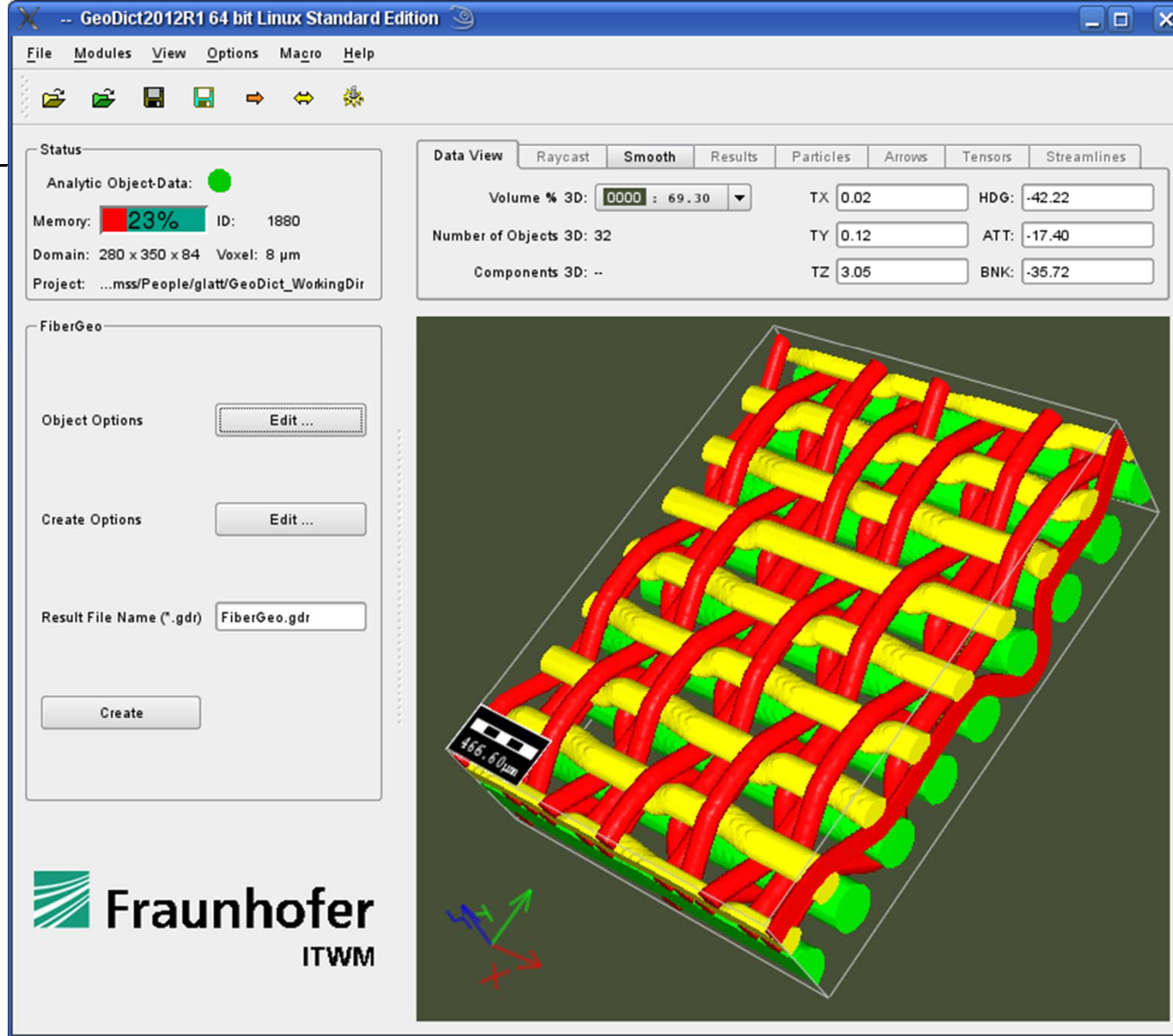
meltblown.gmc



Virtual woven: multiple weft layers



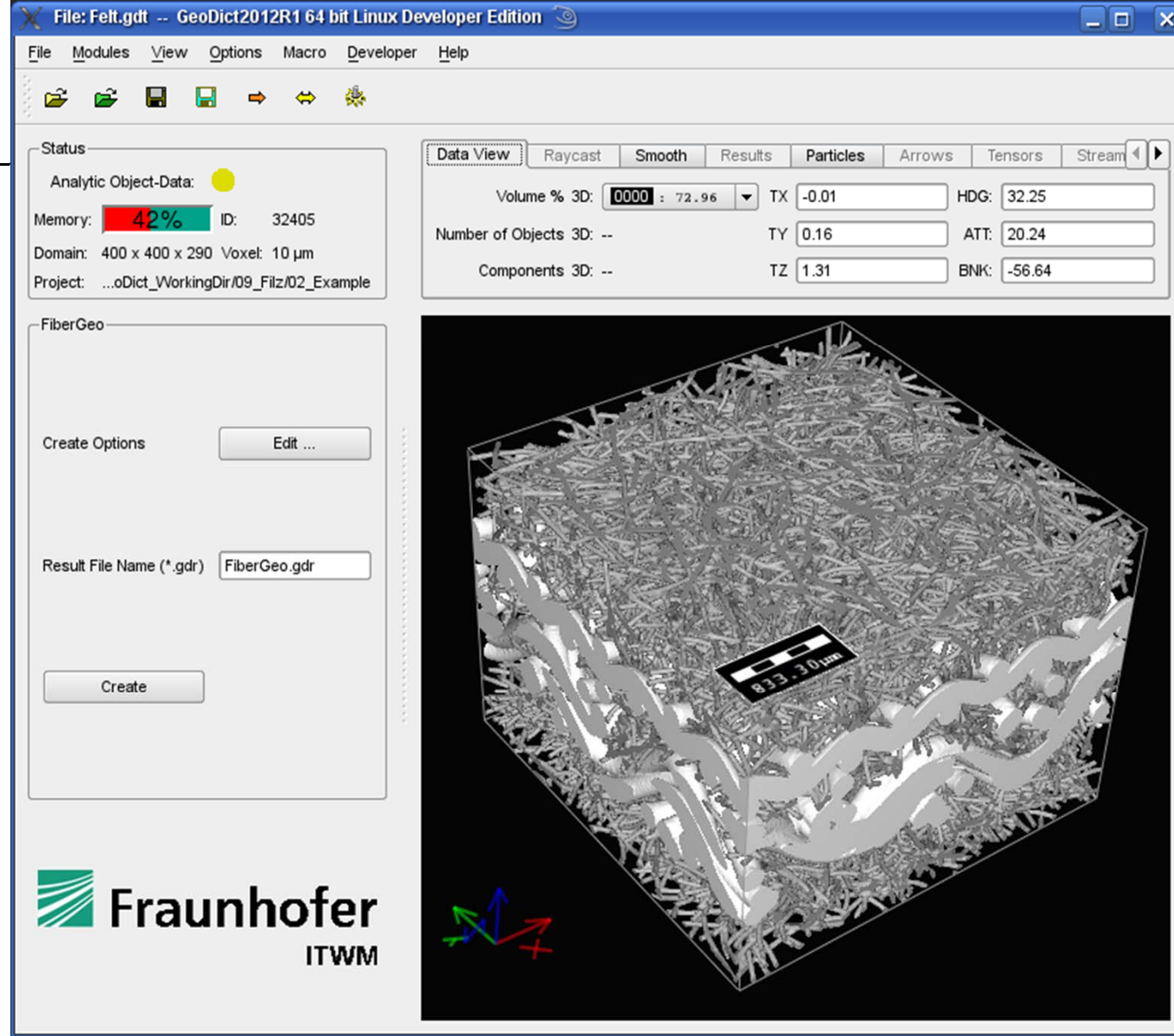
weave.gmc



Virtual felt: woven, nonwoven & needling



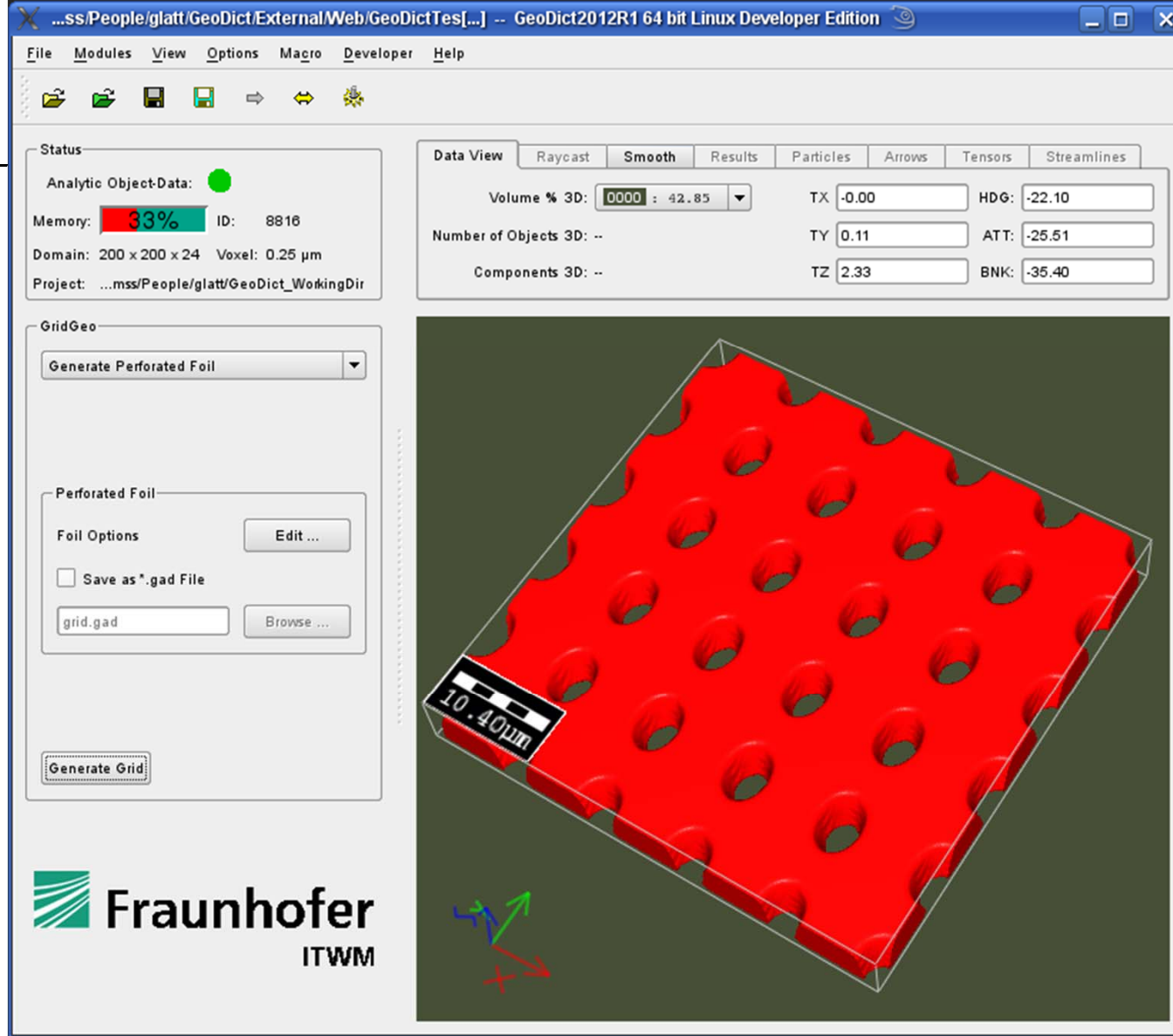
felt.gmc



Virtual foil: oval & conical holes in arbitrary patterns



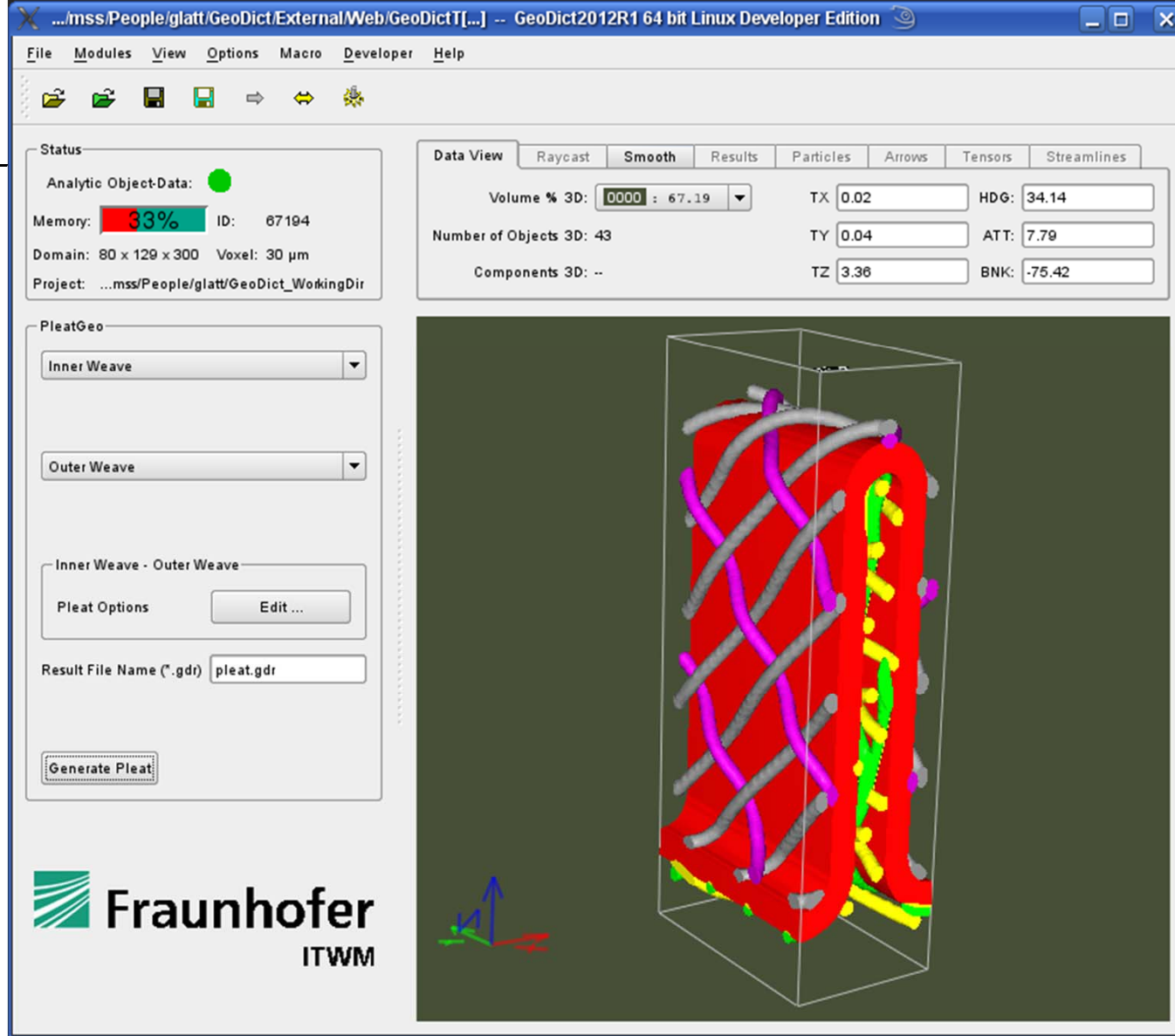
foil.gmc



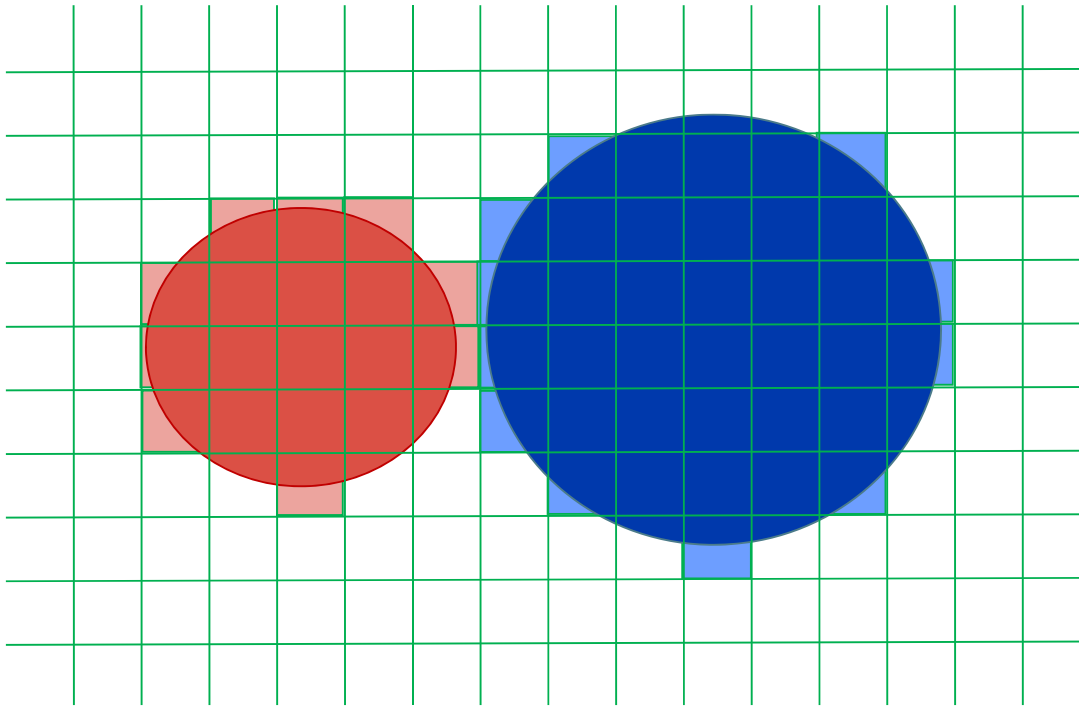
Virtual pleat: filter media + interior and exterior support structures



pleat.gmc



GeoDict structures & simulations are based on infinitesimal cubes



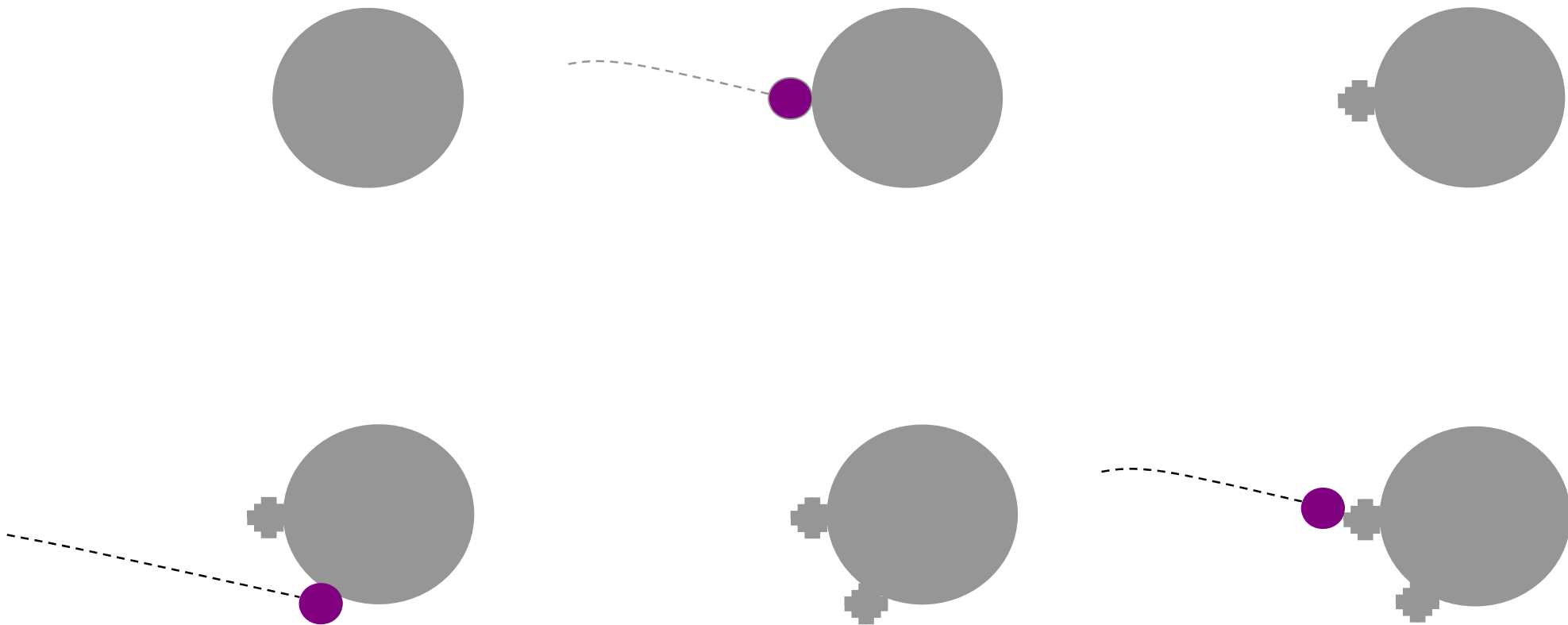
Advantages

- Saves grid generation times
- Compatible with computer tomography
- Straight forward structure generation
- Straight forward solver implementation
- Straight forward parallel computations

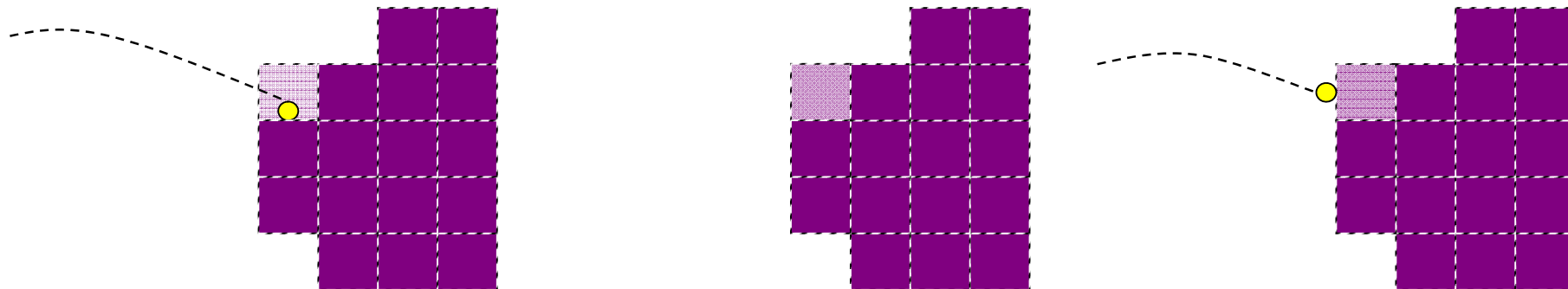
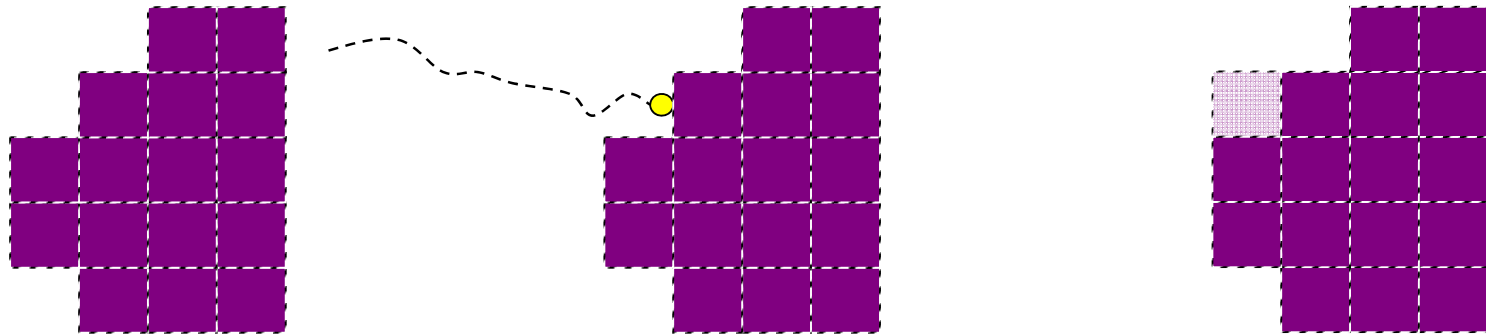
Disadvantages

- Resolved features require many grid cells
- Leads to very large scale computations

Nano-Mode: particle resolved by voxel grid



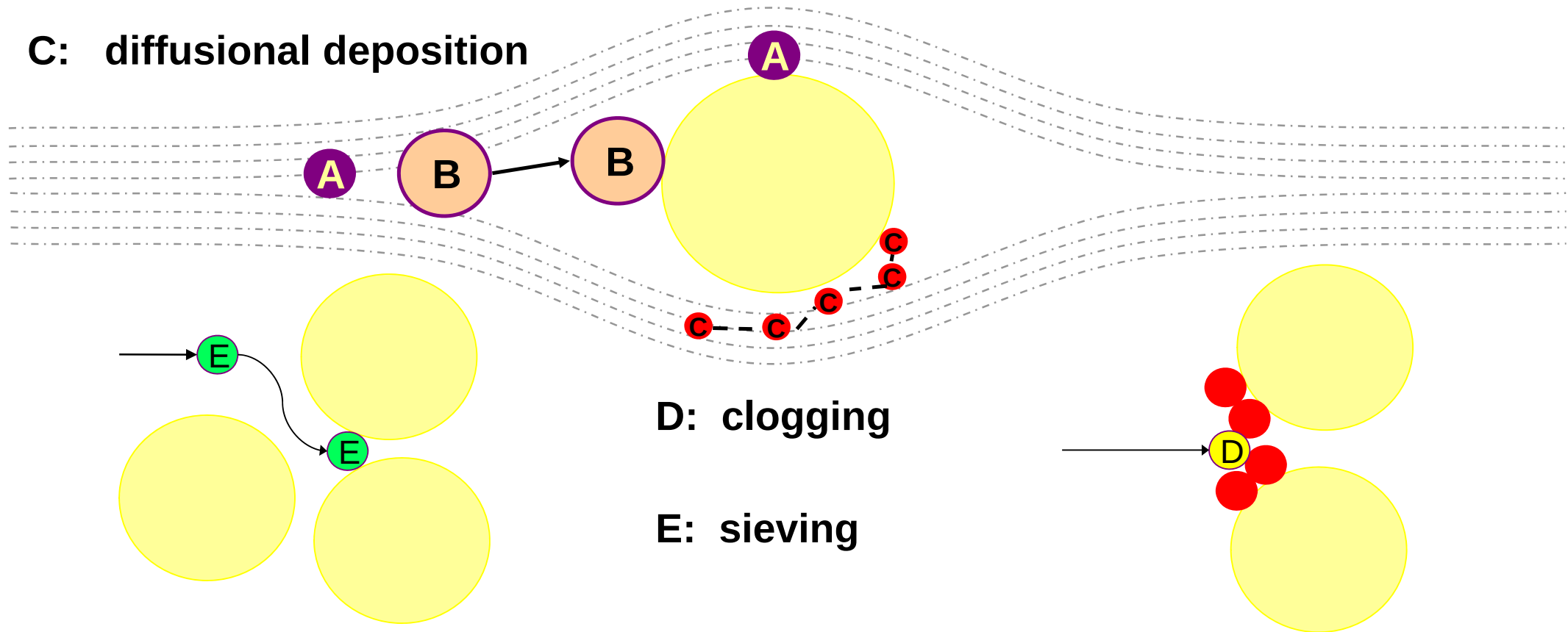
Mikro-Mode: particle not resolved by voxel grid



A: direct interception

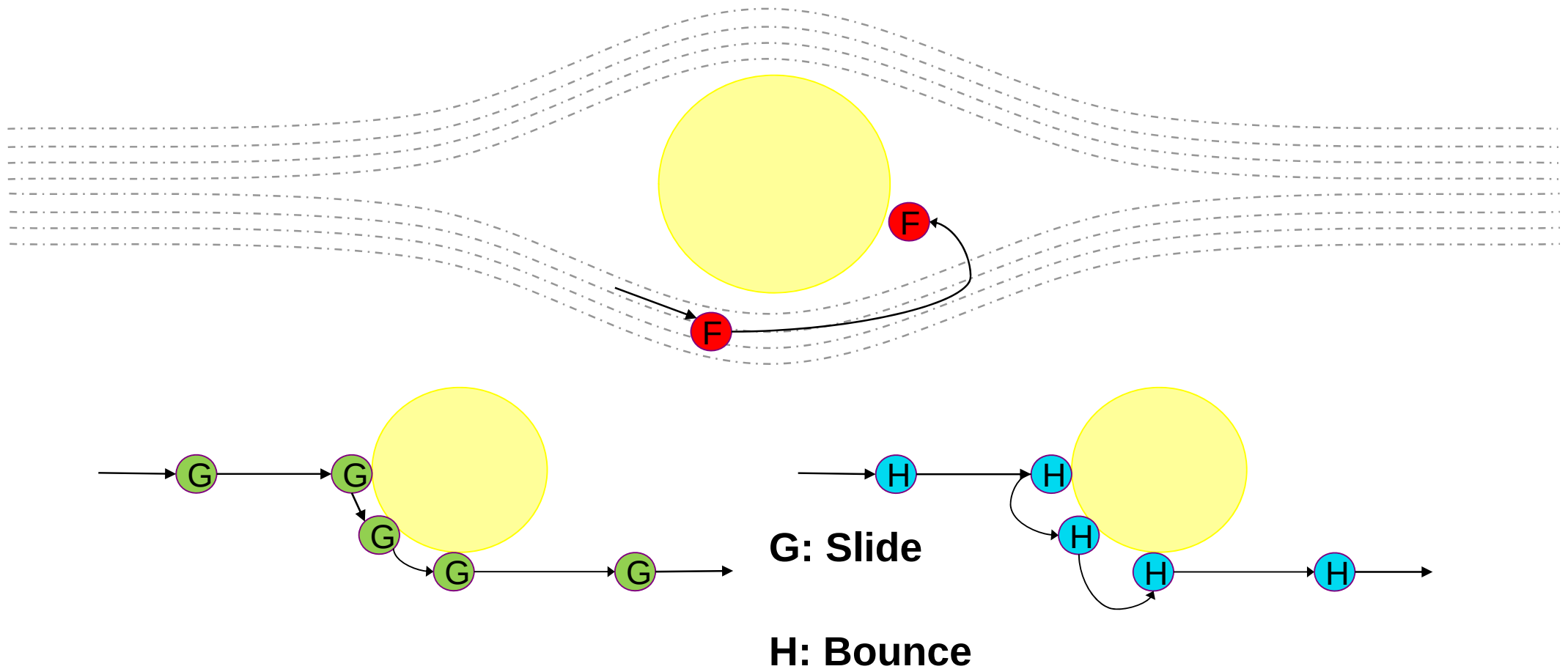
B: inertial impaction

C: diffusional deposition



Filtration Effects II and modes of particle motion

F: electrostatic attraction



$$d\vec{x} = \vec{v} dt, \quad \text{Friction with fluid} \quad \text{Electric attraction} \quad \text{Diffusive motion}$$

$$d\vec{v} = -\gamma \times (\vec{v}(\vec{x}) - \vec{v}_o(\vec{x})) dt + \frac{Q\vec{E}_o(\vec{x})}{m} dt + \sigma \times d\vec{W}(t),$$

$$C_c = 1 + Kn \left(1.142 + 0.558 e^{-0.999/Kn} \right),$$

$$\gamma = 6\pi\rho\mu\frac{R}{C_cm},$$

$$\sigma^2 = \frac{2k_BT\gamma}{m},$$

$$\langle dW_i(t), dW_j(t) \rangle = \delta_{ij} dt,$$

$$Kn = \frac{\lambda}{R},$$

$$\lambda = \frac{k_BT}{\sqrt{32\pi}R^2P}$$

t : time

$\vec{x}$: particle position

$\vec{v}$: particle velocity

R : particle radius

m : particle mass

q : particle charge

T : ambient temperature

P : total pressure

$d\vec{W}(t)$: 3d probability (Wiener) measure

γ : friction coefficient

k_B : Boltzmann constant

$\vec{E}_o$: electric field

$\vec{v}_o$: fluid velocity

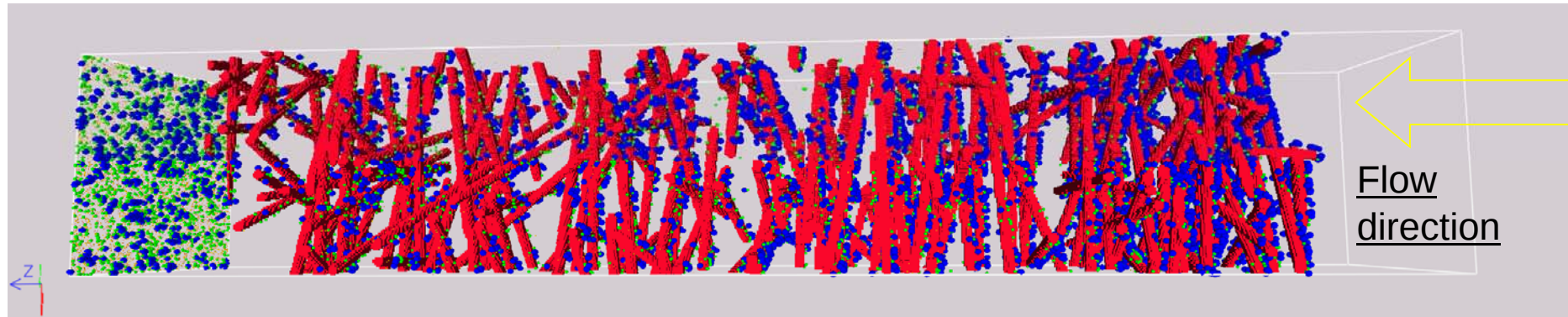
ρ : fluid density

μ : fluid viscosity

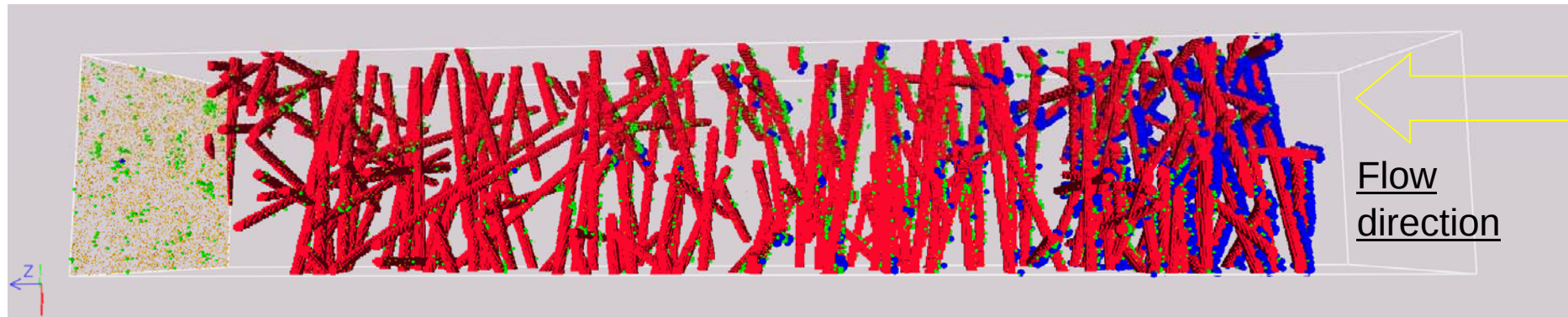
$$\alpha = 0.05,$$
$$d_F = 14,$$
$$v = 0.1\text{m/s}$$

Deposition effects

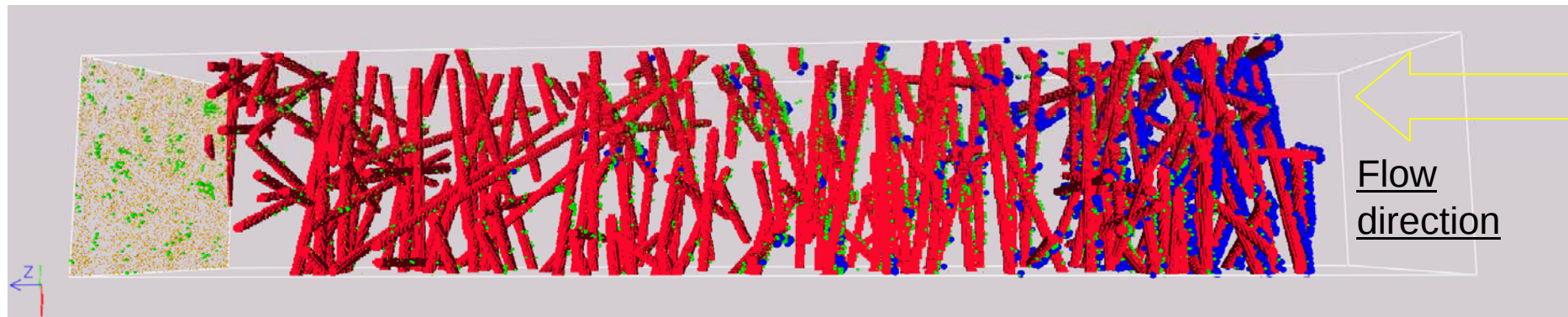
Interception



Interception
+ Impaction



Interception
+ Impaction
+ Diffusion



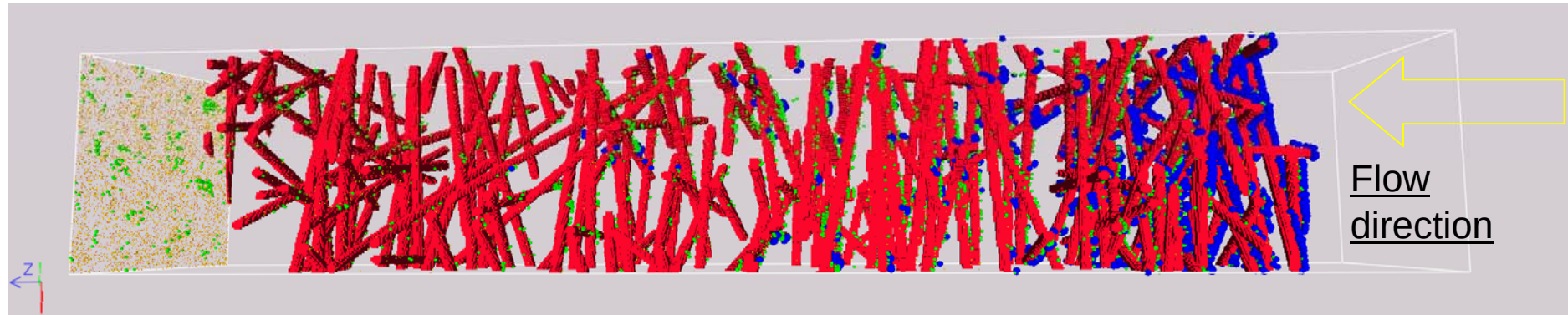
$$\alpha = 0.05,$$

$$dF = 14,$$

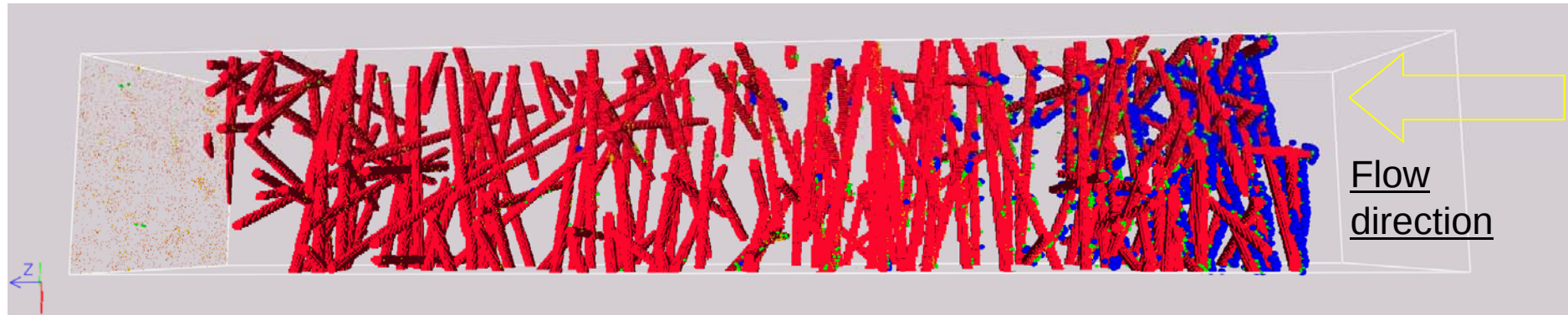
Interception + Impaction + Diffusion

Velocity Effects

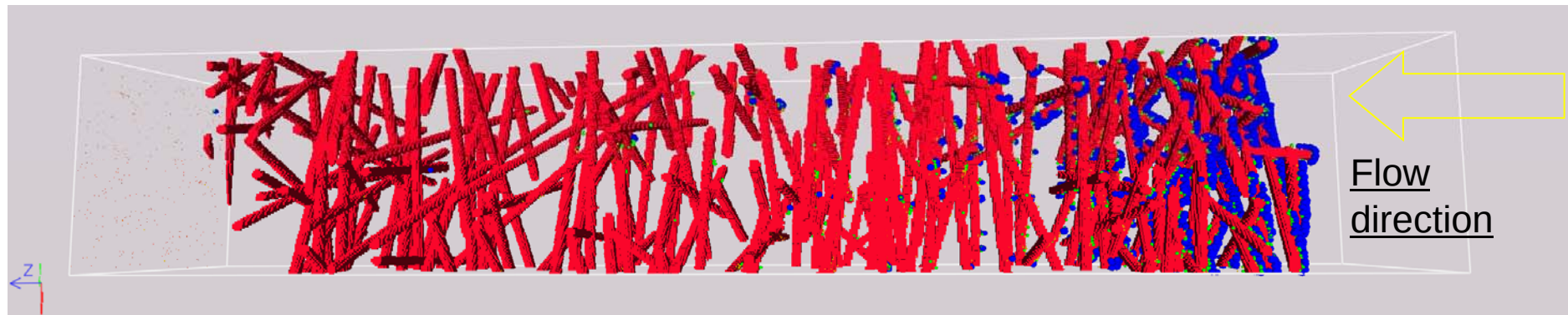
Velocity
 $v = 0.1 \text{ m/s}$



Velocity
 $v = 1 \text{ m/s}$



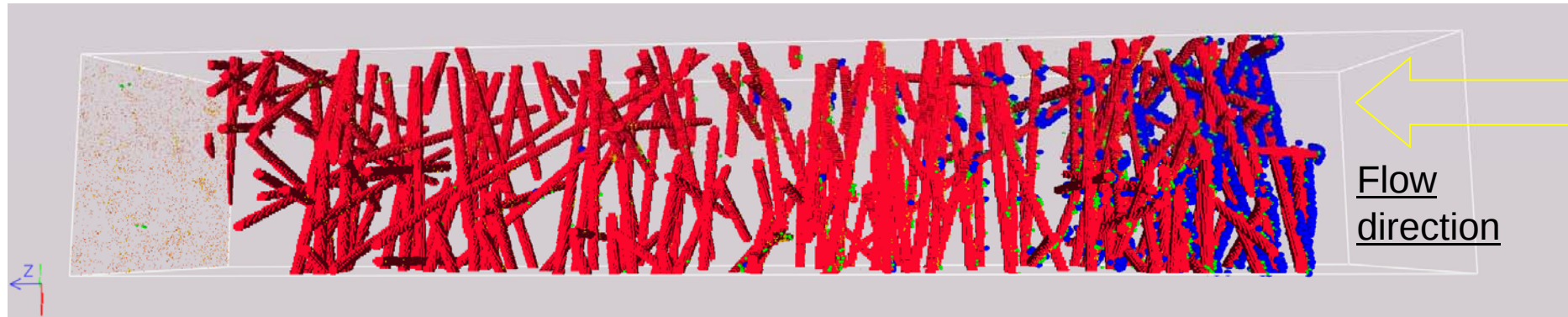
Velocity
 $v = 10 \text{ m/s}$



$dF = 14$,
 $v = 1$ m/s,
Interception + Impaction + Diffusion

Effect of grammage (here: SVF)

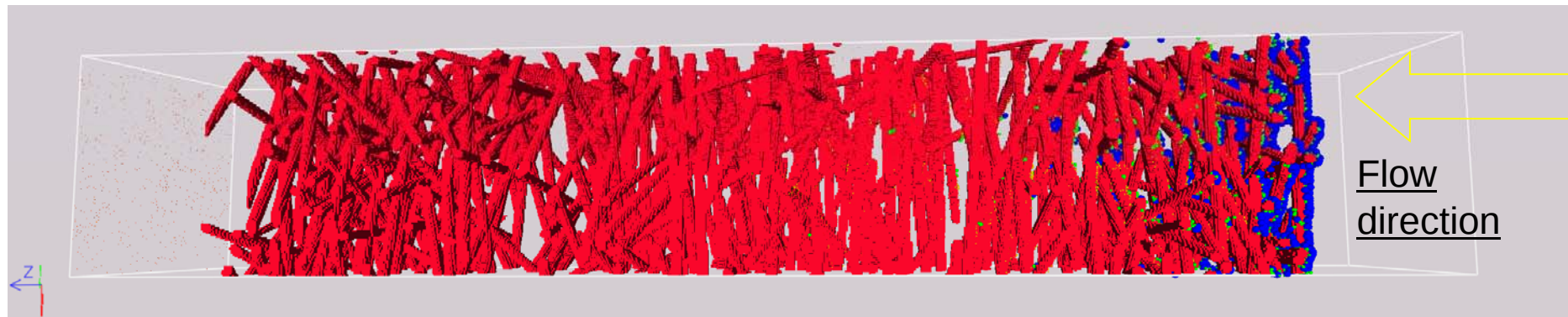
SVF $\alpha=0.05$



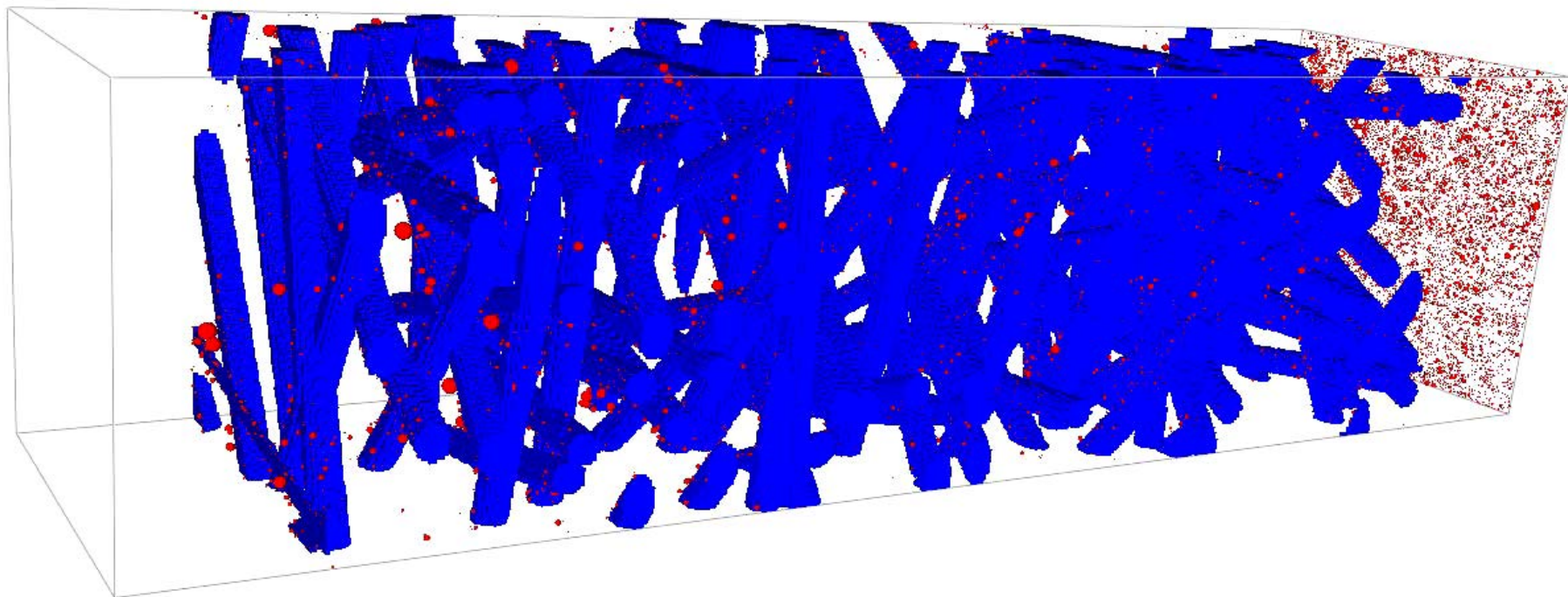
SVF $\alpha=0.07$



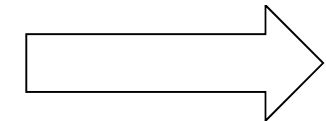
SVF $\alpha=0.1$

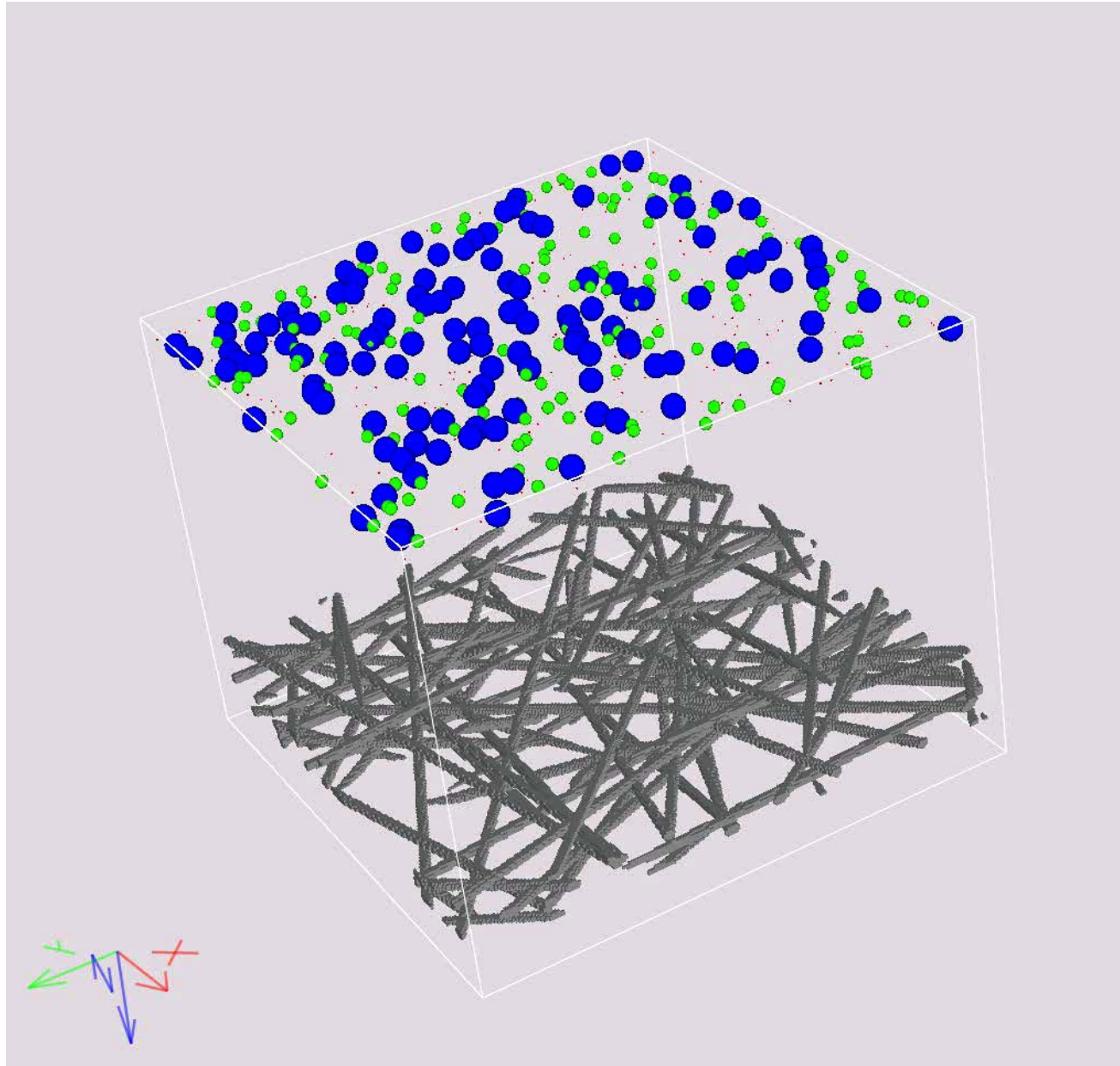


Transition from depth filtration to cake filtration in a single simulation

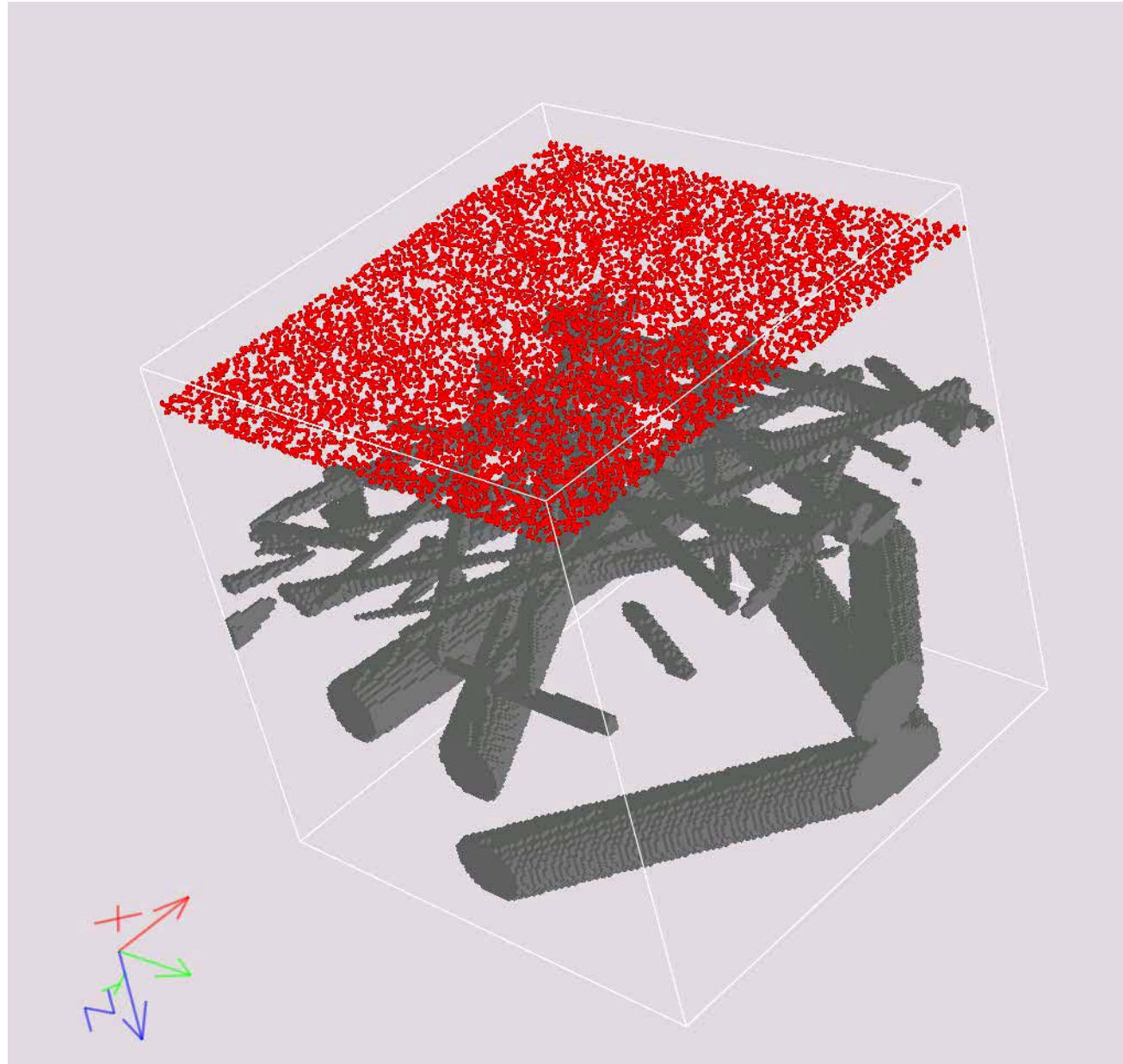


Flow
direction





- Filter Efficiency evolution
- Pressure drop evolution



➤ Uncleaned particles

GeoDict contributions at Fraunhofer ITWM: 2001 - 2012

GeoDict

Andreas Wiegmann
Jürgen Becker
Erik Glatt
Stefan Rief
Heiko Andrä
Sven Linden
Kilian Schmidt
Ashok Kumar Vaikuntam
Rolf Westerteiger
Christian Wagner
Mohammed Alam
Jianping Shen

UsersGuide

Barbara Planas
Vita Rutka
Stefan Rief
Andreas Wiegmann

PoroDict / MatDict

Erik Glatt
Andreas Wiegmann
Jürgen Becker
Kilian Schmidt
Rolf Westerteiger

PleatDict

Andreas Wiegmann
Oleg Iliev
Stefan Rief
Liping Cheng

FilterDict

Jürgen Becker
Stefan Rief
Arnulf Latz
Andreas Wiegmann
Kilian Schmidt
Christian Wagner
Rolf Westerteiger

ThermoDict EJ Solver

Andreas Wiegmann
Liping Cheng
Rolf Westerteiger

FlowDict Lattice Boltzmann

Peter Klein
Dirk Merten
Konrad Steiner
Dirk Kehrwald
Irina Ginzburg
Doris Reinel-Bitzer

FlowDict EJ Solver

Liping Cheng
Andreas Wiegmann
Aivars Zemitis
Rolf Westerteiger
Donatas Elvikis
Vita Rutka
Qing Zhang

DiffuDict Knudsen Solver

Jürgen Becker

ElastoDict

Heiko Andrä
Matthias Kabel
Liping Cheng
Andreas Wiegmann
Vita Rutka
Donatas Elvikis

FlowDict EFV Solver

Andreas Wiegmann
Liping Cheng

FiberGeo

Jürgen Becker
Erik Glatt
Andreas Wiegmann
Katja Schladitz
Joachim Ohser
Hans-Karl Hummel
Petra Baumann

WeaveGeo

Erik Glatt
Andreas Wiegmann
Rolf Westerteiger

SatuDict

Jürgen Becker
Andreas Wiegmann
Volker Schulz
Rolf Westerteiger

SinterGeo

Jürgen Becker
Erik Glatt
Norman Ettrich
Kilian Schmidt

PleatGeo

Erik Glatt
Andreas Wiegmann
Jürgen Becker

PackGeo

Erik Glatt
Andreas Wiegmann
Joachim Seibt

GridGeo

Erik Glatt
Liping Cheng
Andreas Wiegmann
Rolf Westerteiger

RenderGeo

Matthias Groß
Sven Linden
Carsten Lojewski
Rolf Westerteiger

PaperGeo

Erik Glatt

www.geodict.com

www.math2market.de

Thank you for your attention