



**ENERGY AND TRANSPORT SCIENCES LABORATORY**

Department of Mechanical Engineering  
Texas A&M University



# Analysis of Long-range Interactions in Lithium-ion Battery Electrodes

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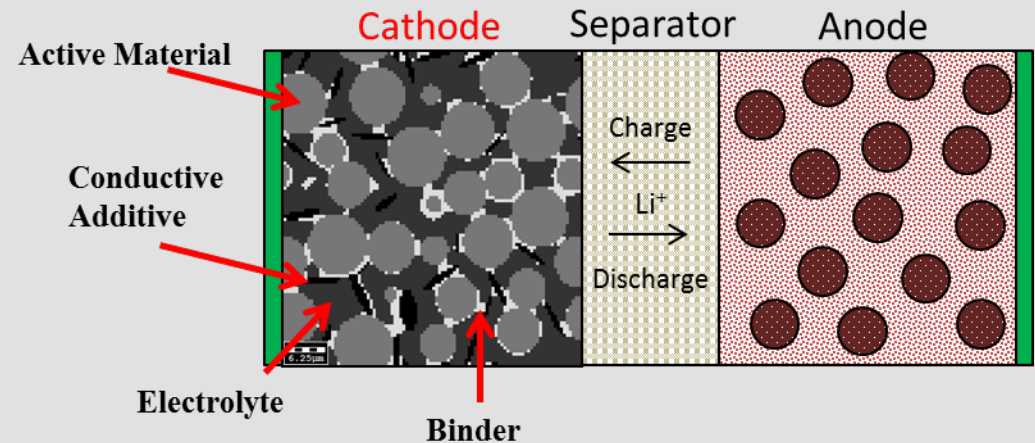
# Overview

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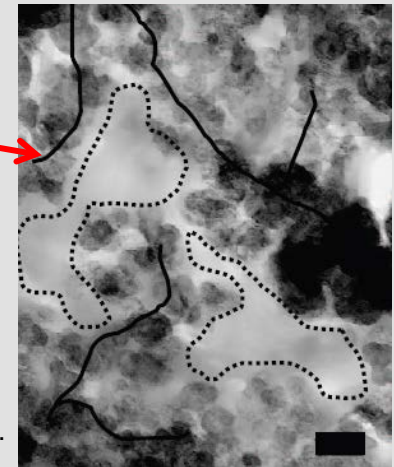
- ❖ Background/Motivation
- ❖ Objective
- ❖ Methodology
- ❖ Results
- ❖ Conclusions
- ❖ Outlook

# Background/Motivation

- ❖ Battery composition: anode, cathode, porous separator, and current collectors
- ❖ Cathode composition: active material, conductive additives, binder, and an electrolyte.
- ❖ Low component electrical conductivity necessitates use of conductive additive
- ❖ Improvement in conductivity is dependent on percolation, or pathway formation



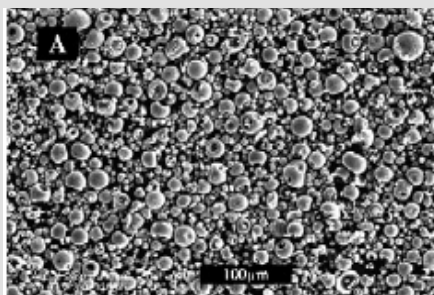
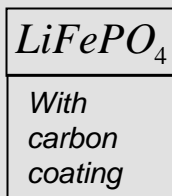
Conductive additive pathway formation



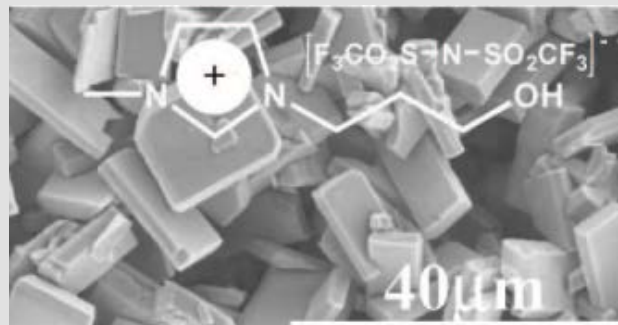
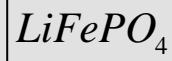
Adapted from V. S. Battaglia, G. Liu, X. Song and H. Zheng, *J. Electrochem. Soc.*, **159**, A214 (2012).

# Background/Motivation

- ❖ Additive type and material content have been shown to affect pathway formation and thus electrical conductivity
  - Pathway formation is dependent on particle interaction within electrode
- ❖ Active material particle shape can be altered or can vary based on chemistry



Adapted from J. Liu, J. Wang, X. Yan, X. Zhang, G. Yang, A.F. Jalbout and R. Wang, *Electrochim. Acta*, **54**, 5656 (2009).



Adapted from N. Recham, L. Dupont, M. Courty, K. Djellab, D. Larcher, M. Armand and J.M. Tarascon, *Chem. Mater.*, **21**, 1096 (2009).

- Variation in AM shape could alter the effectiveness of conductive additives



# Objective

## ❖ Objective

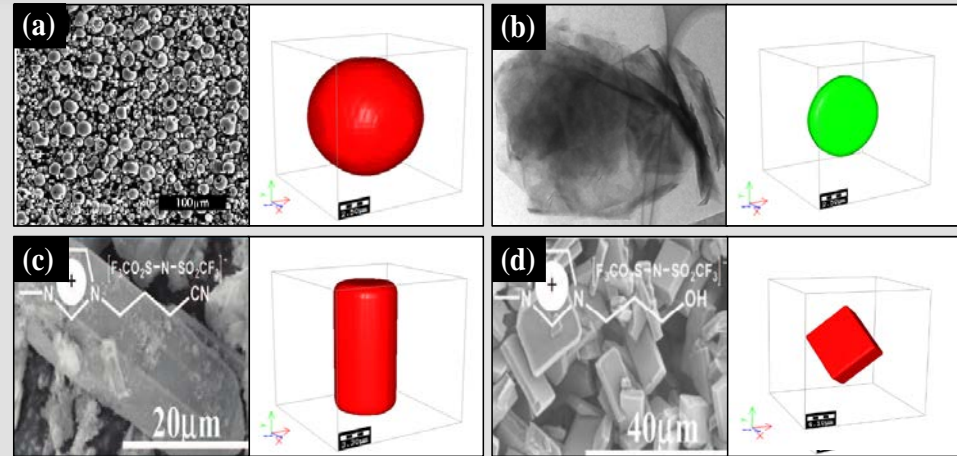
- Determine the effect of active material morphology and electrode composition on the effective conductivity of LIBs.

## ❖ Tasks

- Stochastically generate 3D electrodes (**GeoDict**)
- Evaluate effective electrical conductivity (**GeoDict**)
- Characterize results and draw conclusions

# Methodology – Particle Modeling

- ❖ Finite-volume based modeling approach
- ❖ AM particles modeled as pseudo-spherical, pseudo-cylindrical, and platelet particles
- ❖ Graphite modeled as thin, ellipsoidal disks
- ❖ Volume set constant, with standard deviations set for equivalent volume change
- ❖ Conductivity of additive is much higher than remaining components

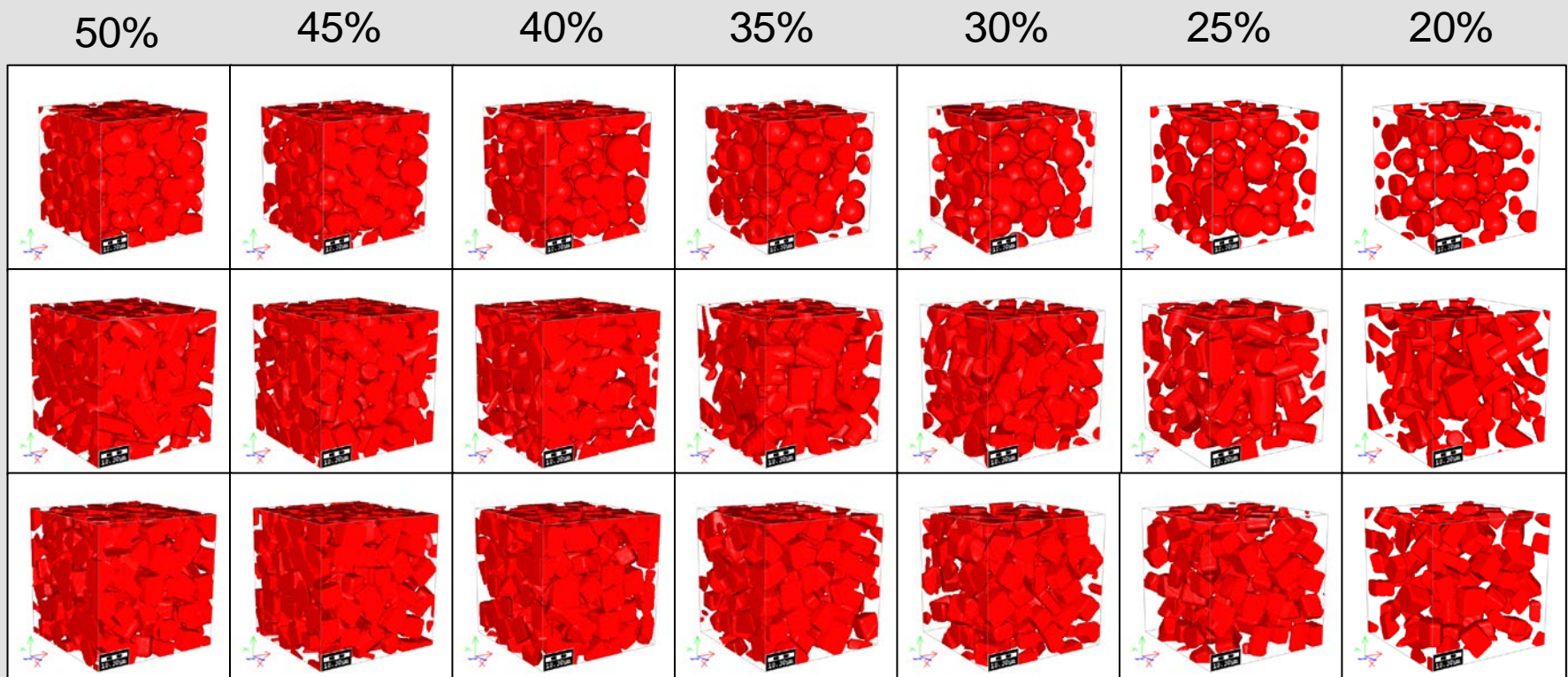


AM Particle	Length	Diameter	Volume	Surface Area
Sphere	--	9.0 $\mu\text{m}$	3.82 E-16 $\text{m}^3$	2.55 E-10 $\text{m}^2$
Cylinder	12.48 $\mu\text{m}$	6.24 $\mu\text{m}$	3.82 E-16 $\text{m}^3$	3.06 E-10 $\text{m}^2$
Platelet	7.25 $\mu\text{m}$	--	3.82 E-16 $\text{m}^3$	3.16 E-10 $\text{m}^2$

Material	Electrical Conductivity
Active Material	.01 S/m
Electrolyte	1 S/m
Graphite	$1.0 \times 10^4$ S/m
PVDF	$1.0 \times 10^{-13}$ S/m





# Methodology – Model Generation

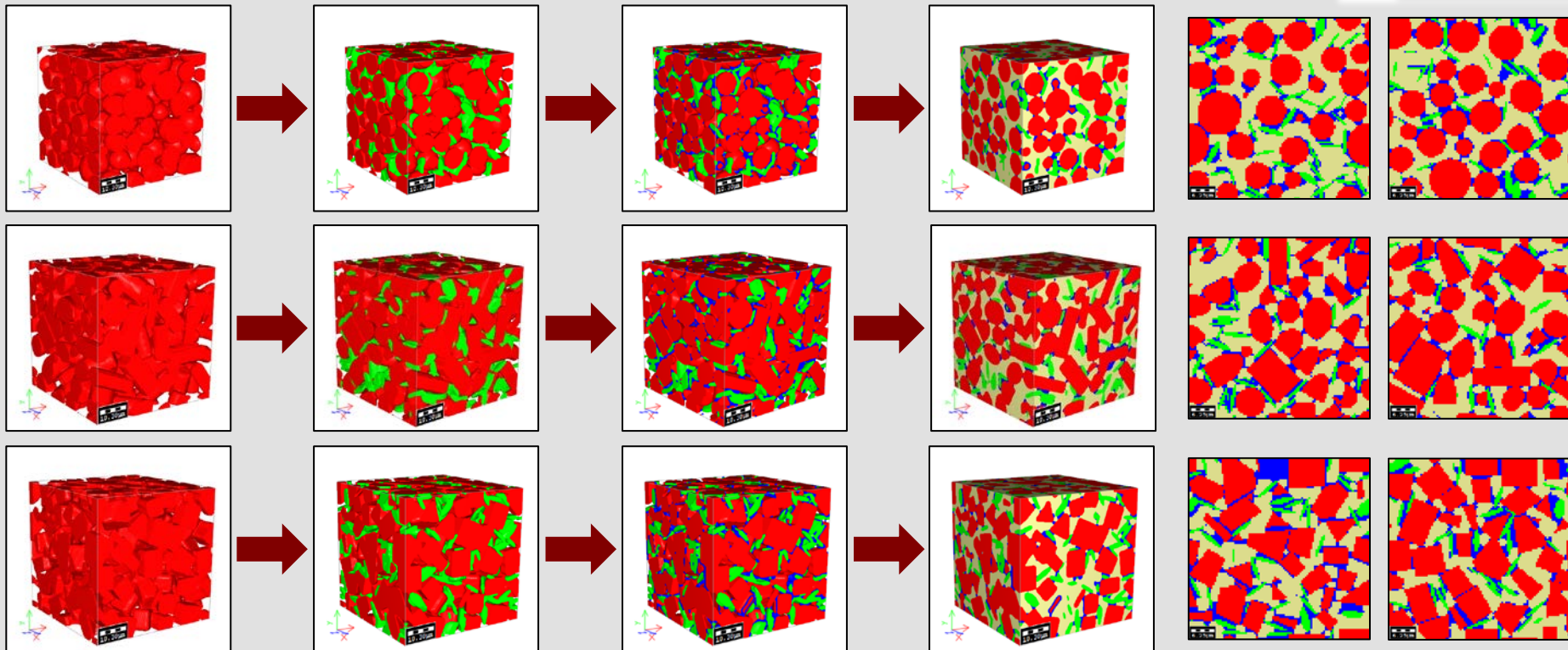
- ❖ Three groups of seven cells were generated in **GeoDict** using spheres, cylinders, and cubes of equal volume
- ❖ Volume percent of each cell was varied from 20 to 50 percent in constant intervals
- ❖ Later, conductive additive and binder are added also with **GeoDict**



# Methodology – Model Generation

- ❖ Ratio of conductive additive to binder kept constant at 0.8:1.0
- ❖ Porosity maintained at 35%
- ❖ Decrease in AM correspond to increase in additive and binder

	Active Material
	Conductive Additive
	Binder
	Electrolyte



# Methodology – Conductivity

- ❖ Effective conductivity determined via the 3D stationary conduction equation

$$\nabla(\sigma \nabla V) = \dot{j} \text{ in } \varphi$$

where  $V$  is the potential,  $\sigma$  is the local electrical conductivity,  $\dot{j}$  is a source term, and  $\Phi$  is the domain under consideration.

- ❖ Only conduction through the domain is considered so  $\dot{j} \rightarrow 0$ .
- ❖ Potential is the same for two objects on opposite sides of an interface
- ❖ Solution is implemented in simulation package **GeoDict**<sup>TM</sup>

**GeoDict**<sup>TM</sup> is a trademark of Math2Market GmbH, Kaiserslautern Germany.





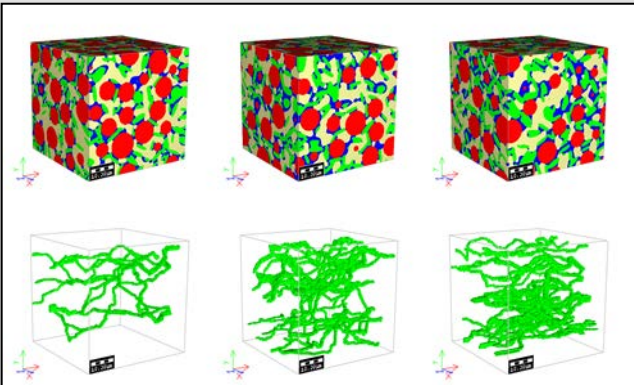
# Results – Percolation

- ❖ Higher degree of percolation occurs with lower volume % AM
- ❖ Effective conductivity increases with path number and decreasing overall path tortuosity
- ❖ Percolation, effective conductivity and tortuosity are available in **GeoDict™**

	Conductive Paths	Conductivity (S/m)	Tortuosity
<b>Sphere</b>			
35%	11	17.4	1.89
30%	39	28.2	1.54
25%	52	55.3	1.38
20%	97	81.8	1.42
<b>Cylinder</b>			
35%	2	8.52	1.54
30%	10	23.1	1.51
25%	59	61.6	1.48
20%	84	70.7	1.42
<b>Platelet</b>			
35%	1	4.95	1.61
30%	11	29.0	1.39
25%	46	46.1	1.51
20%	92	78.6	1.41

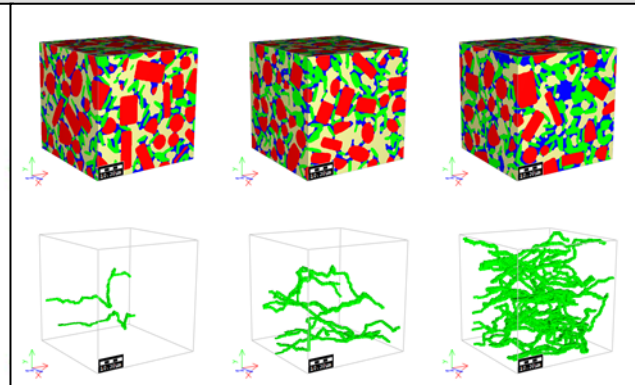
Pseudo-Spherical

35% 30% 25%



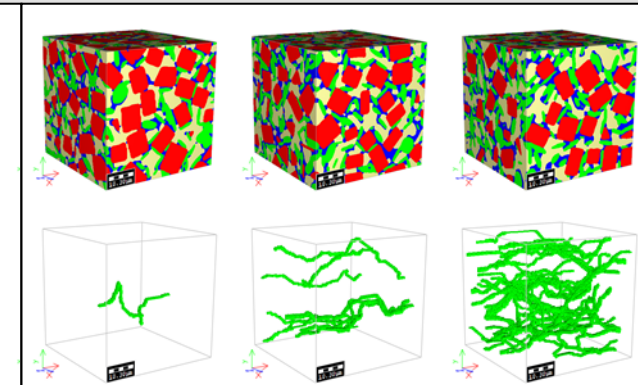
Pseudo-Cylindrical

35% 30% 25%



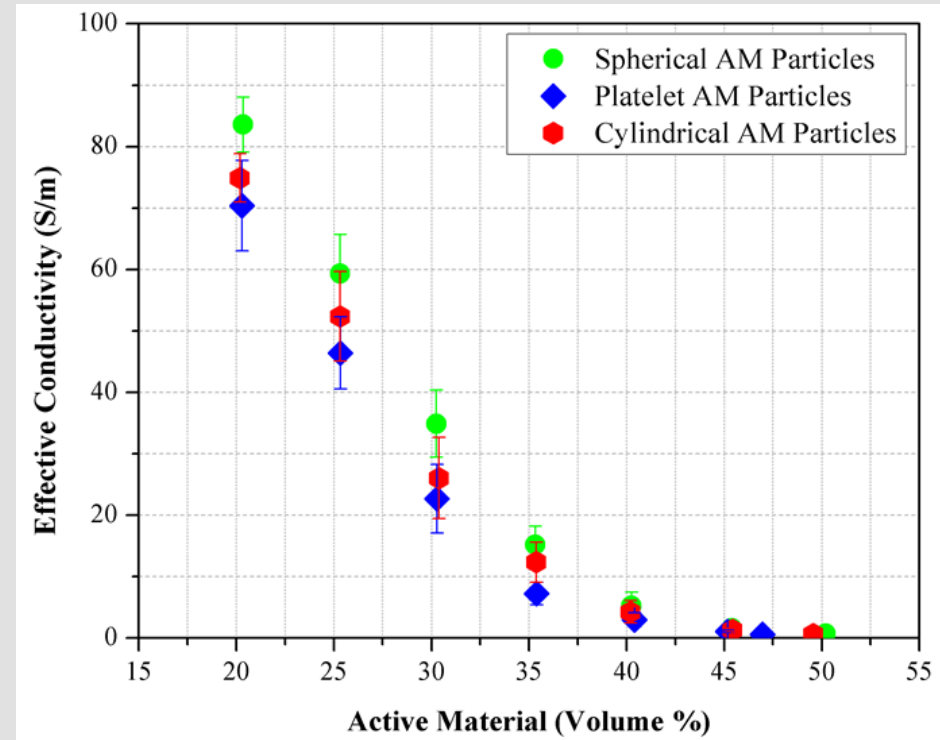
Platelet

35% 30% 25%

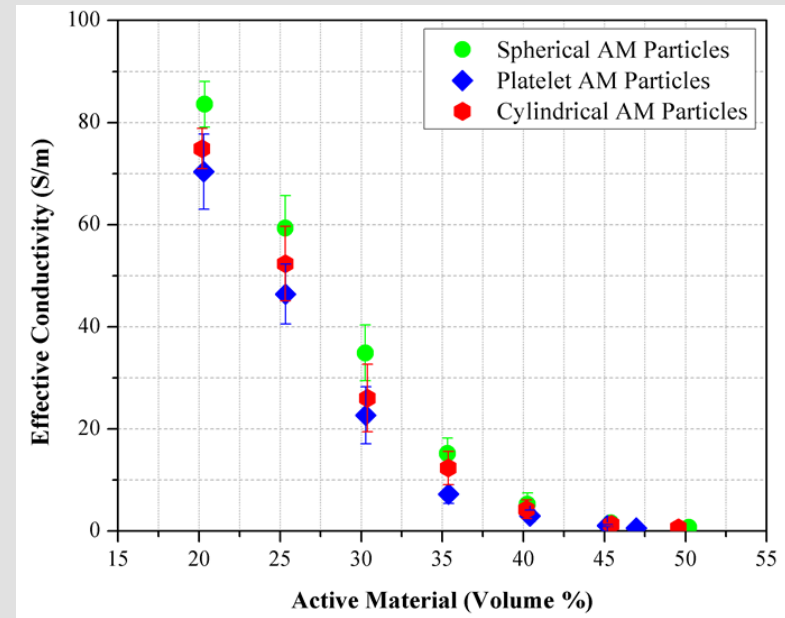
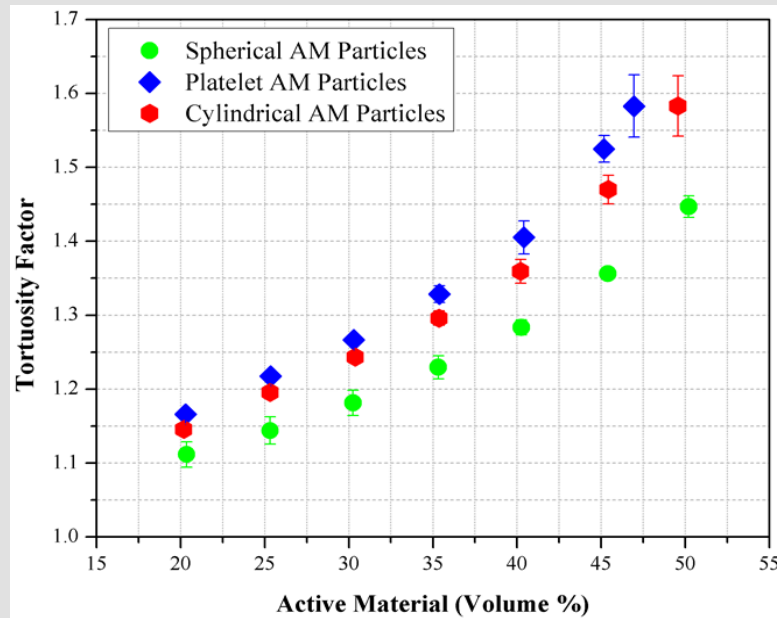


# Results – Effective Conductivity

- ❖ Simulation results for the effective electrical conductivities for each set of electrodes are shown to the right.
- ❖ Averaged data were plotted in the figure, with error bars of  $\pm\sigma$ .
- ❖ At  $> 35\%$  AM,  
 $\sigma_{\text{eff-sphere}} \square \sigma_{\text{eff-cylinder}} \square \sigma_{\text{eff-cube}}$
- ❖ At  $25\%-35\%$  AM,  
 $\sigma_{\text{eff-sphere}} \square \sigma_{\text{eff-cube}}$
- ❖ At  $20\%$ ,  
 $\sigma_{\text{eff-sphere}} > \sigma_{\text{eff-cylinder}} \approx \sigma_{\text{eff-cube}}$
- ❖ Distribution of AM affects pathway formation  
→ quantified in terms of tortuosity



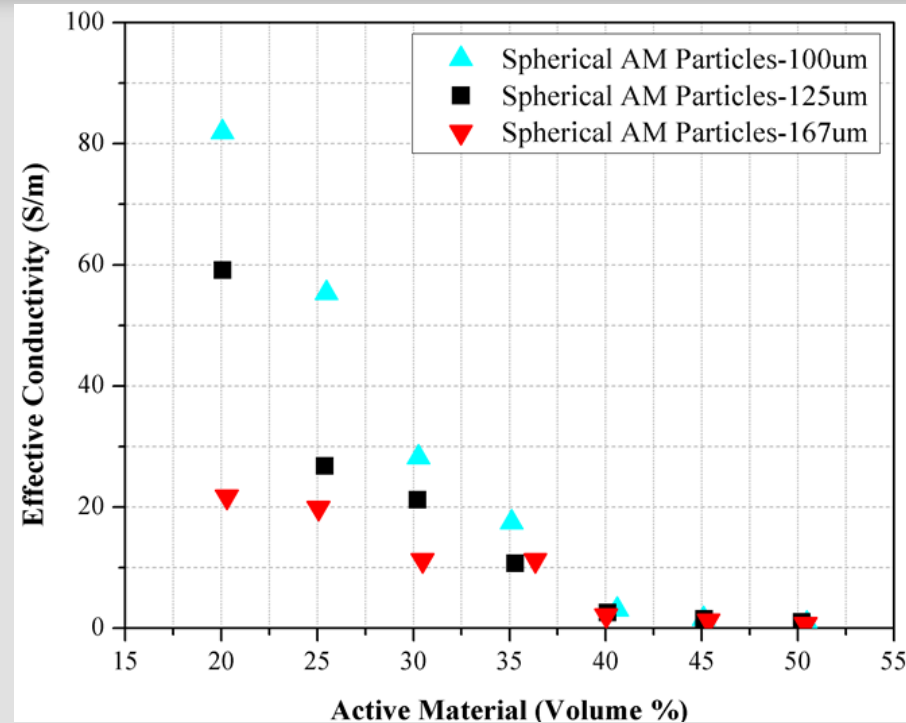
# Results – Tortuosity Factor



- ❖ Tortuosities  $\uparrow$  with  $\uparrow$  in active material particle surface area ( $Sa_{\text{sphere}} < Sa_{\text{cylinder}} < Sa_{\text{cube}}$ )  
where  $Sa$  is the surface area for each active material shape
- ❖ Above a certain tortuosity threshold, the formation of pathways is very difficult
- ❖ General trend can be seen in terms of average effective conductivity and tortuosity factor
- ❖ Random nature of pathway formation obscures this



# Results – Resolution



- ❖ Electrodes consisting of spherical active material particles at varying resolution created
- ❖ Trends expected to be similar for all AM shapes
- ❖ General increase in conductivity with voxel size
- ❖ Lowest resolution utilized for speed; experimental validation required

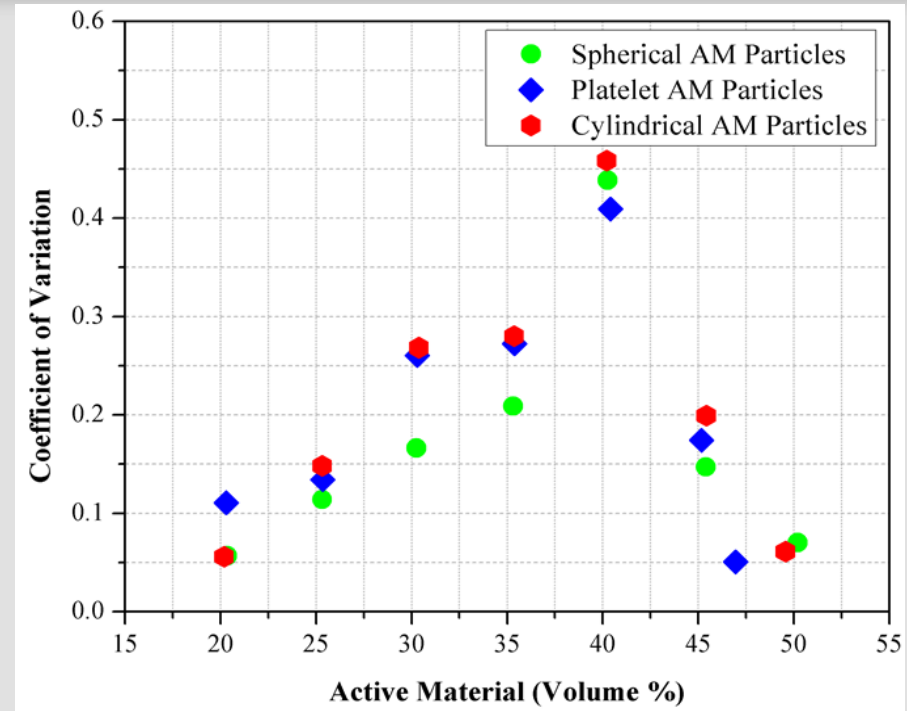
# Results – Domain Size

- ❖ Domain must be large enough to obtain consistent results
- ❖ Domain length/Particle diameter ratio chosen as >5
- ❖ To ensure that the generated models were free from variation of size effect, the coefficient of variation was evaluated for the final conductivity data.

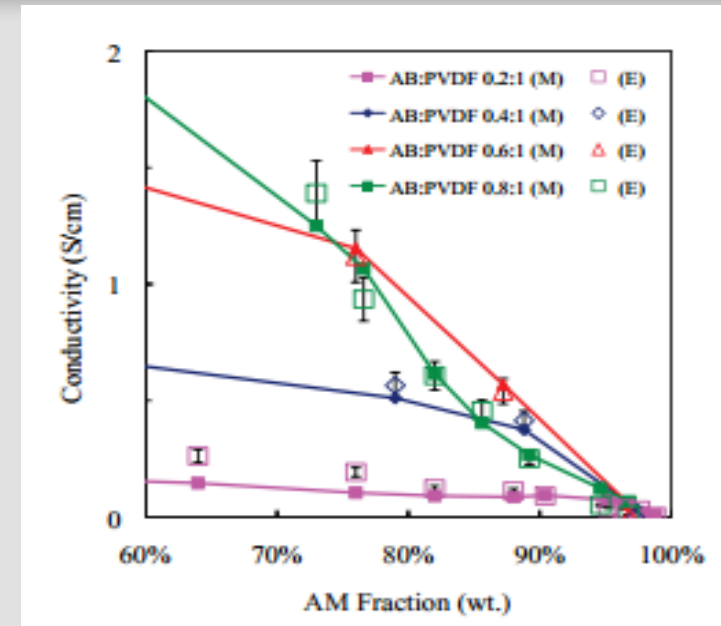
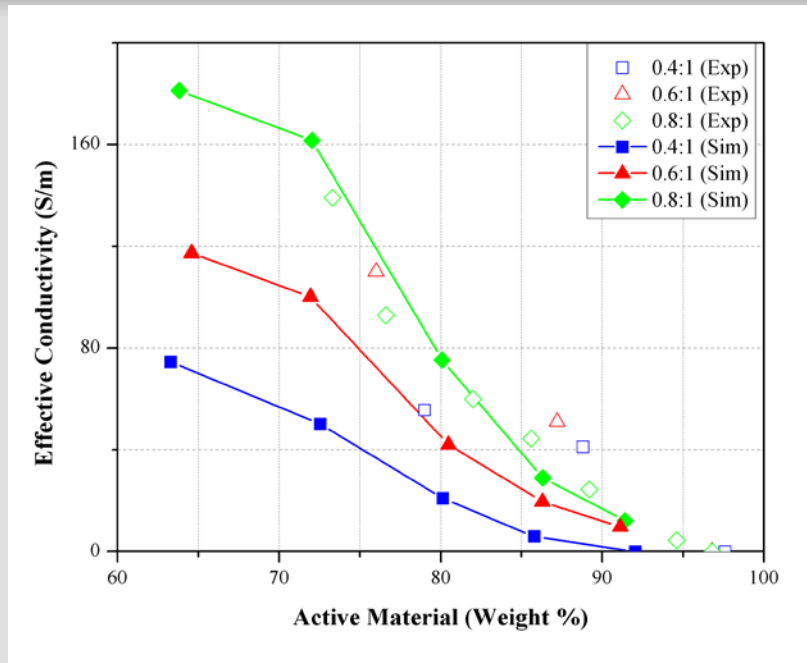
$$CV = \frac{\sigma}{\mu} \quad \begin{array}{ll} 0.0 < CV < 0.5 & \text{homogenous} \\ 0.5 < CV < 1.0 & \text{heterogeneous} \\ 1.0 < CV & \text{very heterogeneous} \end{array}$$

where  $\sigma$  is the standard deviation and  $\mu$  is the arithmetic mean

- ❖ Evaluation of coefficient of variation reveals acceptable level of homogeneity



# Results – Model Validation



Adapted from V. S. Battaglia, G. Liu, X. Song and H. Zheng, *J. Electrochem. Soc.*, **159**, A214 (2012).

- ❖ Separate set of models made to correlate with results of Liu et. al.
- ❖ Percolation achieved at 4% acetylene black by weight for both sets
- ❖ A decrease in AM results in an increase in effective conductivity for both sets of data
- ❖ Simulations deviate from experimental data in terms of expected trends based on CA/B ratio

Stein, Wiegmann, Mukherjee, *in preparation* (2013).

# Conclusions

- ❖ At loadings greater than 35% the active material shape does not have a significant bearing on the effective conductivity.
- ❖ For loadings less than 35%, spherical active material particles will likely yield the greatest return for effective conductivity – although this effect could be obscured.

# Outlook/Future Work

- Experimentally validate results and assumptions
- The modeling technique utilized can be extended to more complex geometries for property analysis
- 3D structures generated via this method can be coupled with external programs for electrochemical analysis

# Acknowledgements

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Thank you!