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# Numerical Analysis of Transport Processes in Porous Layers

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Math2Market GmbH

ModVal 11, Winterthur 2014

# Math2Market GmbH

- Founded September 21 2011 in Kaiserslautern.
- Spin-off of Fraunhofer Institute for Industrial Mathematics ITWM. Located in the Business and Innovation Center in Kaiserslautern.
- Business based on GeoDict software formerly developed by ITWM. Continued close cooperation with ITWM on algorithms.



- GeoDict® exists since 2001, first sales in 2003, first sales for filtration (FilterDict® module) in 2005.
- The intellectual property rights to the GeoDict software belong to Math2Market GmbH since January 1, 2013.

# Outline

1. General approach: the virtual material lab
2. Import and analysis of CT data
3. Creating realistic 3D structure models
4. Determination of transport properties

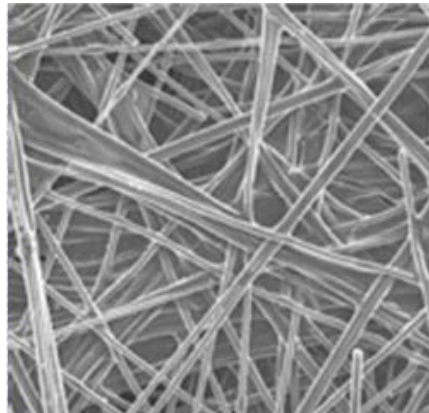
# **1. General Approach: The Virtual Material Lab**

# The Virtual Material Lab Approach:

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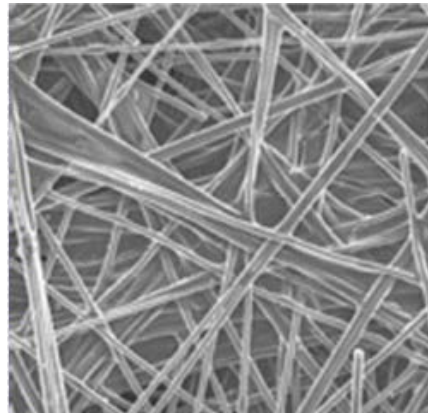
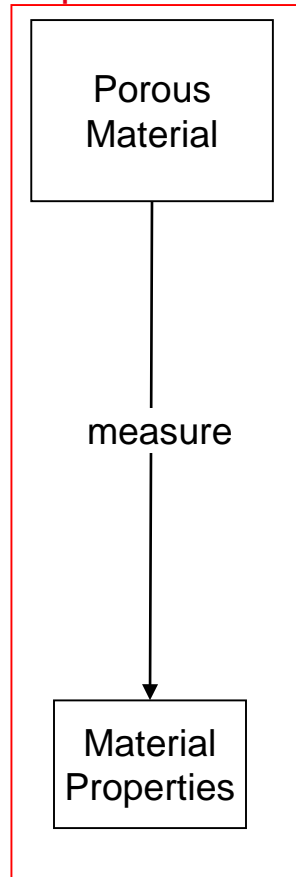
Experiment / Lab

Porous  
Material



# The Virtual Material Lab Approach:

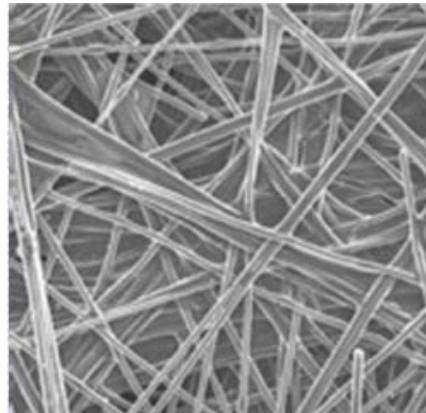
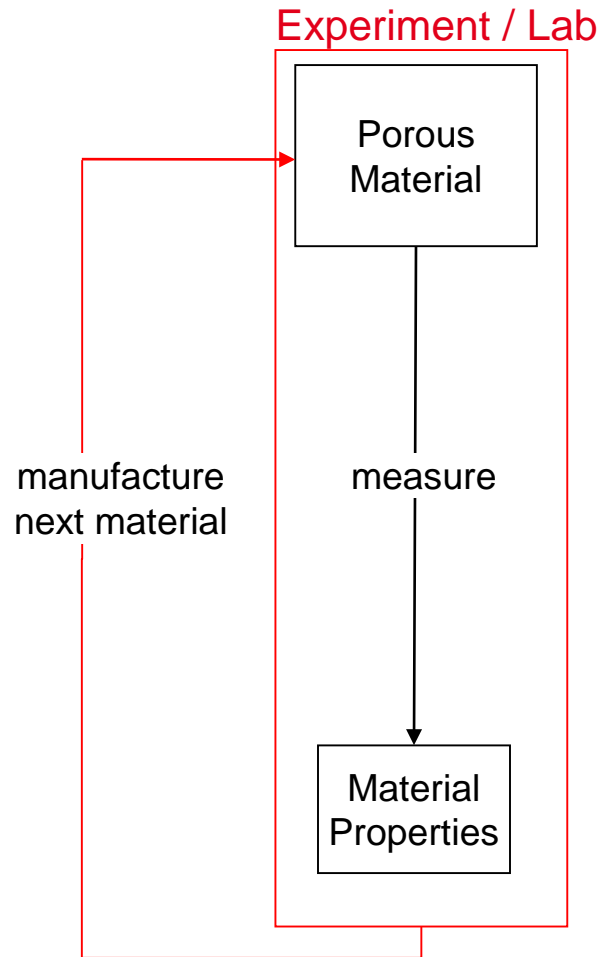
## Experiment / Lab



Properties are:

- pore size distribution
- effective diffusivity
- permeability
- stiffness
- ...

# The Virtual Material Lab Approach:

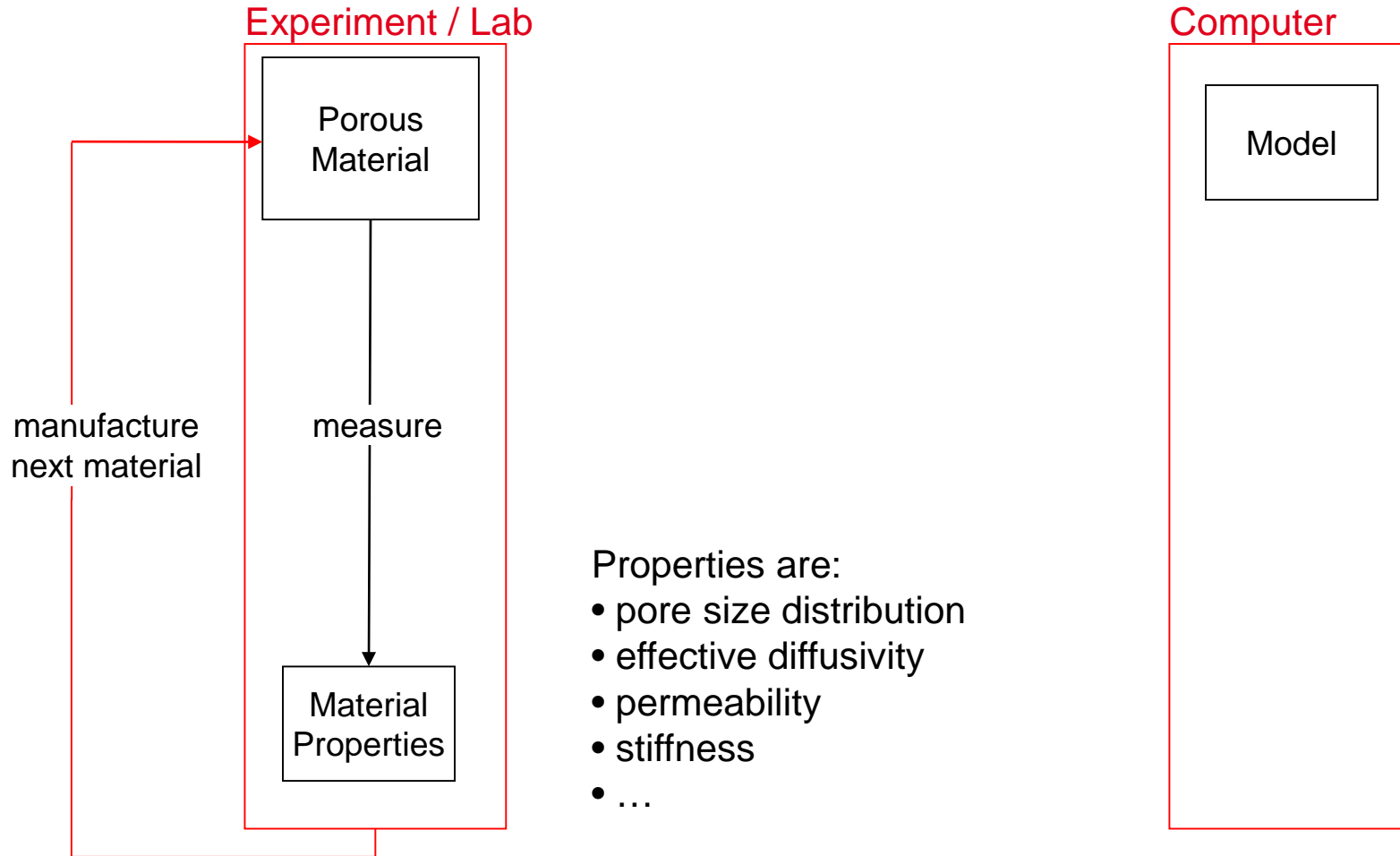


Properties are:

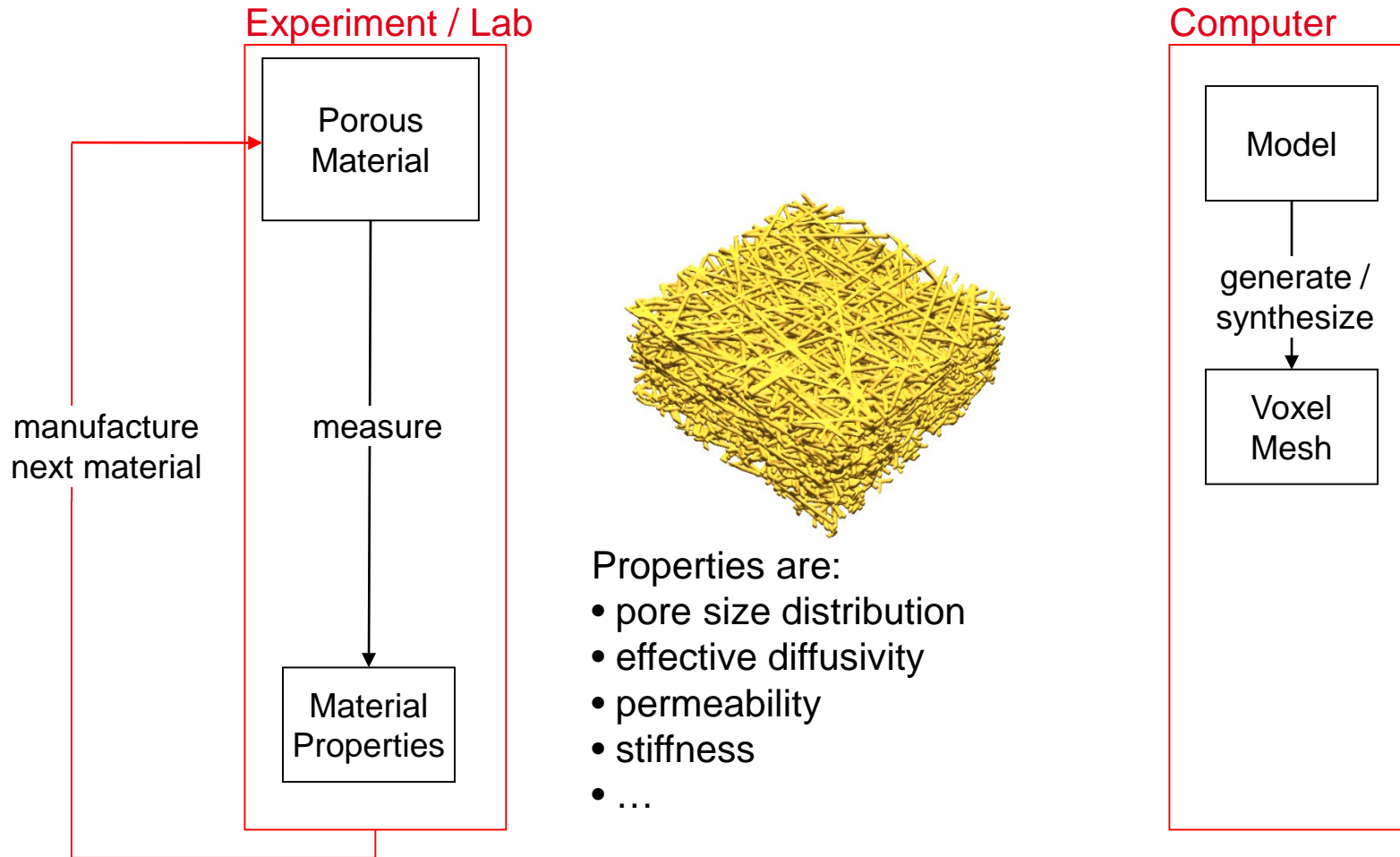
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- effective diffusivity
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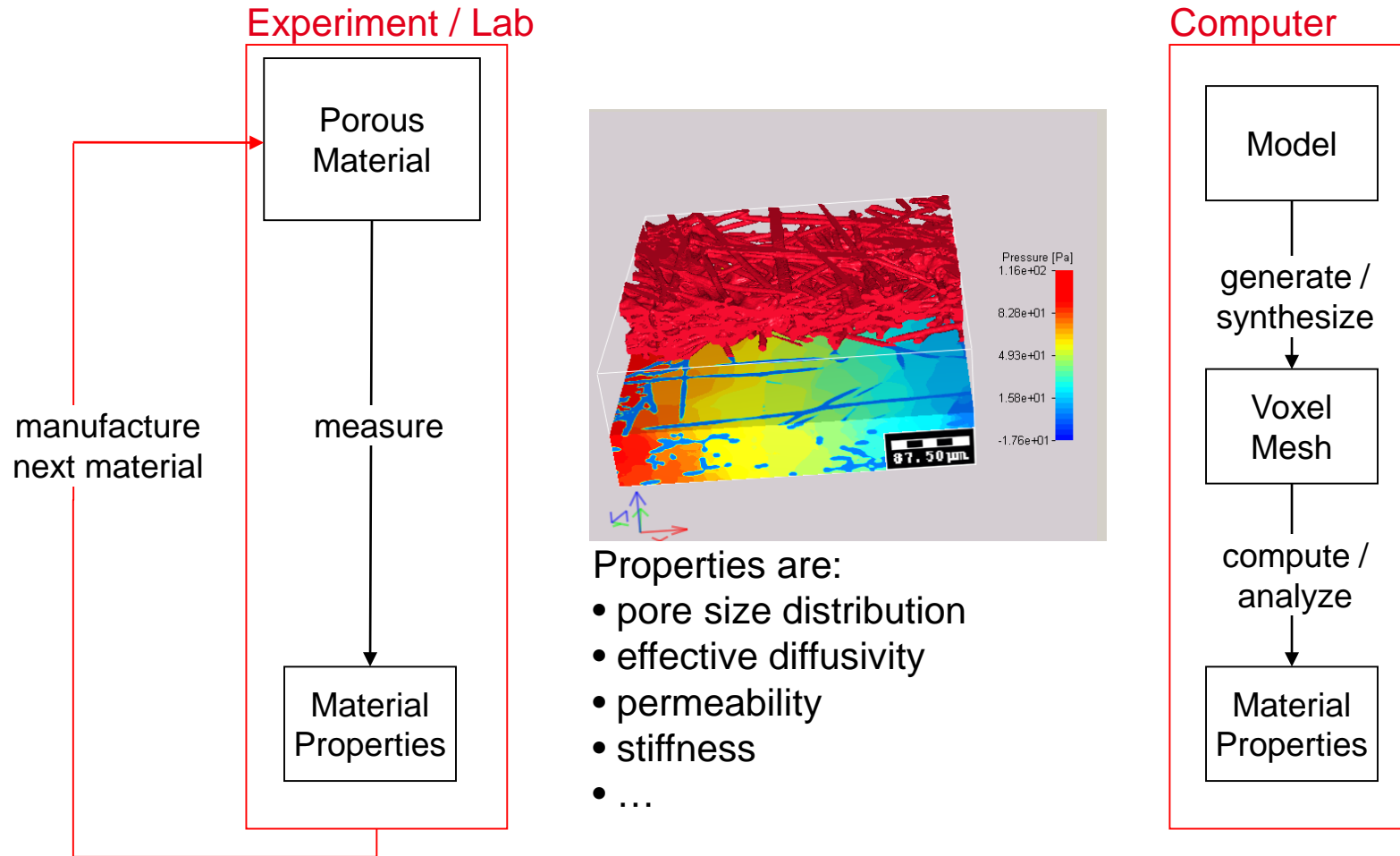
# The Virtual Material Lab Approach:



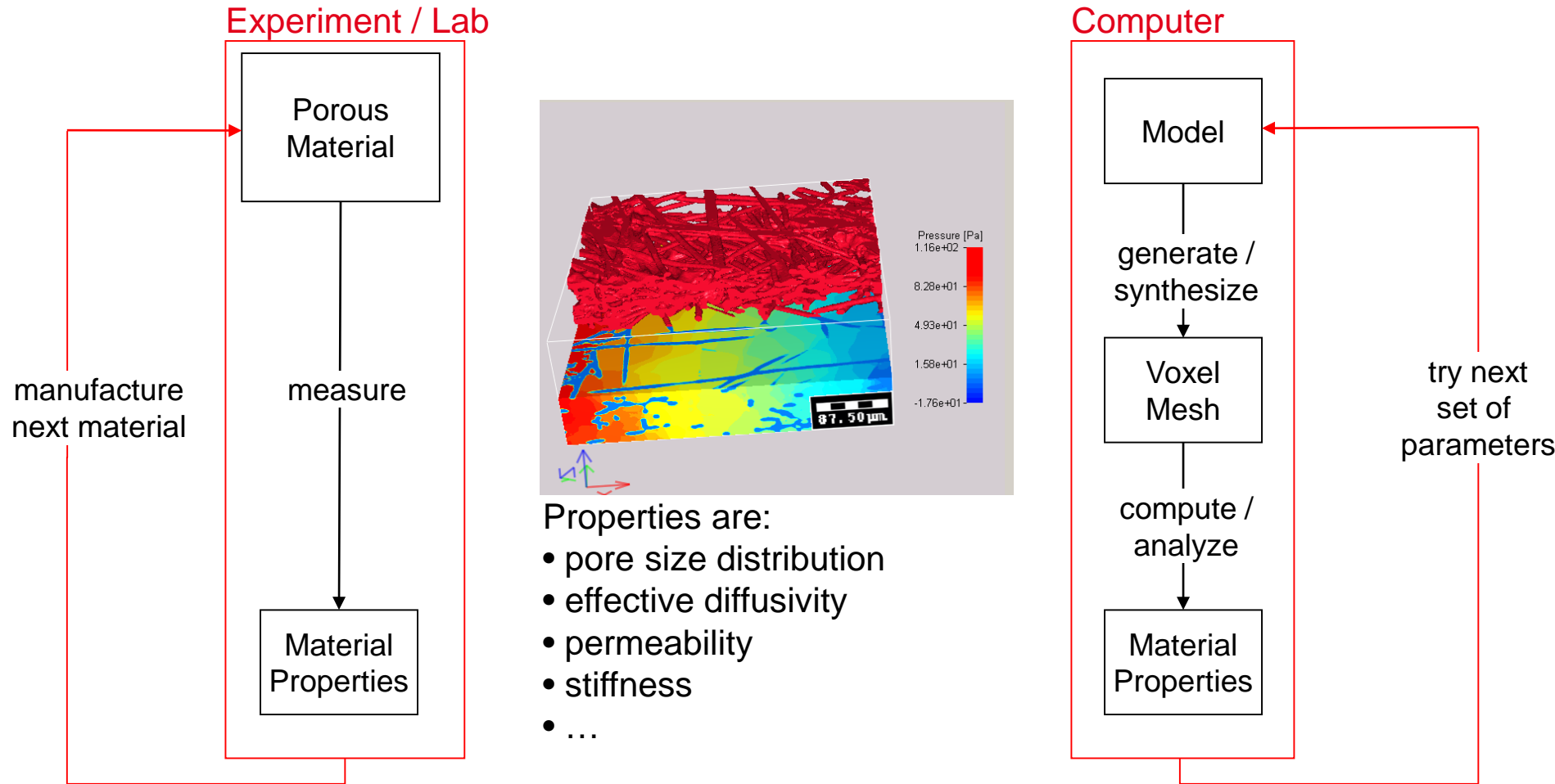
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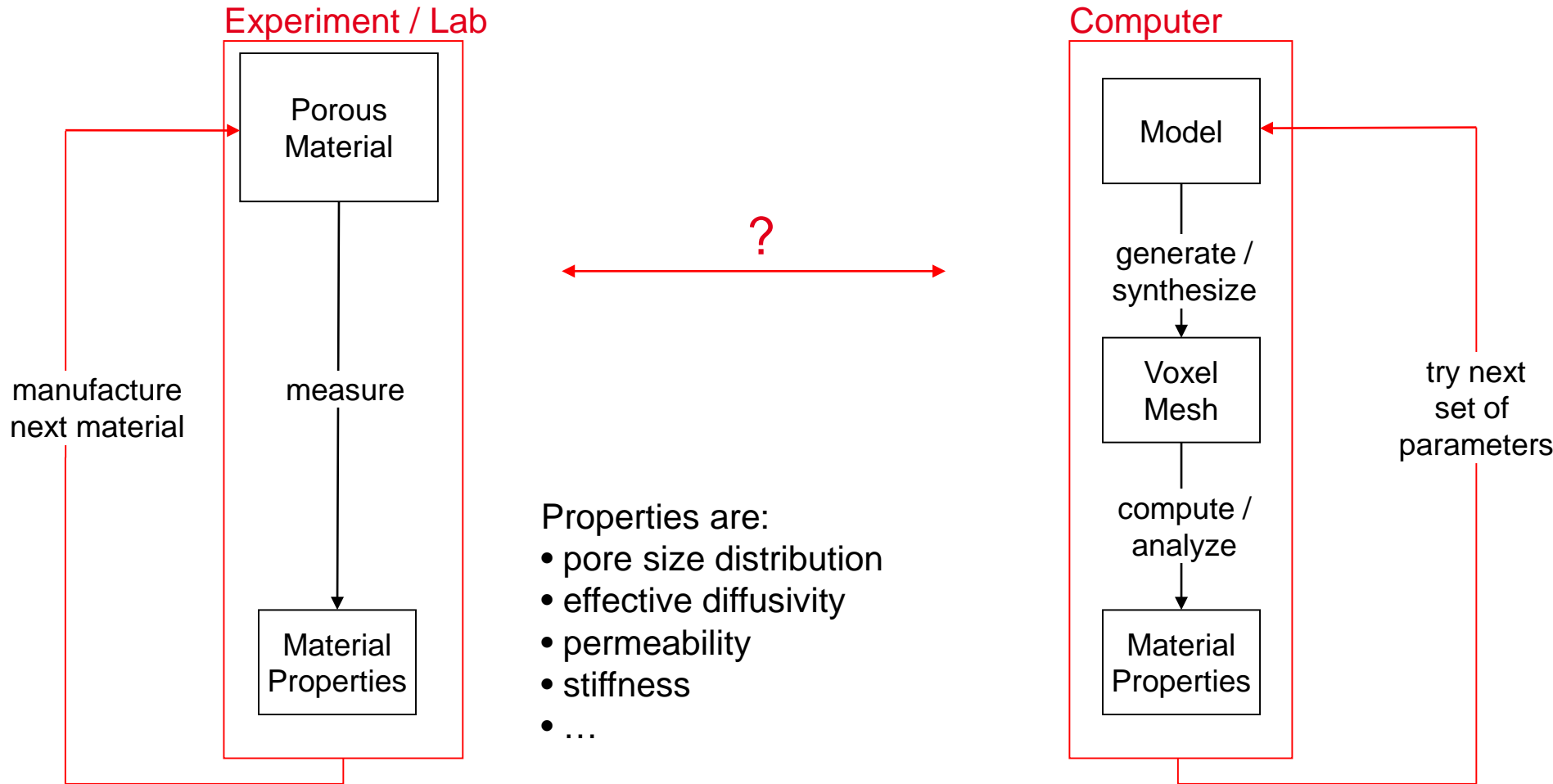
# The Virtual Material Lab Approach:



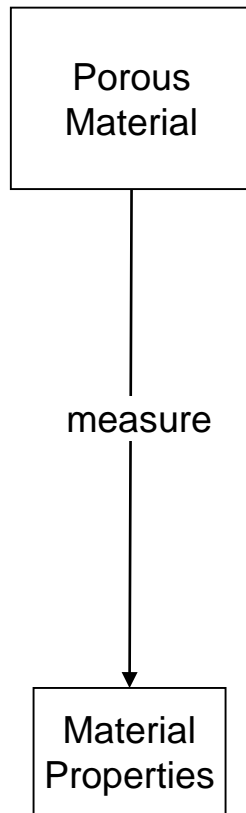
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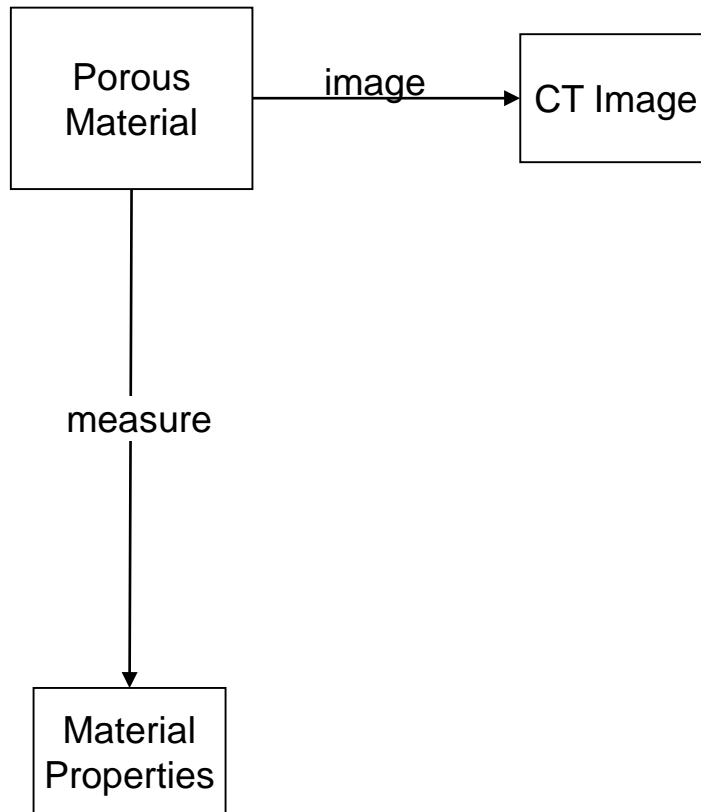
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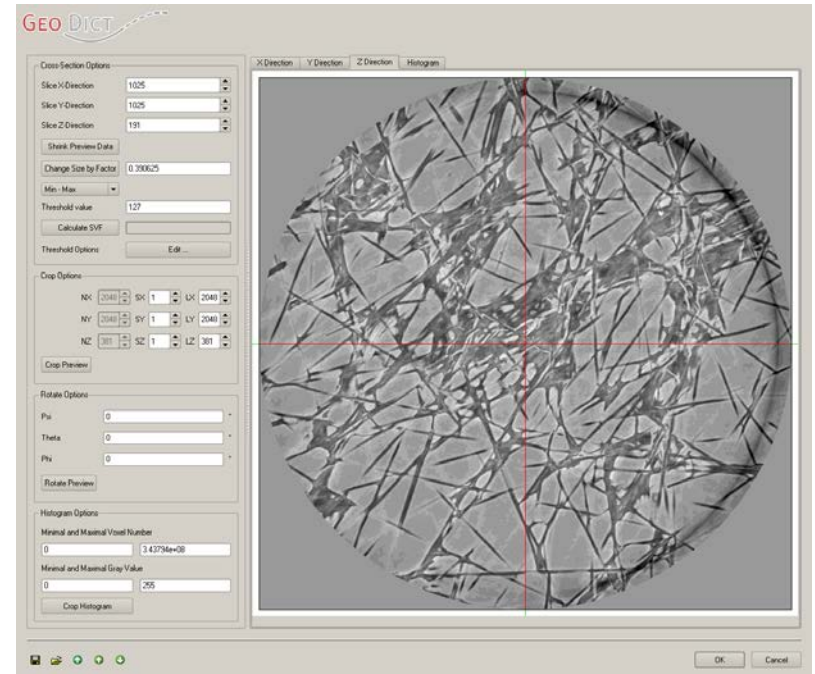
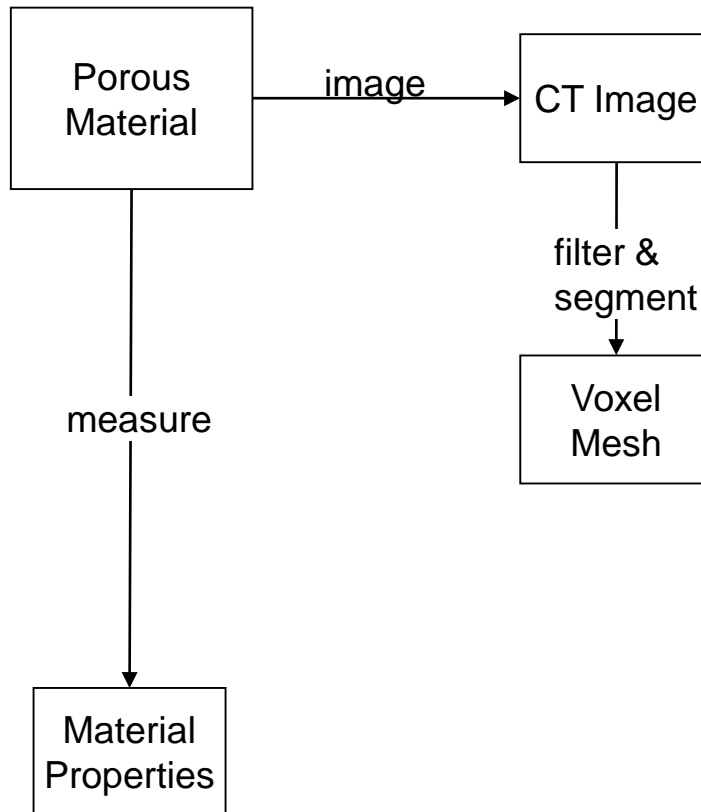
# Validation - Step 1: Analysis or Property Computations



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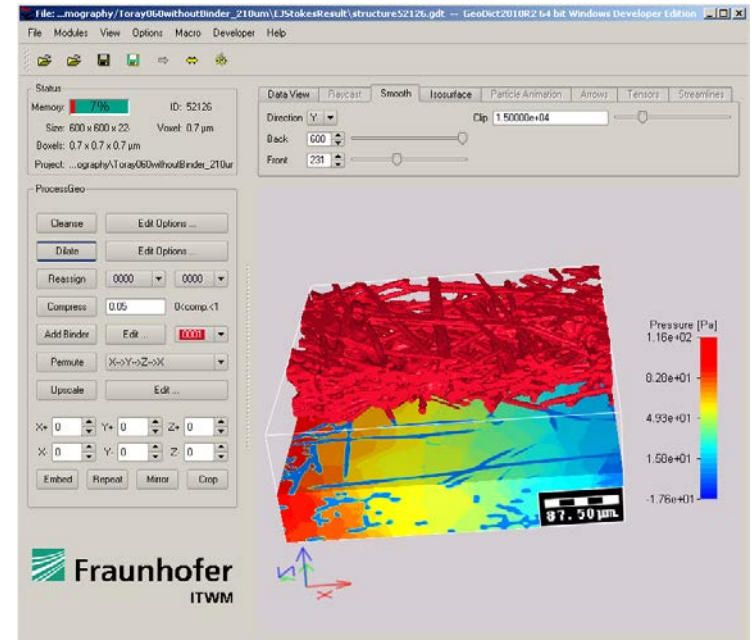
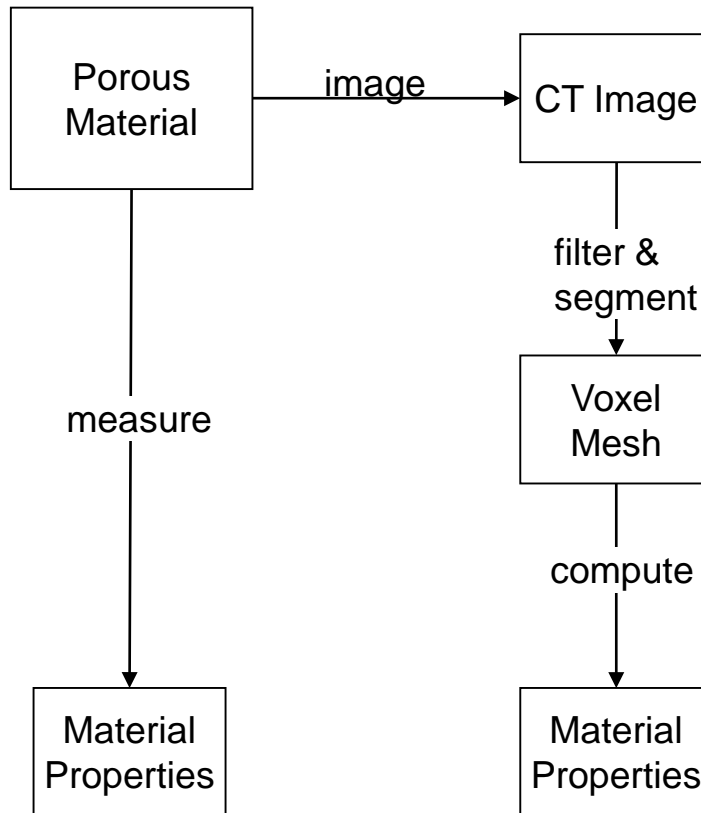


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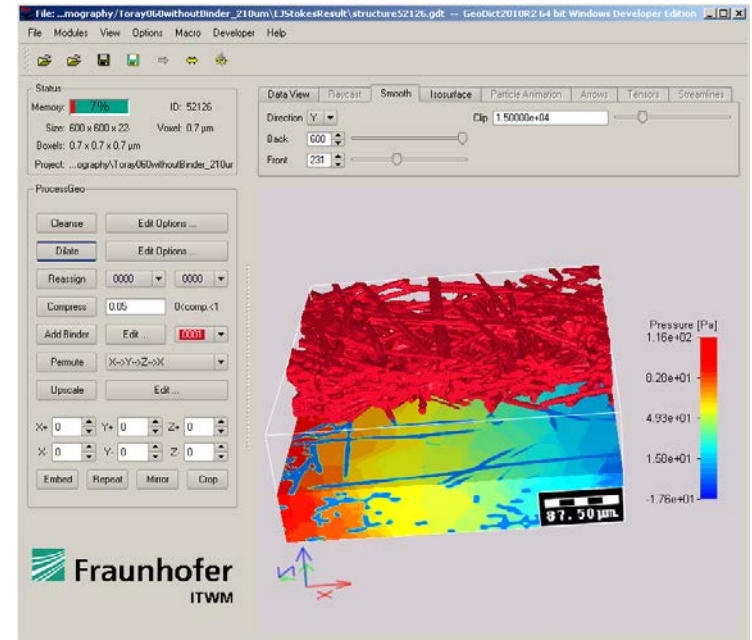
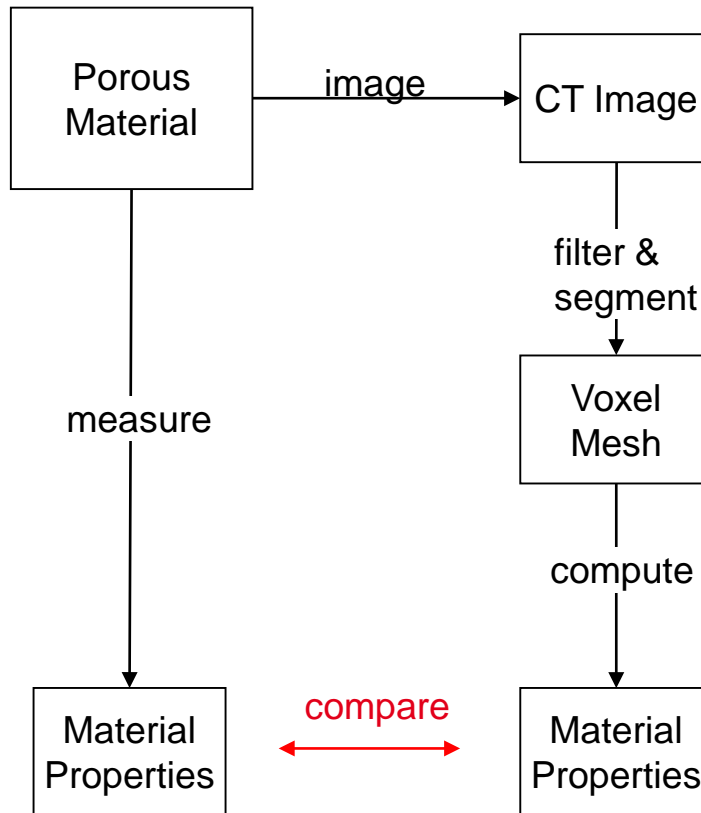




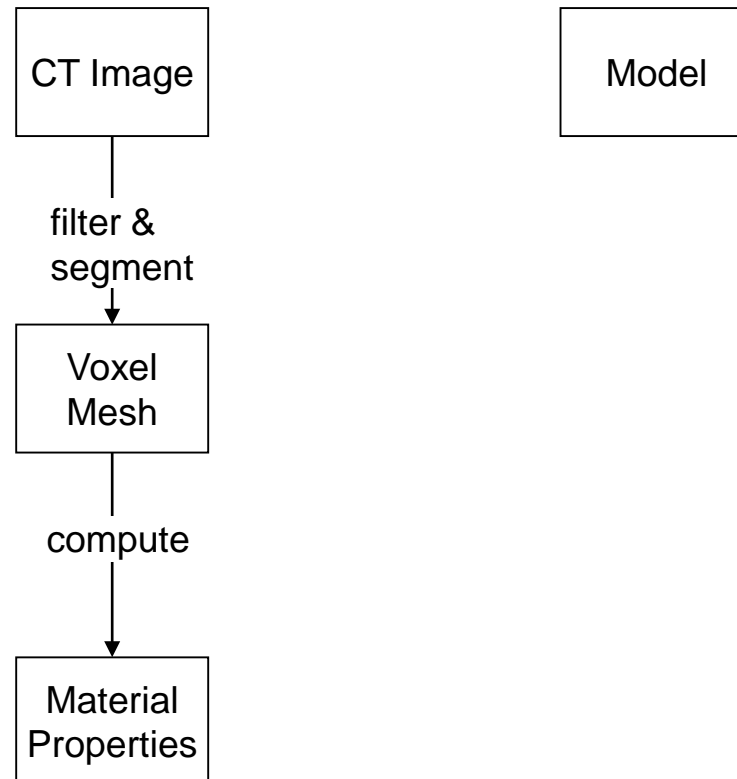
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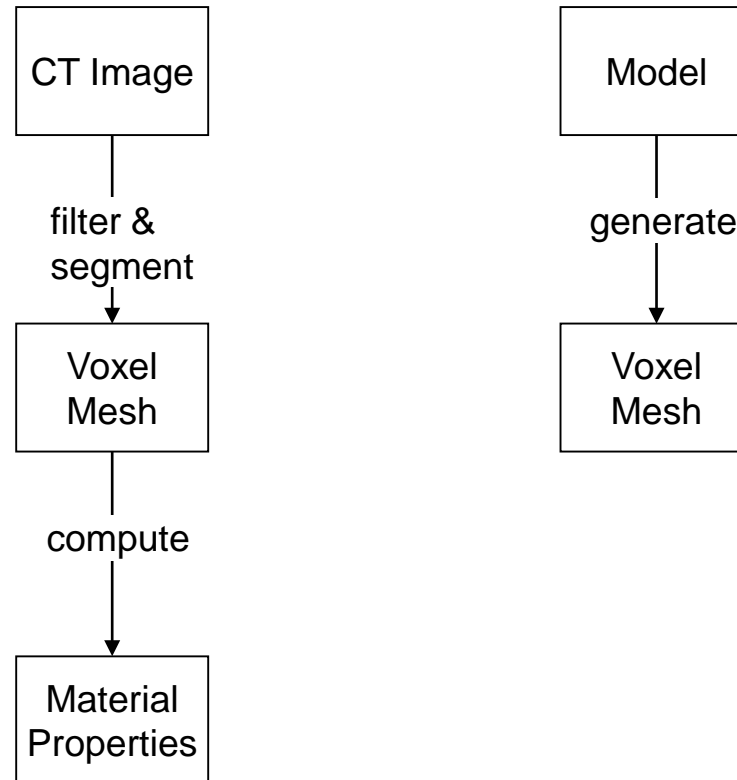
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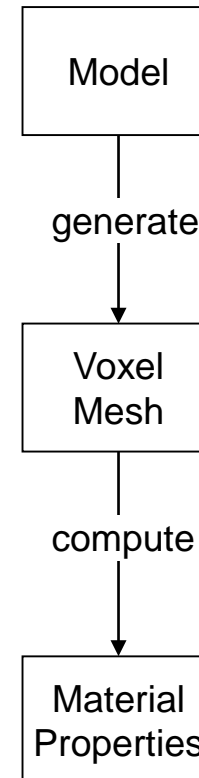
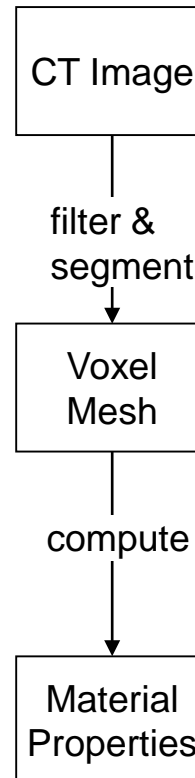
# Validation - Step 2: Synthesis or Material Models



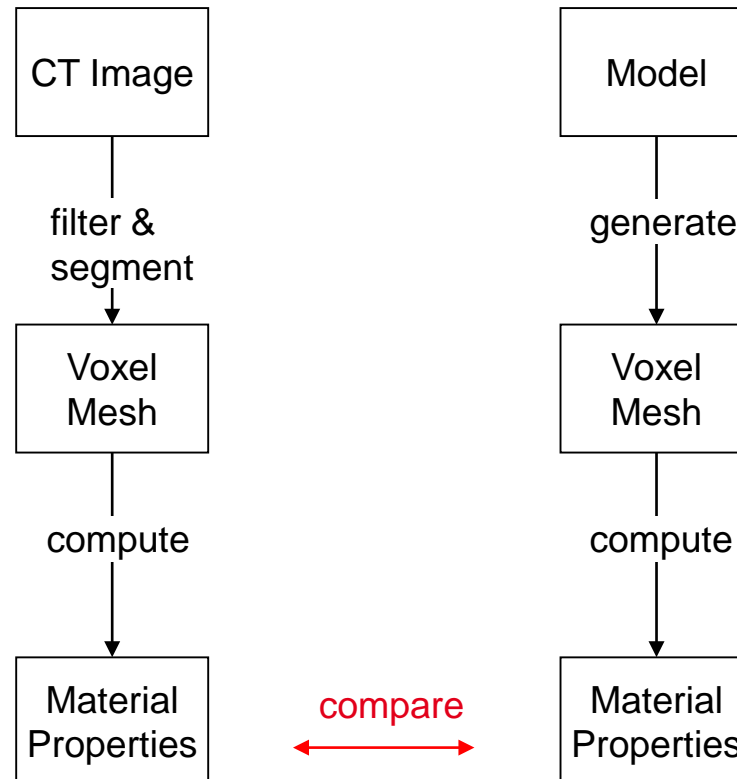
# Validation - Step 2: Synthesis or Material Models



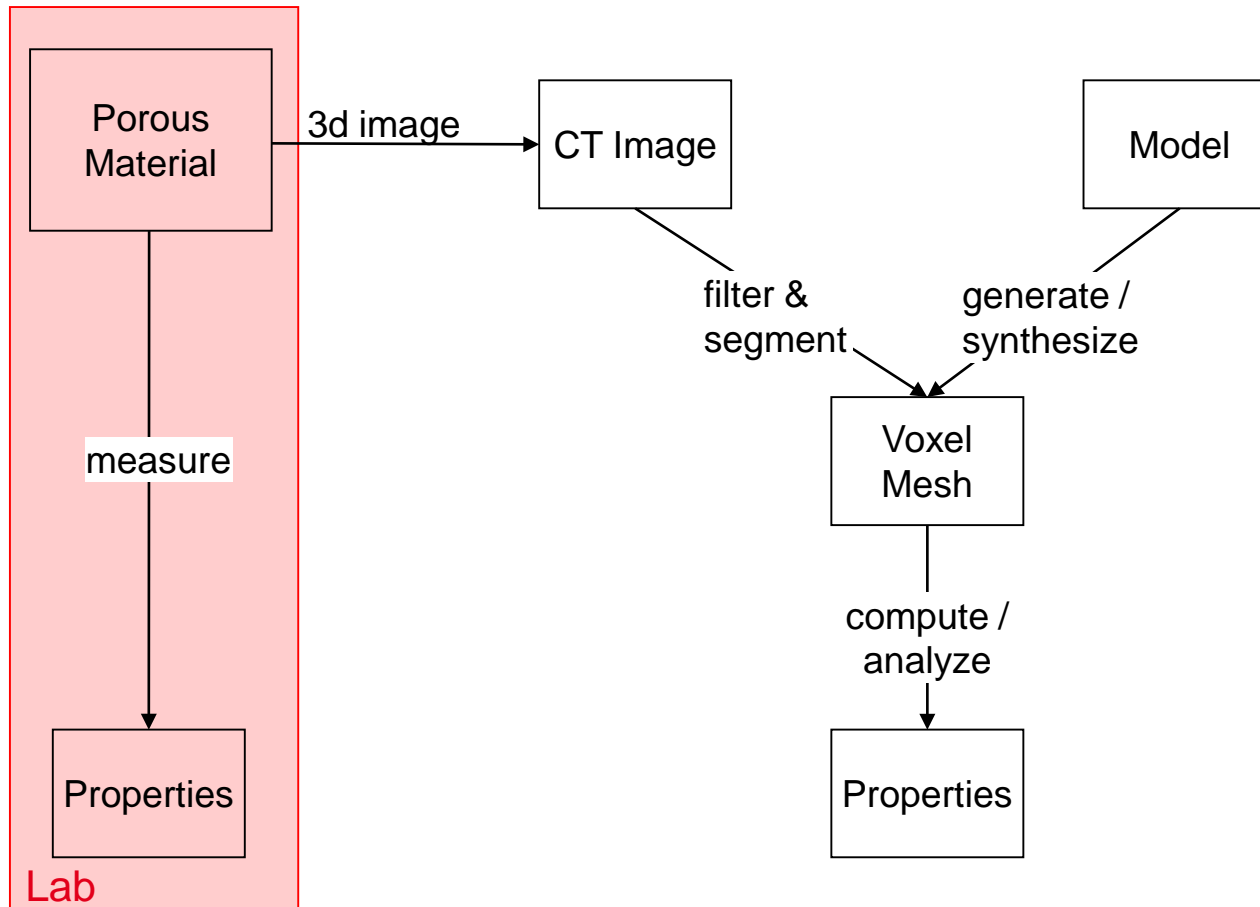
# Validation - Step 2: Synthesis or Material Models



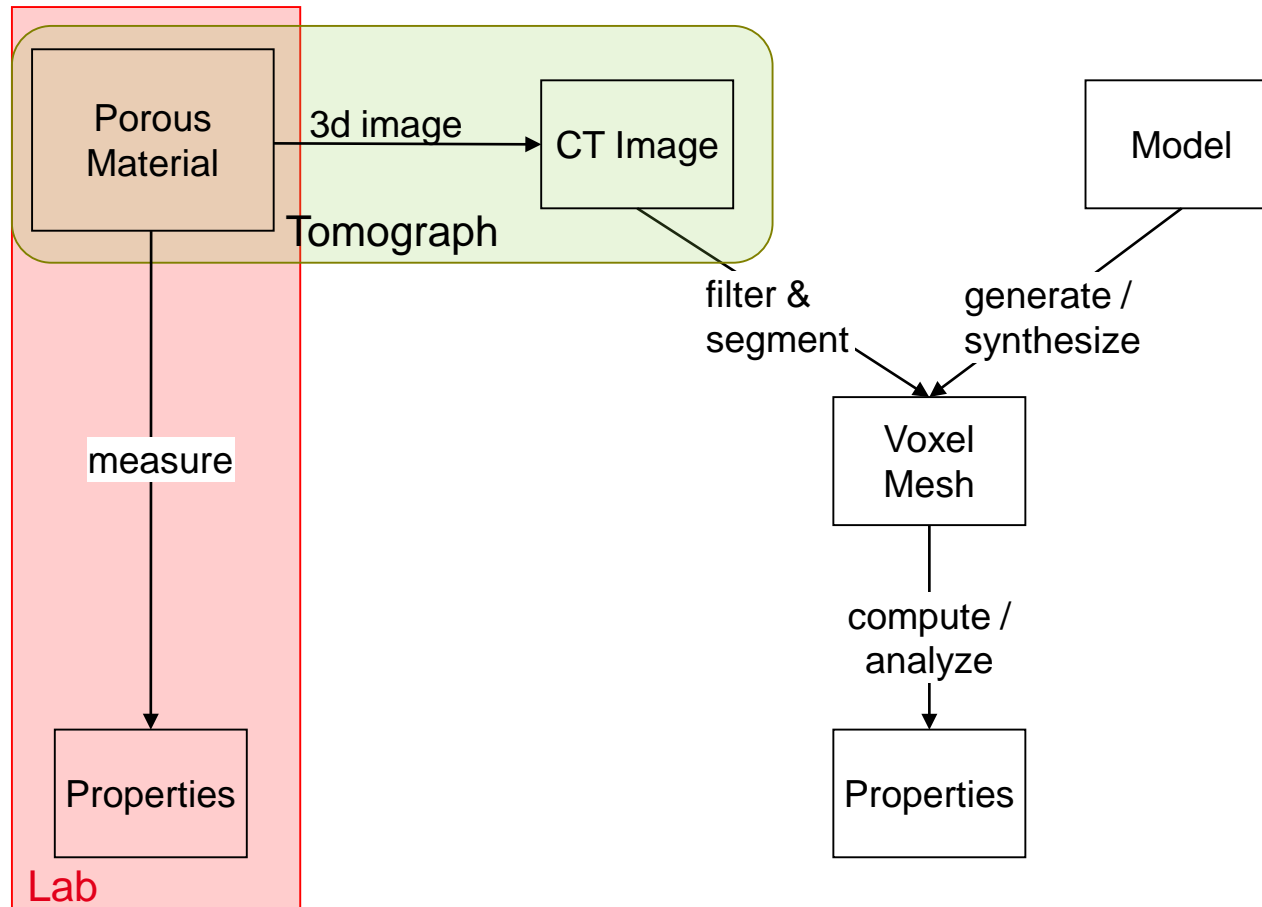
# Validation - Step 2: Synthesis or Material Models



# The Virtual Material Lab Approach:

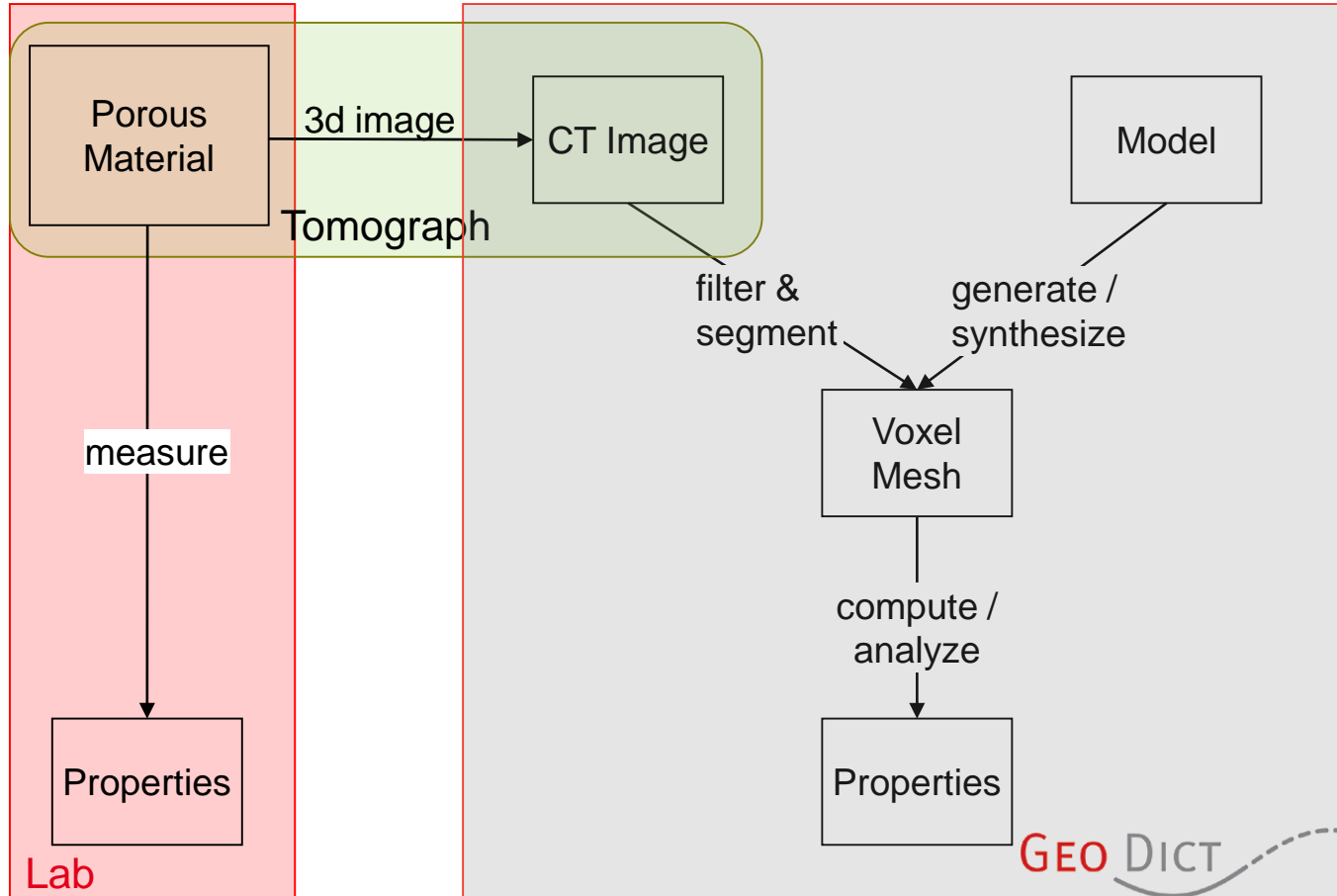


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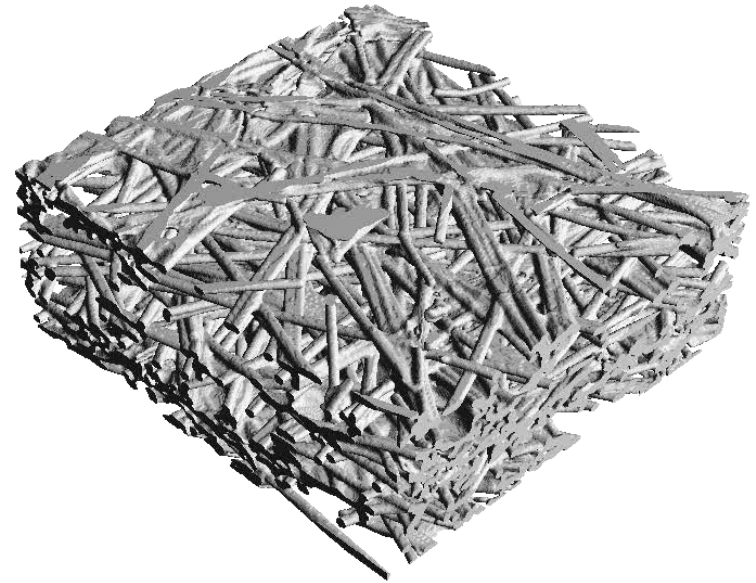
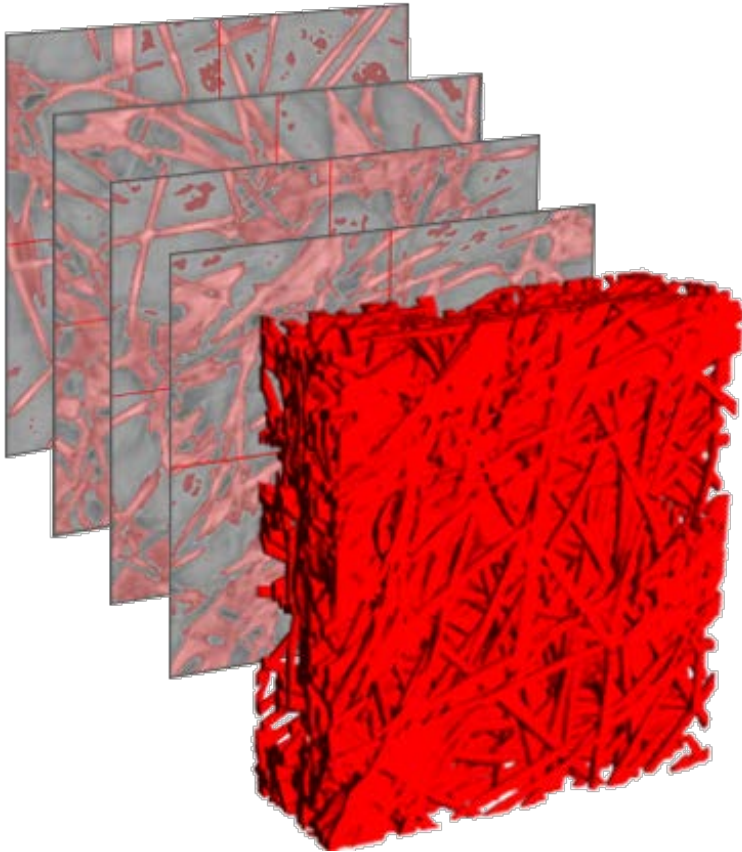


# The Virtual Material Lab Approach:



## 2. Import and Analysis of CT Images

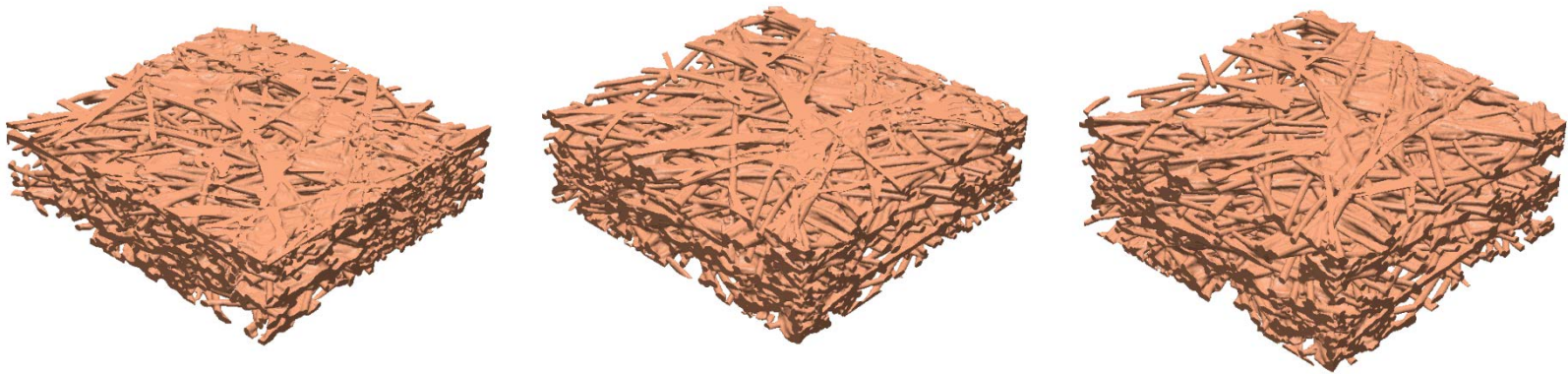
# Import of CT Data (GDL)



# Transport Properties at Different Compression Levels

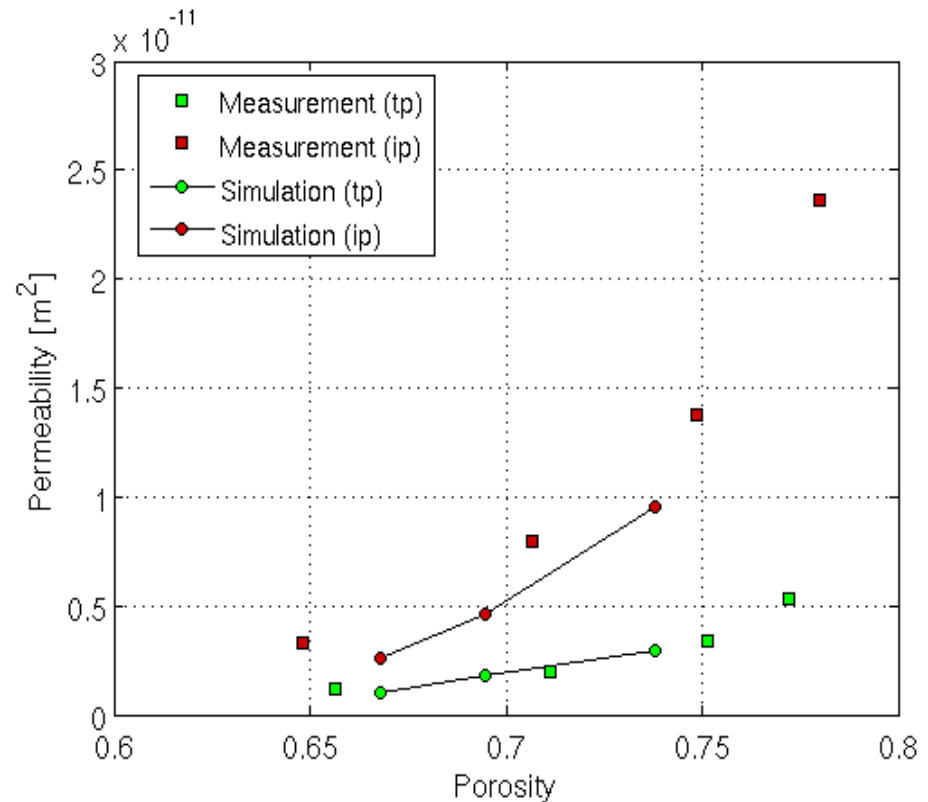
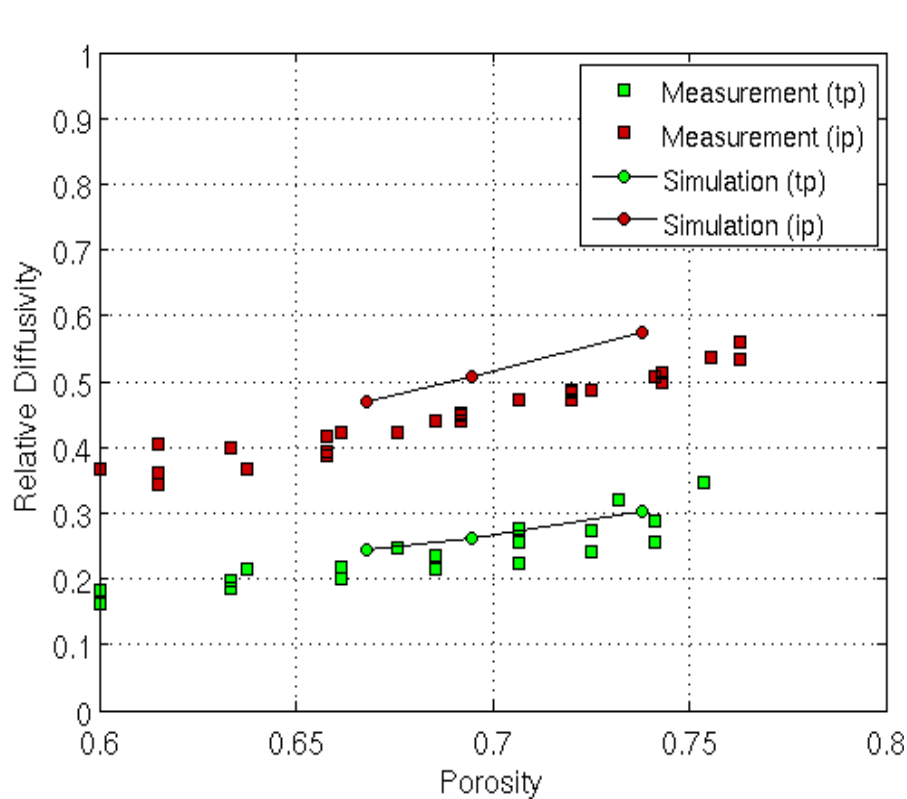
Data from Paul Scherrer Institute:

- Tomography images of Toray TGP H 060 at different compression levels
- Diffusivity, permeability and conductivity were measured at different compression levels experimentally



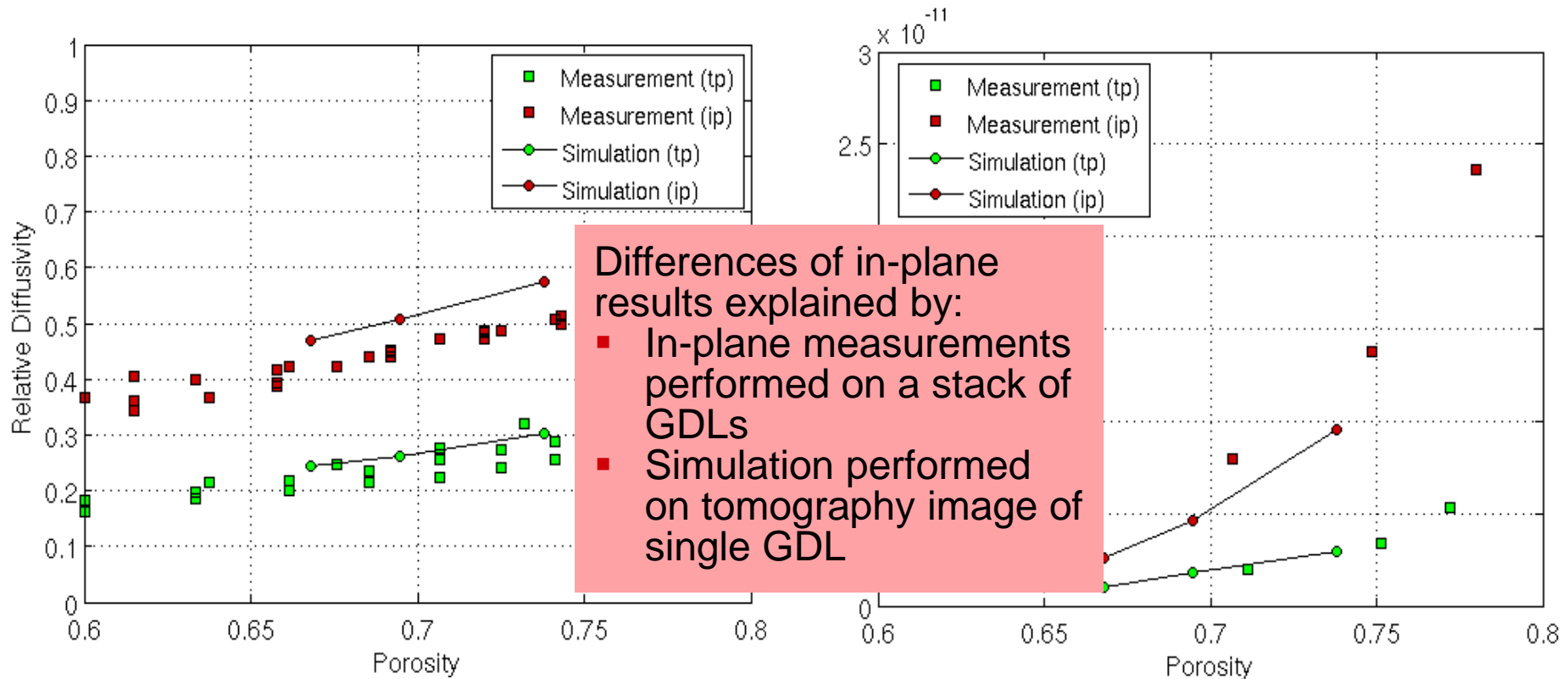
*Becker, Flückiger, Reum, Büchi, Marone, Stampanoni, 2009, J. Electrochem. Soc. 156*

# Transport Properties at Different Compression Levels



Becker, Flückiger, Reum, Büchi, Marone, Stampanoni, 2009, *J. Electrochem. Soc.* 156

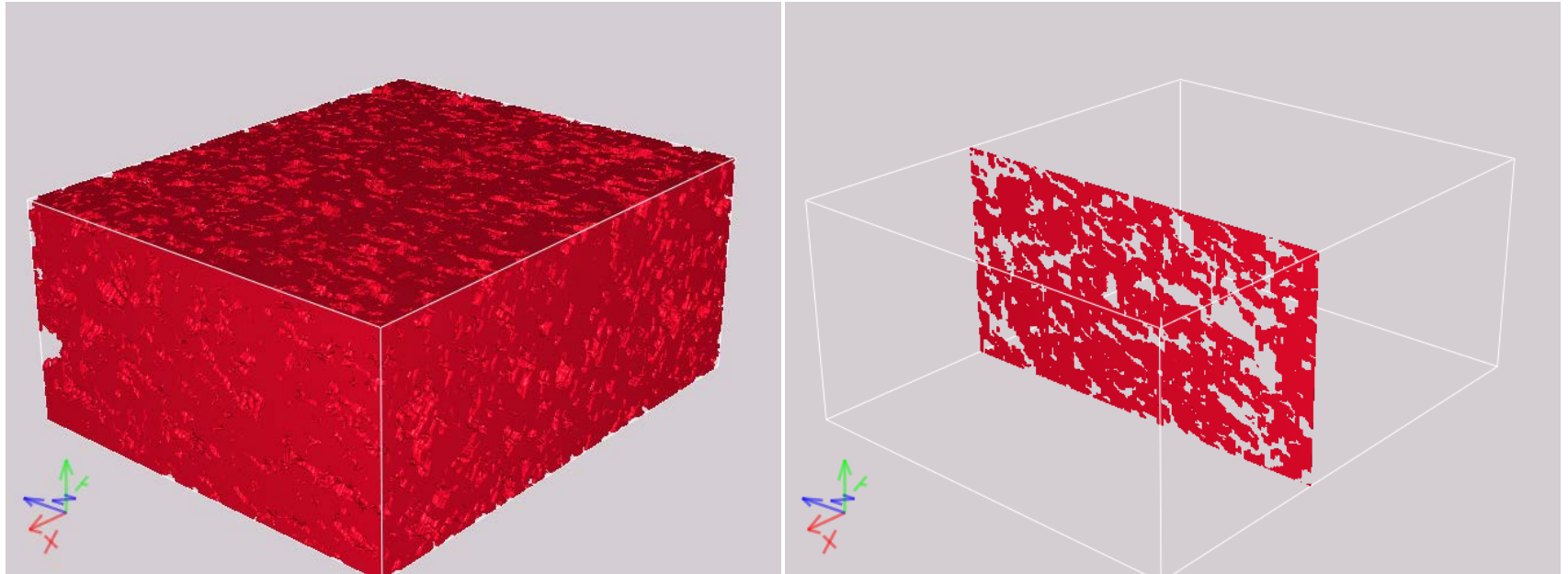
# Transport Properties at Different Compression Levels



Becker, Flückiger, Reum, Büchi, Marone, Stampanoni, 2009, *J. Electrochem. Soc.* 156

# FIBSEM Data of Catalyst Layer

- Pore Structure obtained from FIBSEM Data (IMTEK, Uni Freiburg)

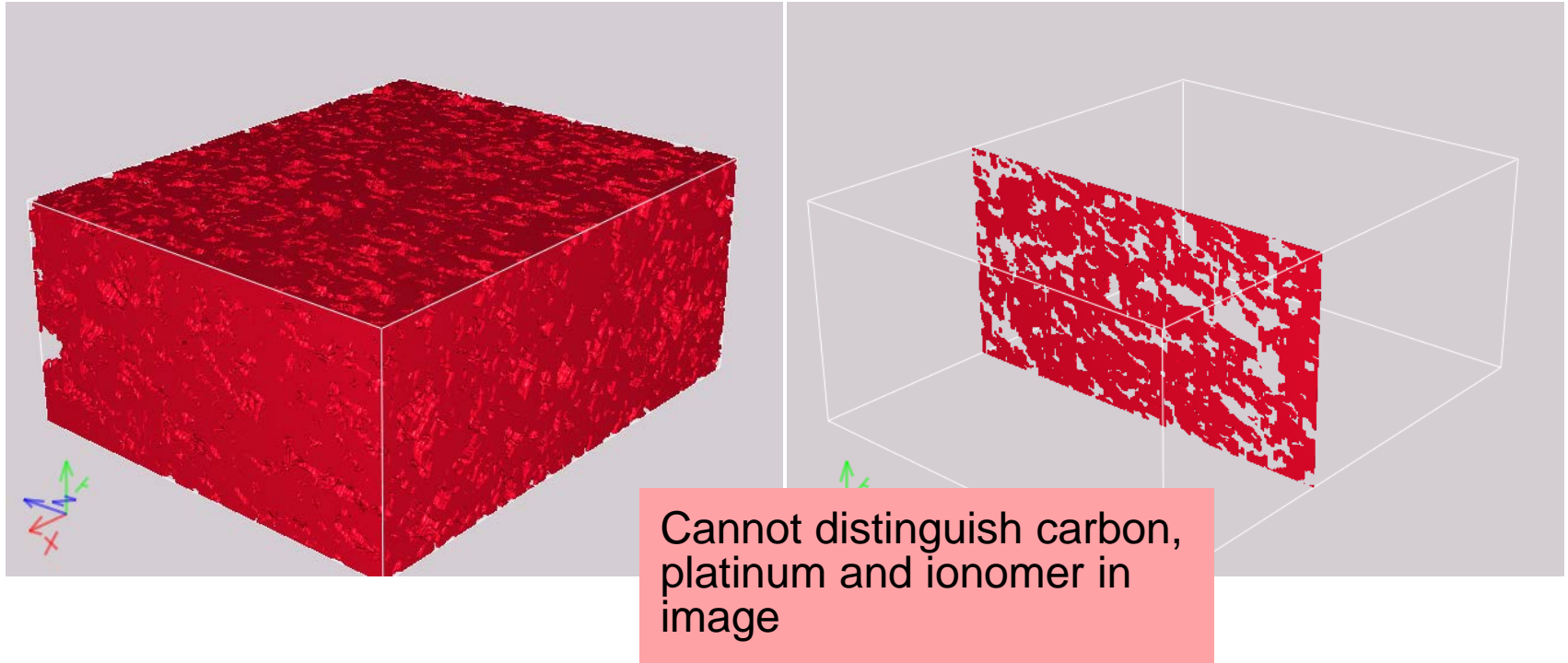


*T. Hutzenlaub, J. Becker, R. Zengerle und S. Thiele, J. Power Sources 227, pp 260-266, 2013.*



# FIBSEM Data of Catalyst Layer

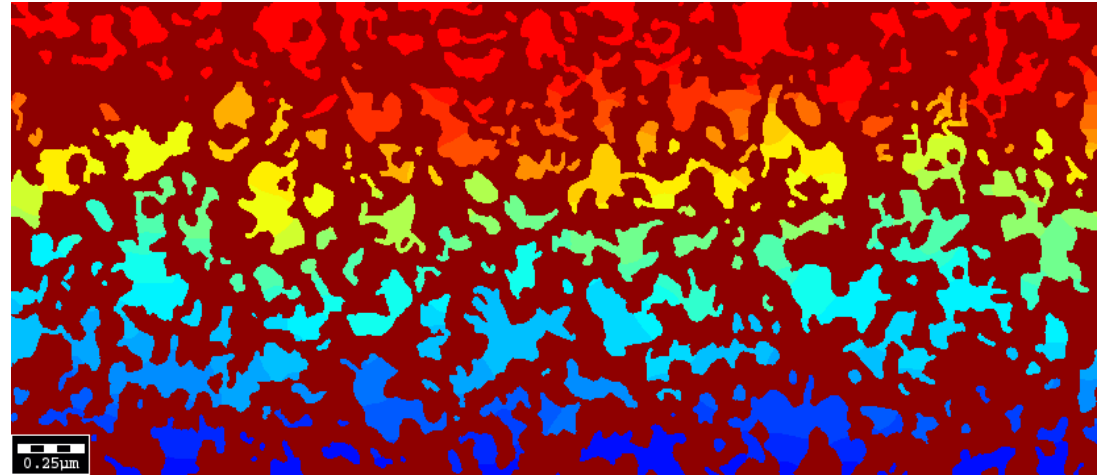
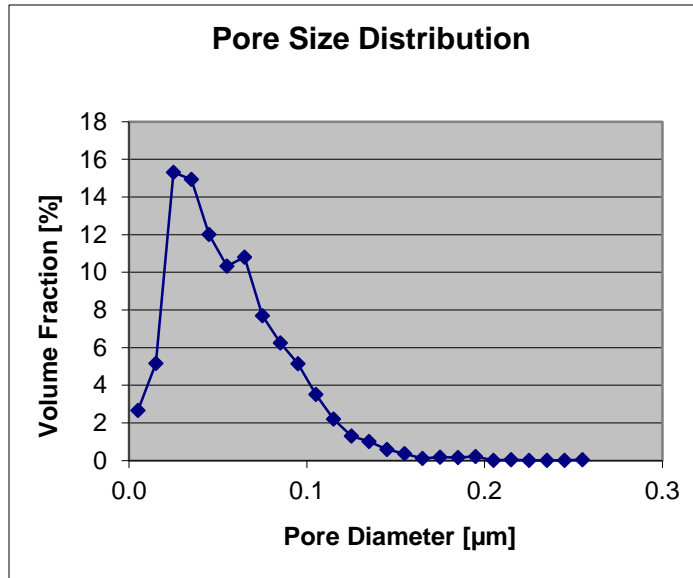
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*T. Hutzenlaub, J. Becker, R. Zengerle und S. Thiele, J. Power Sources 227, pp 260-266, 2013.*



# FIBSEM Data of Catalyst Layer



Concentration field from diffusion simulations

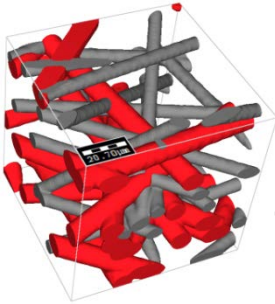
Determine:

- Pore size distribution, diffusivity

*T. Hutzenlaub, J. Becker, R. Zengerle und S. Thiele, J. Power Sources 227, pp 260-266, 2013.*

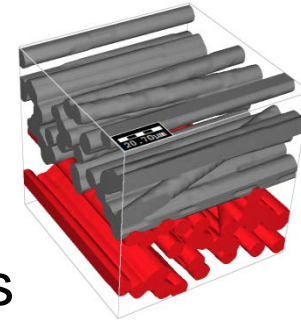
# 3. Structure Generation

# GeoDict Material Models



nonwovens

fiber reinforced composites



papers

ceramic materials

rocks

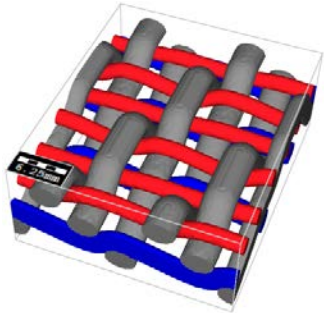
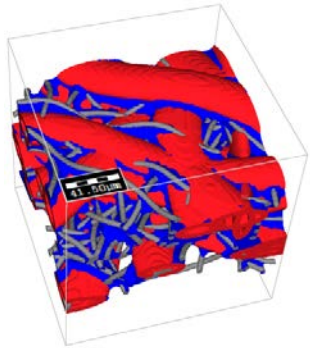
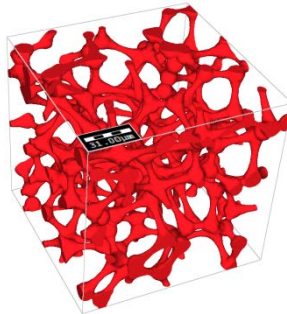
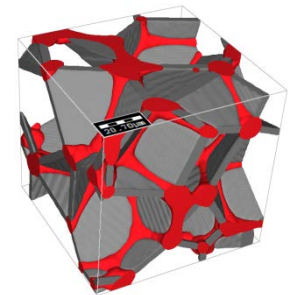
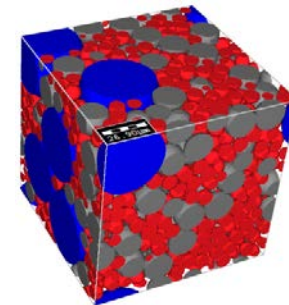
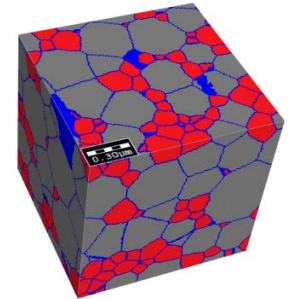
dense (sphere) packing

woven materials

foams

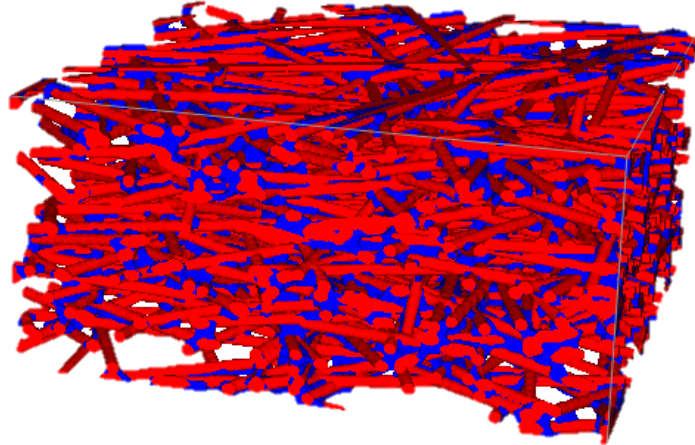
sponges

regular materials

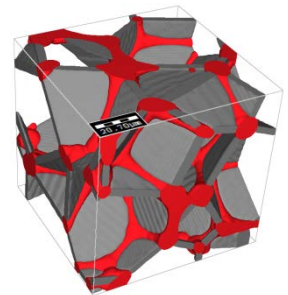
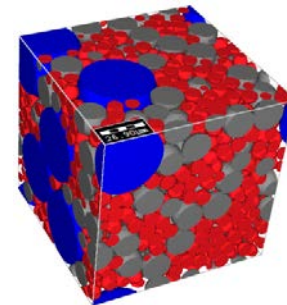
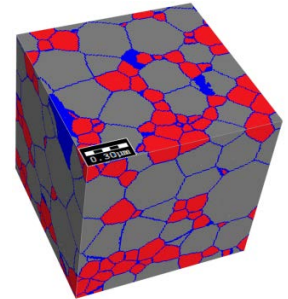
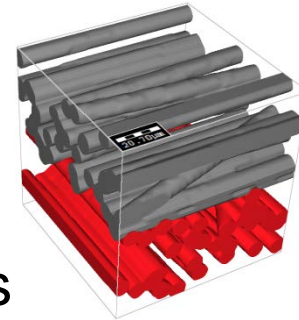


# GeoDict Material Models

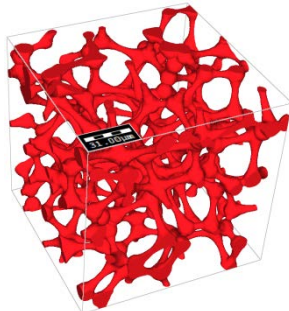
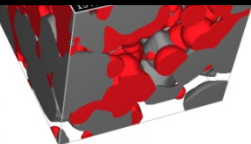
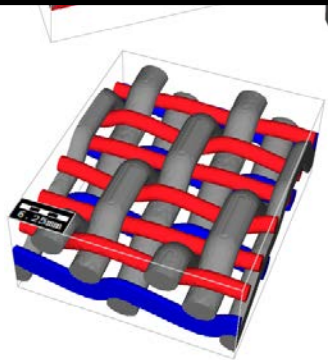
Gas Diffusion Layer



wovens  
ed composites  
pers  
materials  
cks



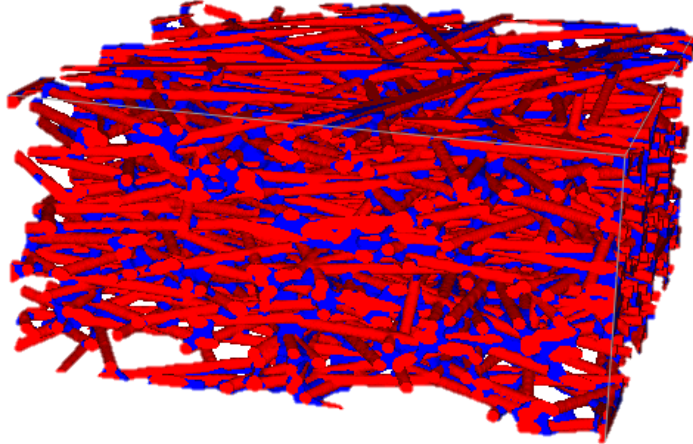
dense (sphere) packing  
woven materials  
foams  
sponges  
regular materials



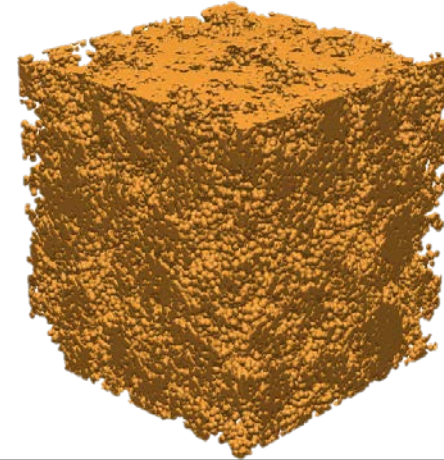


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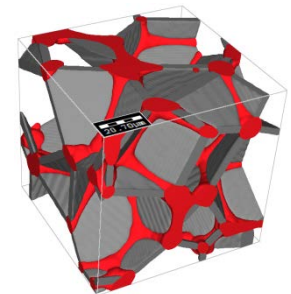
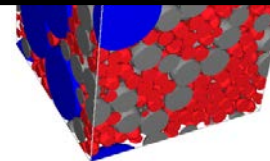
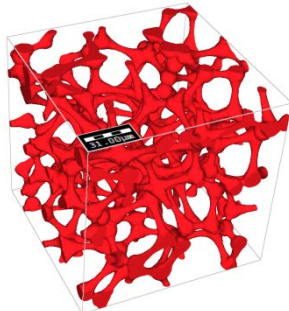
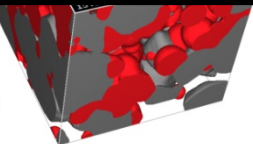
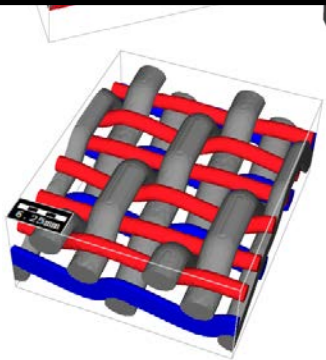
Gas Diffusion Layer



Microporous Layer

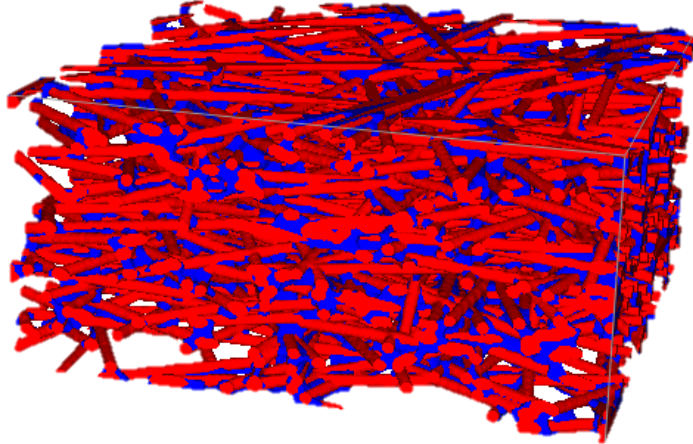


dense (sphere) packing  
woven materials  
foams  
sponges  
regular materials

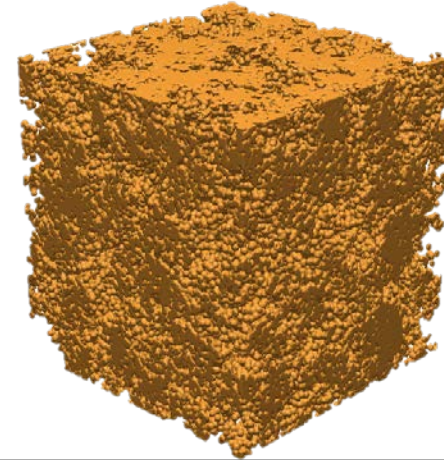


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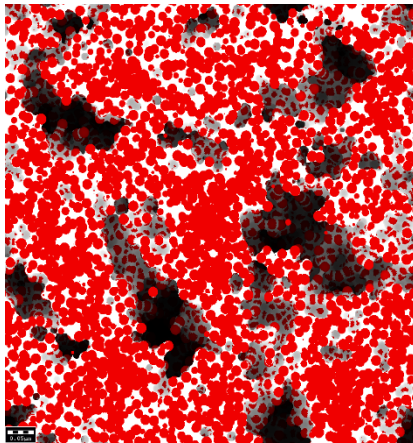
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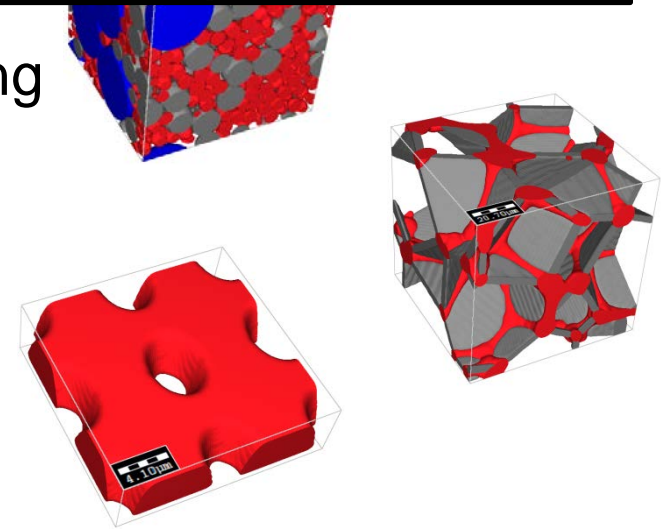
Microporous Layer



Catalyst Layer

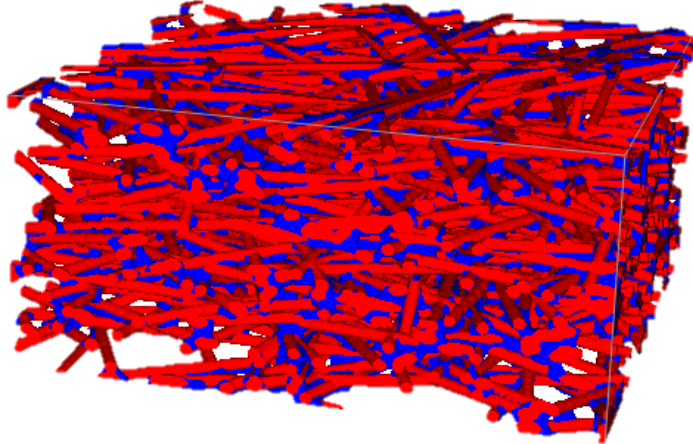


ere) packing  
materials  
ms  
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materials

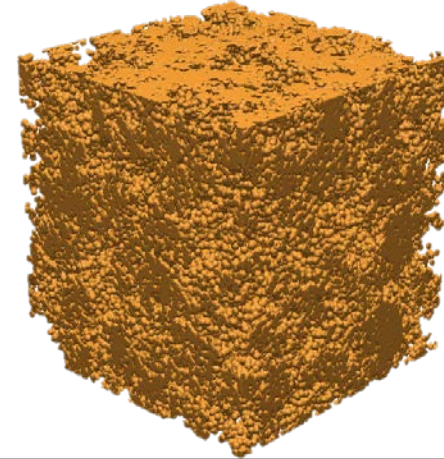


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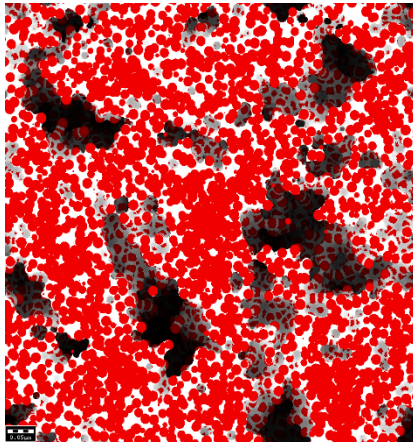
Gas Diffusion Layer



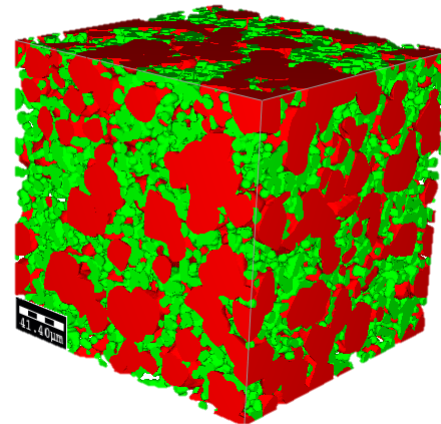
Microporous Layer



Catalyst Layer



LiO Battery Electrode





# Gas Diffusion Layer Model

Created with a stochastic process

Input:

- Porosity
- Thickness
- Fiber diameter and length
- Fiber cross sectional shape
- Fiber orientation tensor





# Gas Diffusion Layer Model

Created with a stochastic process

Input:

- Porosity
- Thickness
- Fiber diameter and length
- Fiber cross sectional shape
- Fiber orientation tensor
- (Fiber crimp)

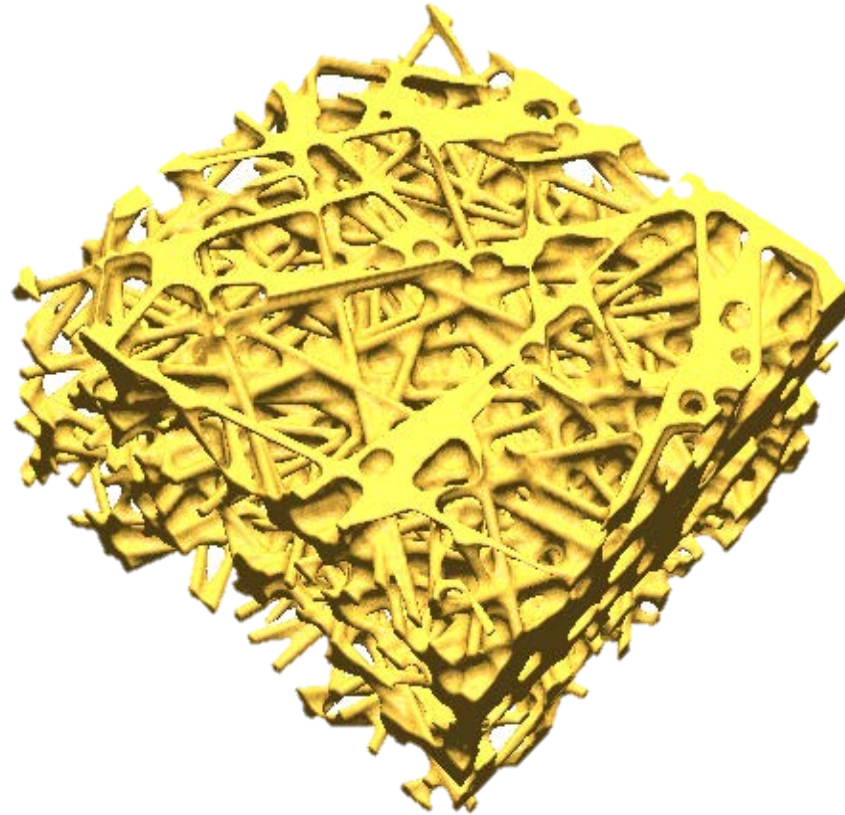


# Gas Diffusion Layer Model

Created with a stochastic process

Input:

- Porosity
- Thickness
- Fiber diameter and length
- Fiber cross sectional shape
- Fiber orientation tensor
- (Fiber crimp)
- (Weight% binder)



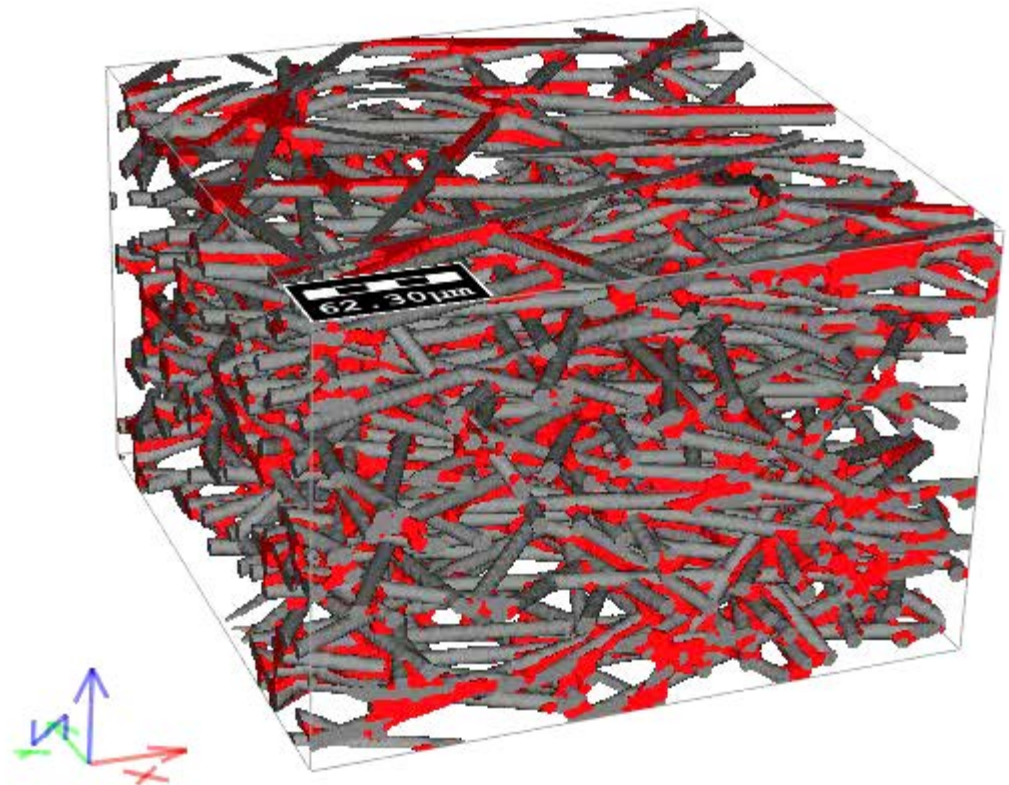
# Compression of a GDL

Clamping pressure applied to GDL



- Transverse isotropic elastic modulus for fibers
- Isotropic elastic modulus for binder
- 30% compression

10 min on Laptop  
13.5 mio grid points



# 4. Determination of Transport Properties

# Permeability

**Macroscopic description  
(homogenized porous media model)**

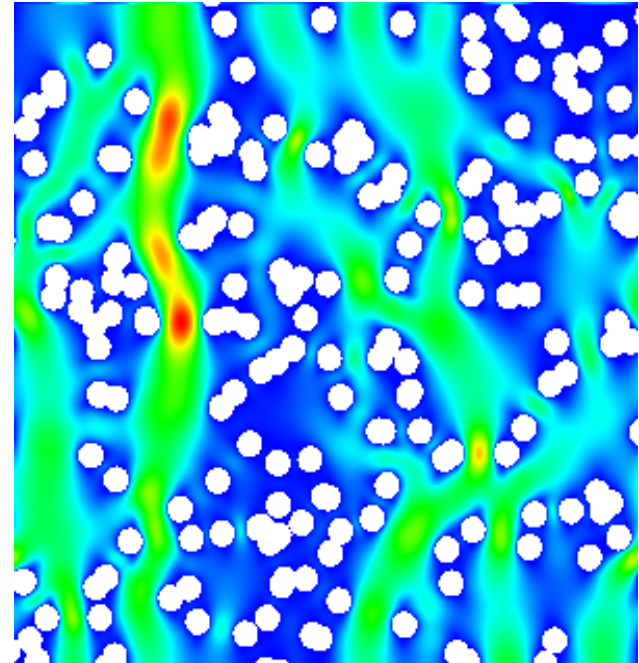
$$\text{Darcy's law : } u = -\frac{1}{\mu} \kappa \nabla p$$

$u$  : average flow velocity

$\kappa$  : permeability tensor **unknown**

$\mu$  : viscosity

$p$  : pressure



# Permeability

## Macroscopic description (homogenized porous media model)

$$\text{Darcy's law : } u = -\frac{1}{\mu} \kappa \nabla p$$

$u$  : average flow velocity

$\kappa$  : permeability tensor **unknown**

$\mu$  : viscosity

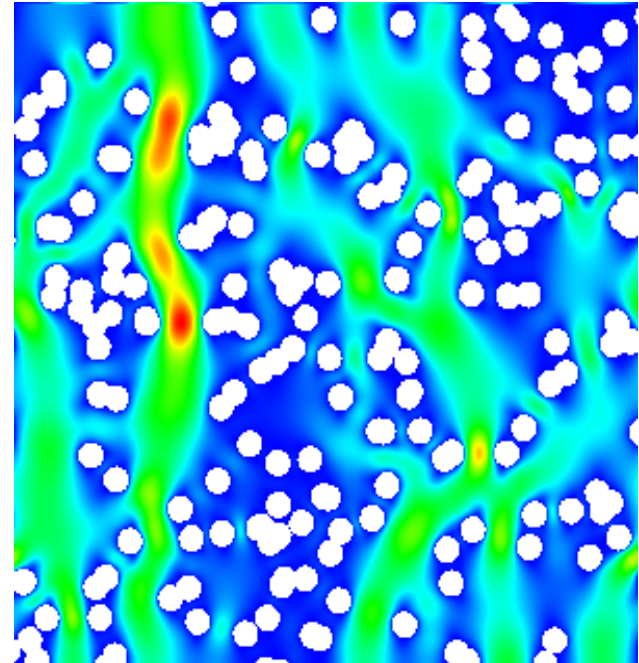
$p$  : pressure

## Microscopic description (pore structure model)

$$\text{Stokes equation: } -\mu \Delta u + \nabla p = 0$$

Boundary conditions: no-slip on fibre surface, pressure drop

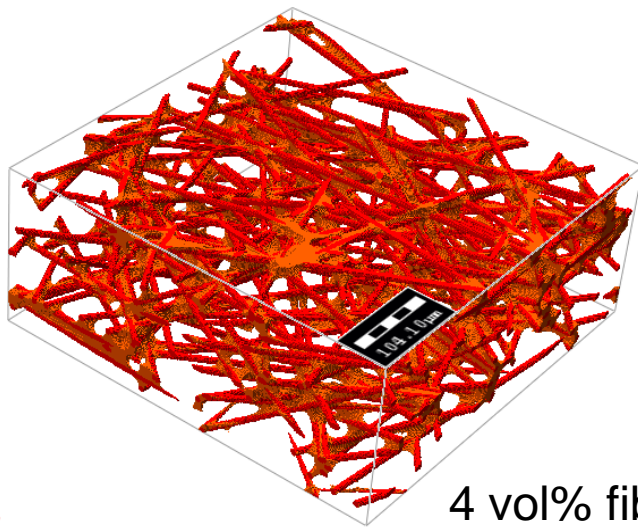
$\kappa$  can be determined from the solution!



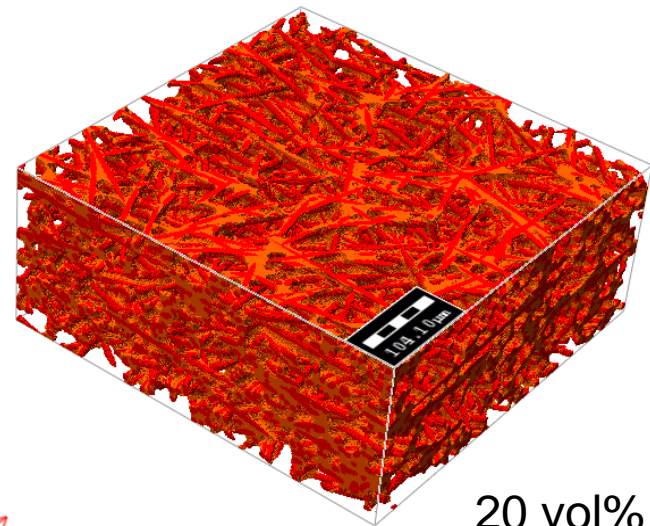


# Design Study: Effect of GDL Porosity

- 7  $\mu\text{m}$  fiber diameter
- 40 wt% binder content

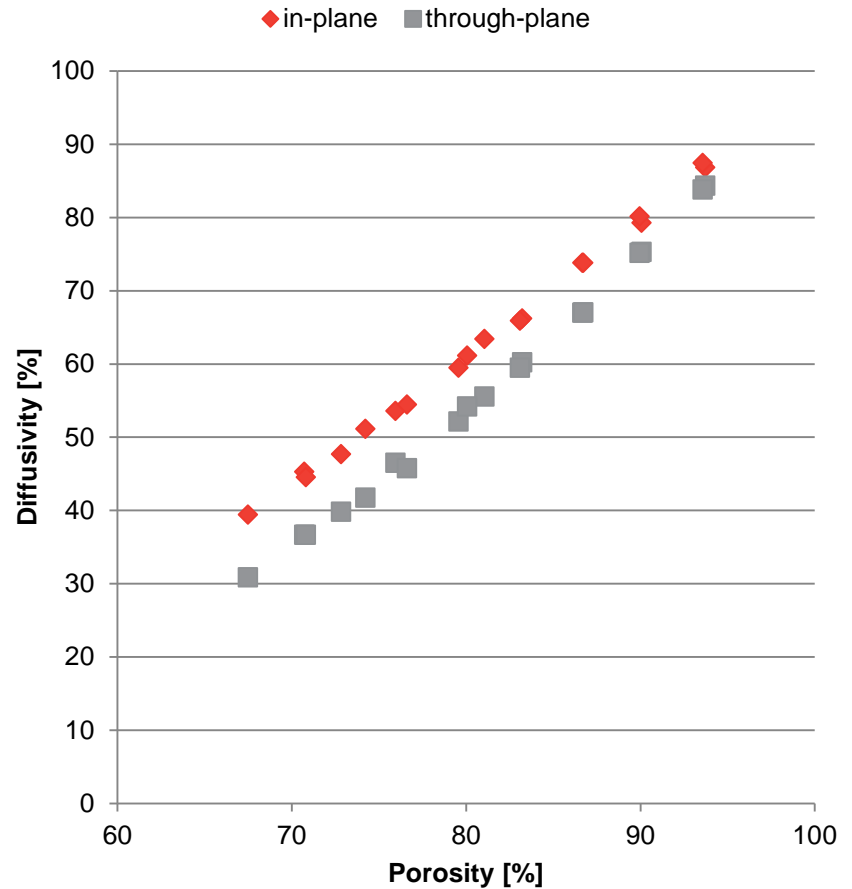
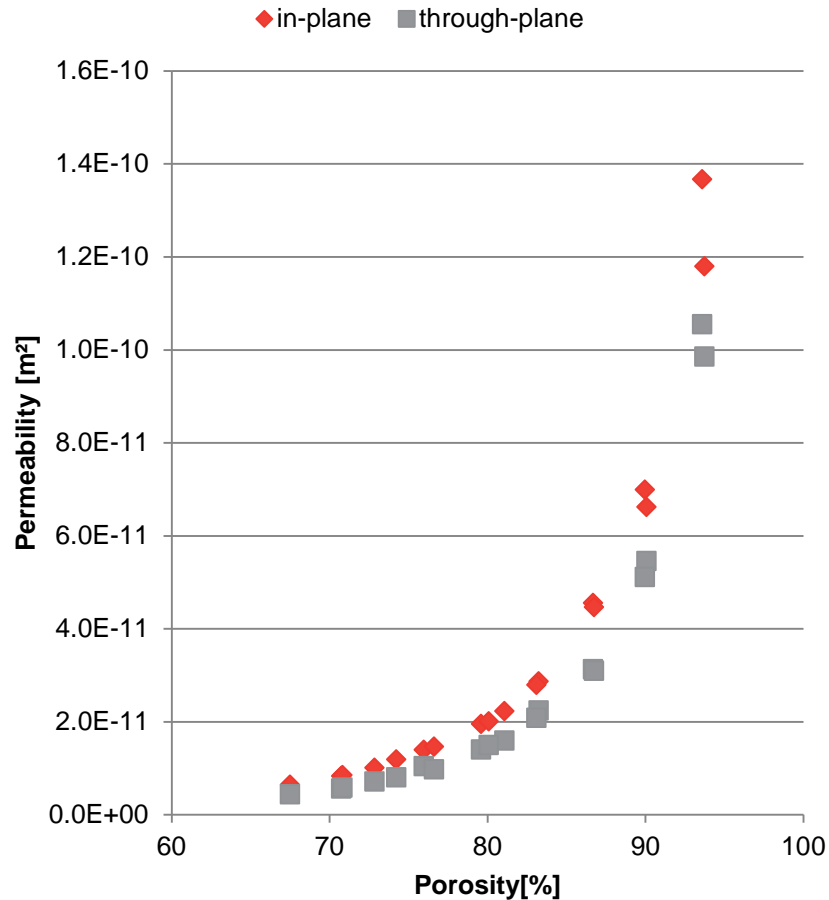


4 vol% fibers



20 vol% fibers

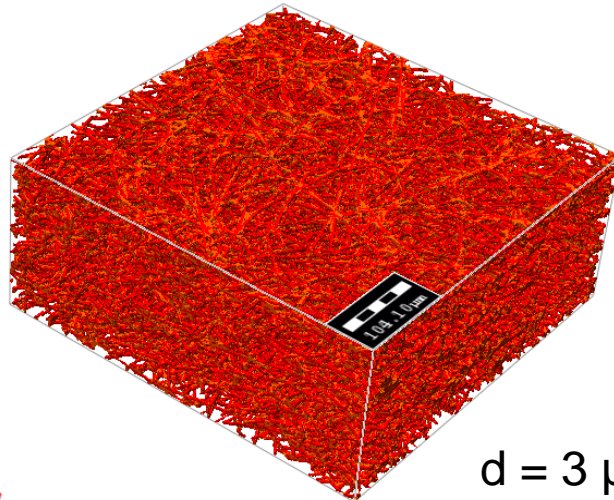
# Permeability and Diffusivity



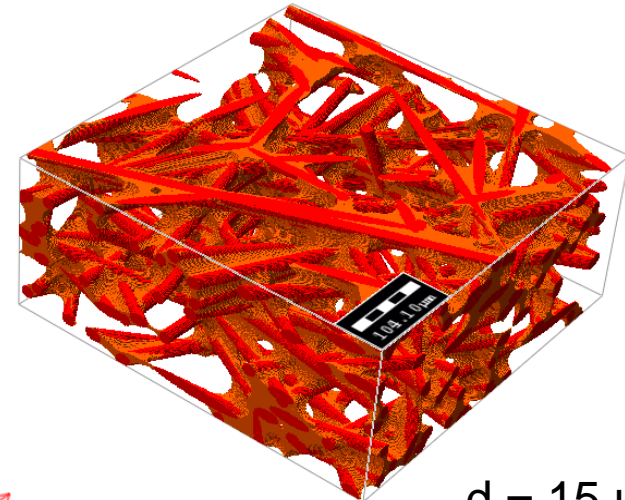


# Design Study: Fiber Diameter

- 12 vol% fibers
- binder content 40 wt% (leads to porosity 80%)

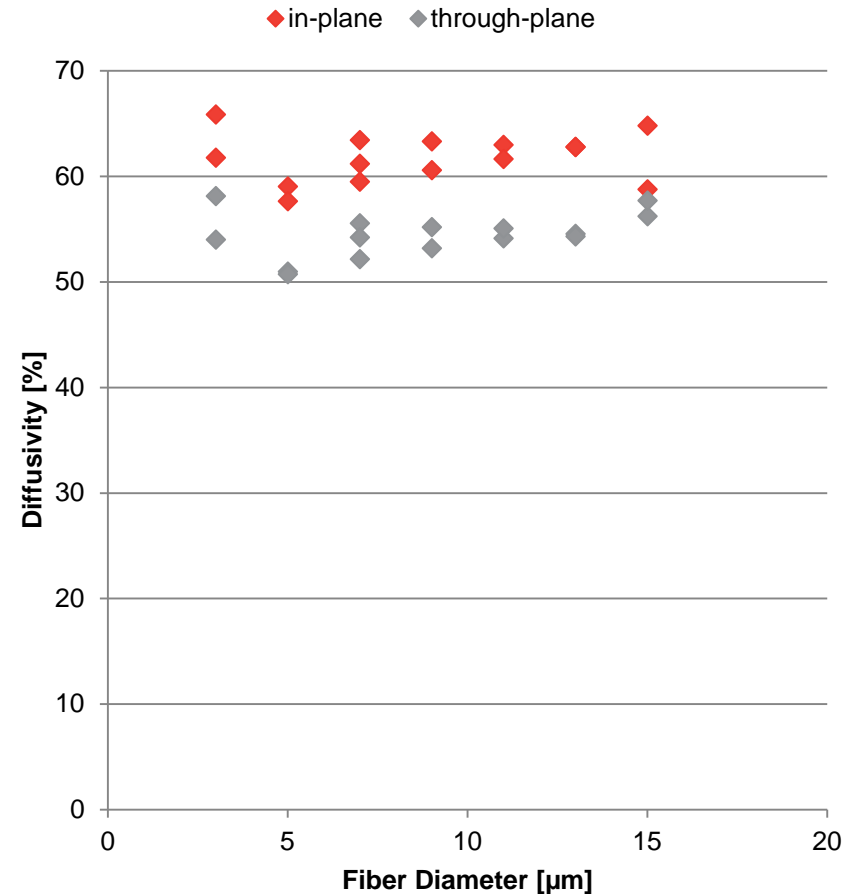
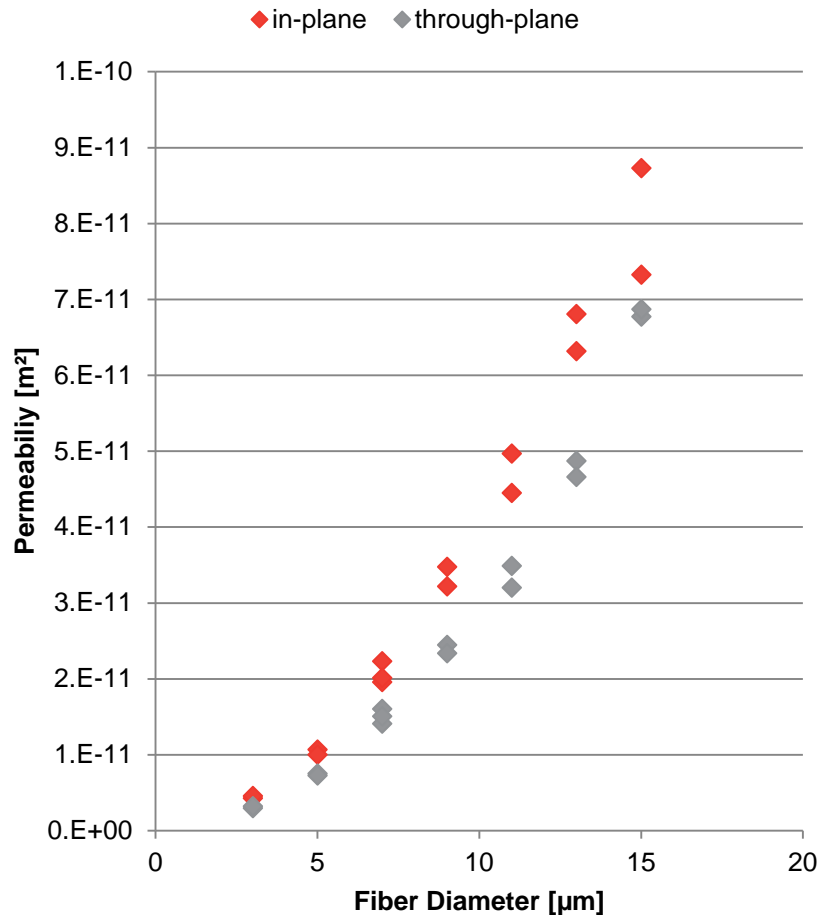


$d = 3 \mu\text{m}$



$d = 15 \mu\text{m}$

# Permeability and Diffusivity



# Thank You !



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