

---

# Mikrostruktursimulation der mechanischen Deformation von Fasermaterialien

---

Heiko Andrä<sup>1</sup>, Andreas Fink<sup>1</sup>, Michael Godehardt<sup>2</sup>, Matthias Kabel<sup>1</sup>,  
Janis Sliseris<sup>1</sup>, Sarah Staub<sup>1</sup>, Oliver Wirjadi<sup>2</sup>

<sup>1</sup> Strömungs- und Materialsimulation

<sup>2</sup> Bildverarbeitung

Fraunhofer ITWM, Kaiserslautern

VVD 2015 – Verarbeitungsmaschinen und Verpackungstechnik  
12. und 13. März 2015 in Dresden/Radebeul

# Outline

- Introduction and Motivation
- Image processing of 3D  $\mu$ CT scans
- Generation of representative volume elements for microstructures
- Microscale simulation and numerical homogenization
- Two-scale simulation

# Computer Aided Material Characterization

Mechanical properties of fibrous materials (paper, paperboard, fiberboard) depend on a variety of microstructural parameters, e.g.:

- Fiber orientation (FO)
  - Fiber length, curvature and thickness
  - Fiber volume fraction
- Measurements are complicated (or even impossible) and need to be done for many samples

A combination of measurements for simple specimens and simulations for varying complex microstructure parameters accelerates the material characterization of fibrous materials.

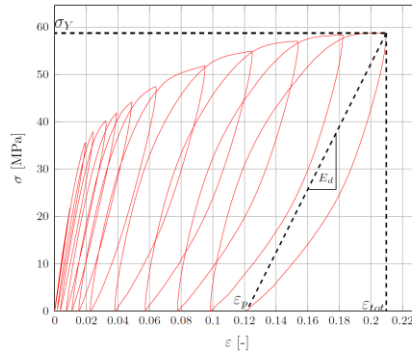
Nonlinear computations on realistic samples are expensive.

→ Fast microscale solvers necessary

# Computer Aided Material Characterization

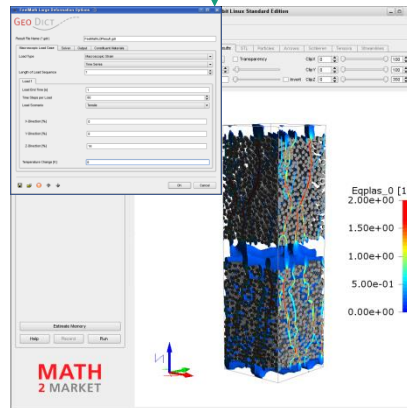
Measurement for specimen

- Isotropic behavior
- Rate dependent

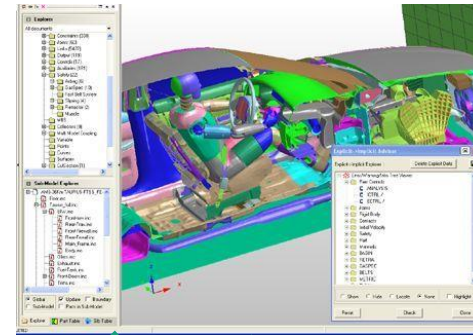


Microscale simulation

- Microstructure can be easily changed
- Effect of defects (pores) can be studied
- Complicated coupon test can be reduced



Material CAE

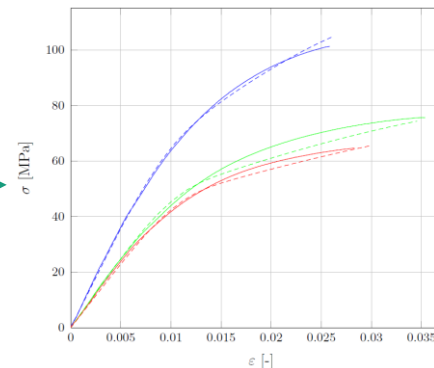


Macro-scale simulation with LS-DYNA or PAMCRASH

- Arbitrary geometries
- Local mesh refinement

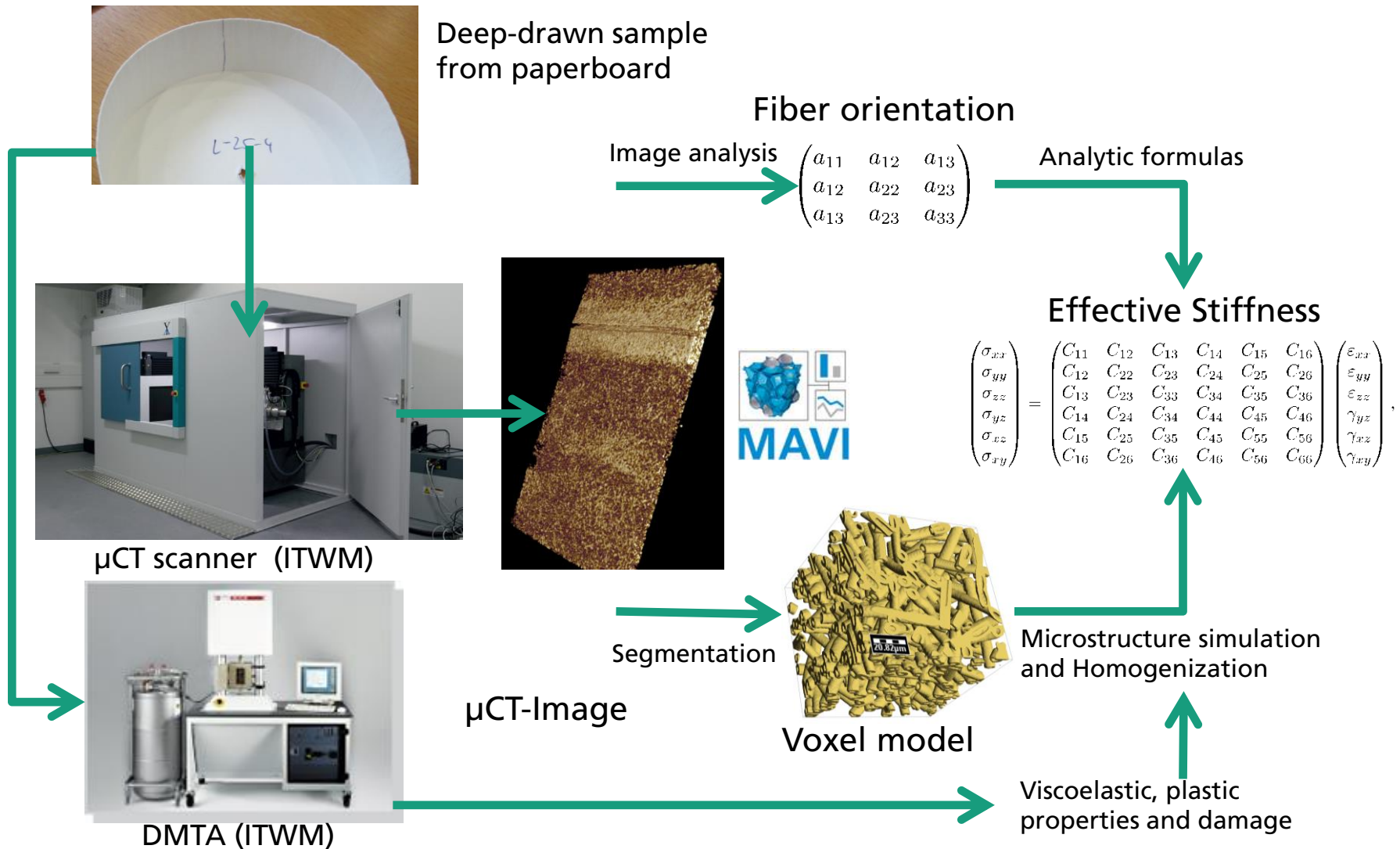
Material cards

- Simulation results are used to derive effective material laws
- Anisotropic behavior
- Rate dependent

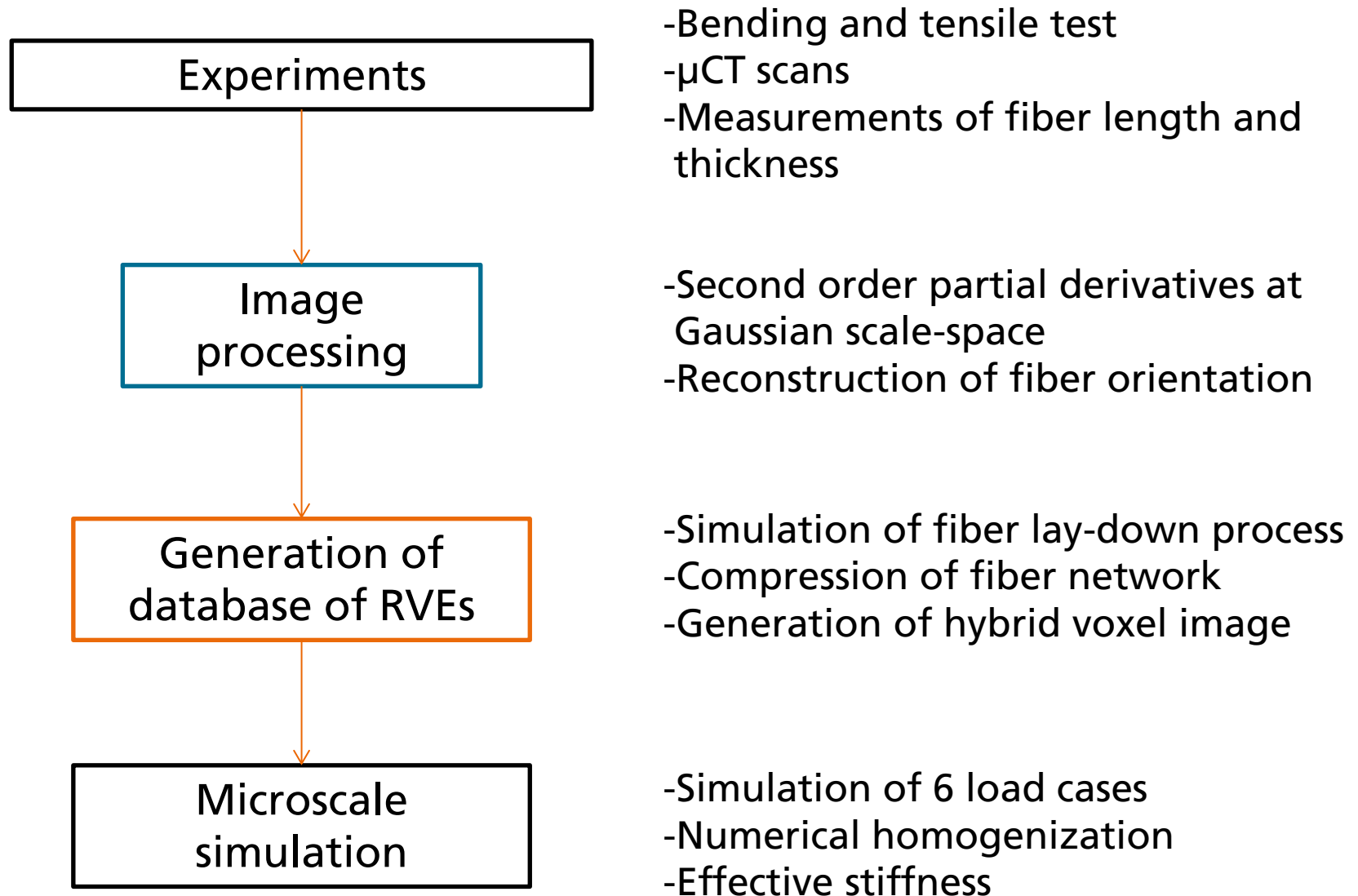


Structural CAE

# Material and microstructure characterization

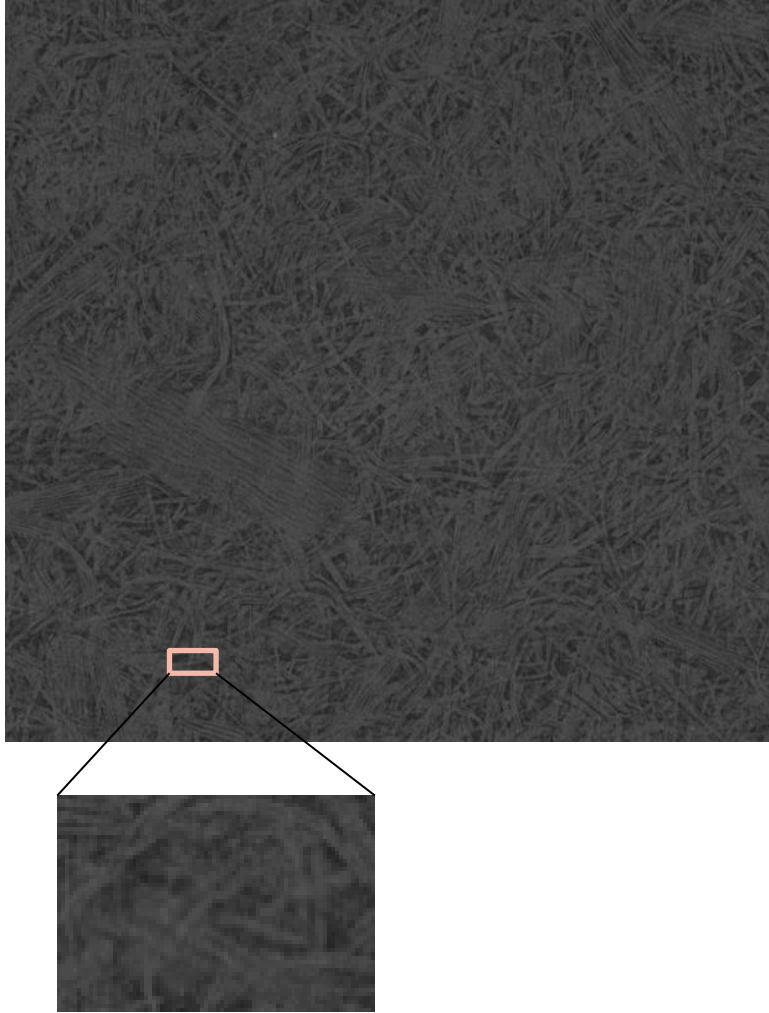


# Microstructure simulation technique



# 3D Imaging: Fiberboard

$\mu$ CT with 8  $\mu$ m voxel length

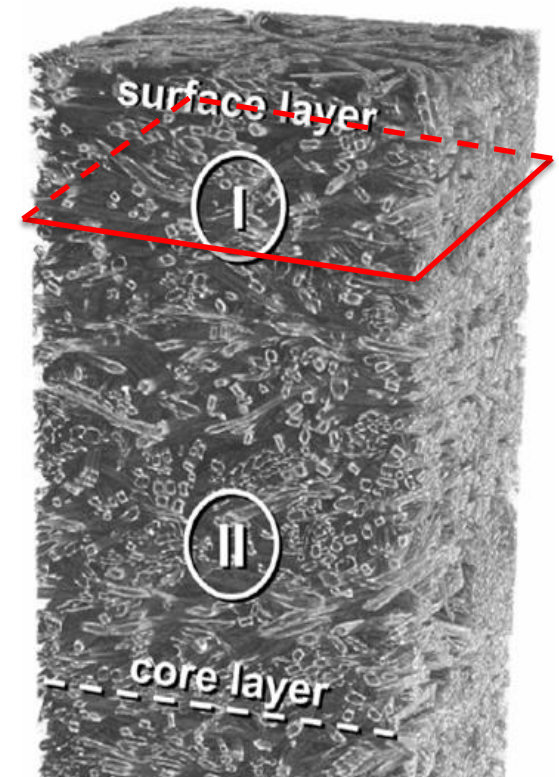
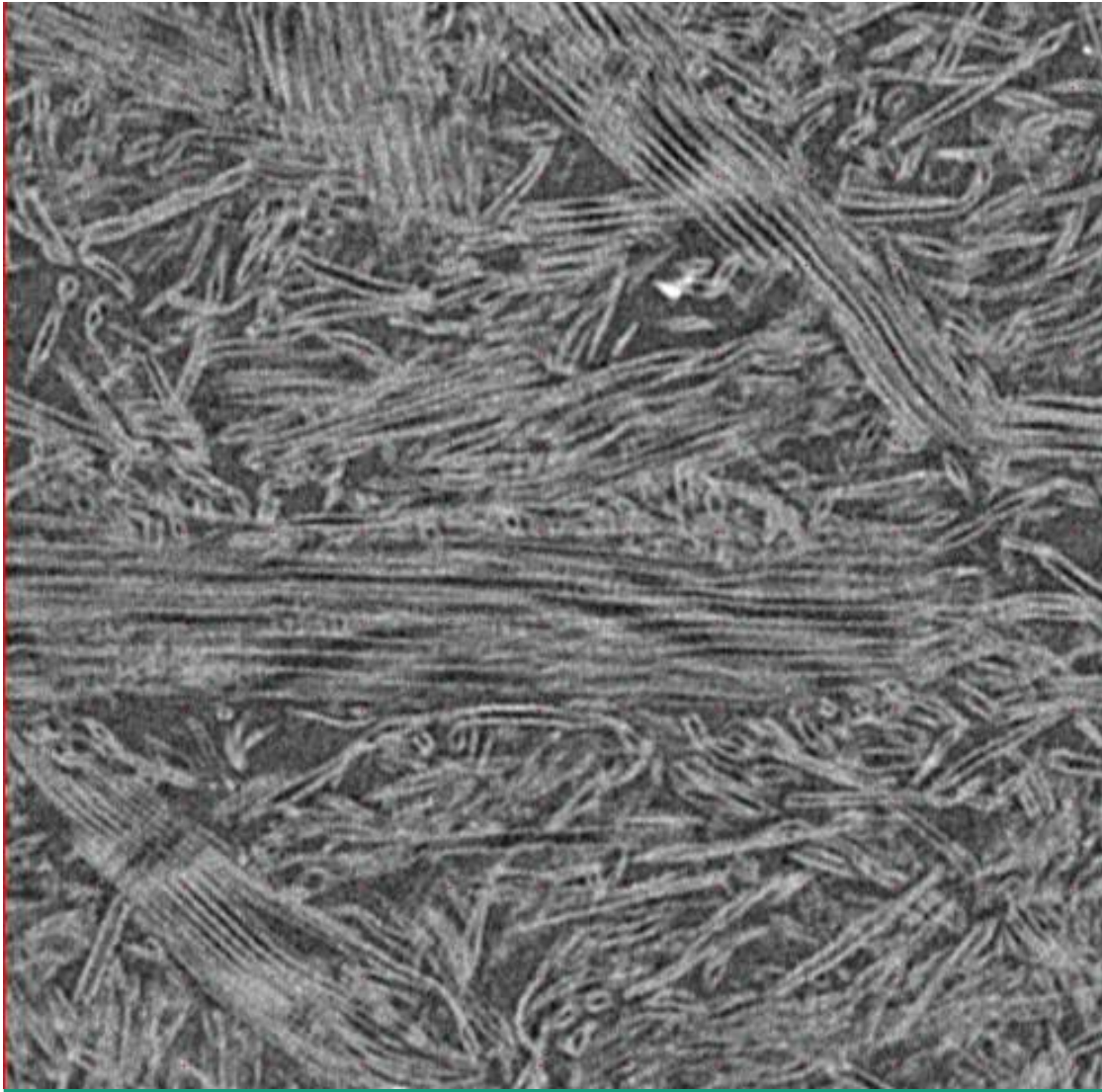


$\mu$ CT with 4  $\mu$ m voxel length





# 3D Imaging: Fiberboard



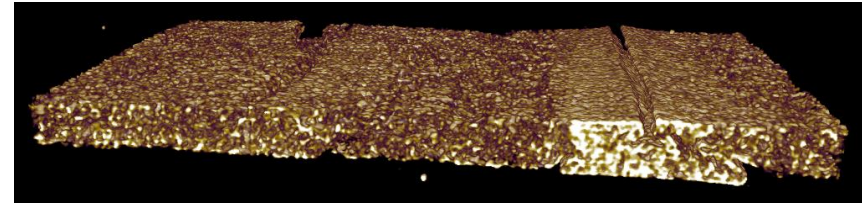
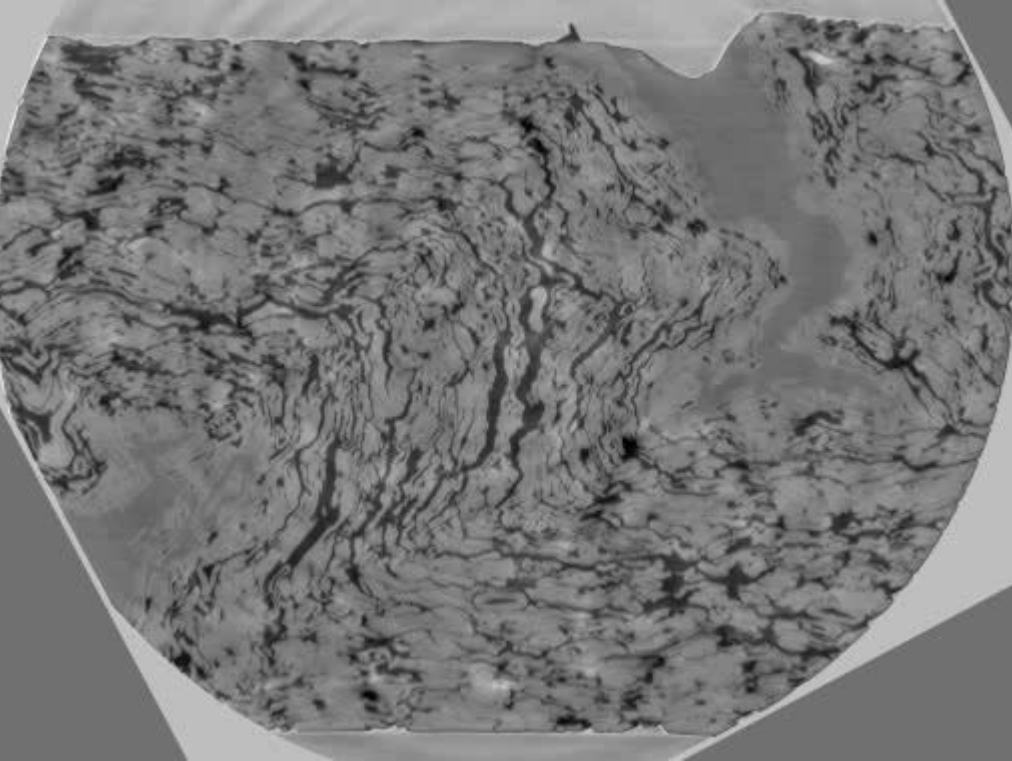
Resolution: 4  $\mu\text{m}$   
Diameter: 8 mm,  
Height: 6 mm



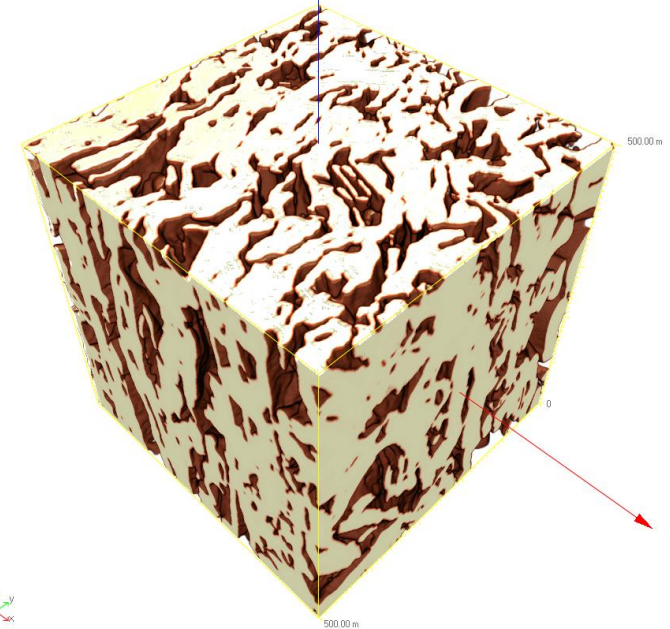
# 3D Imaging: Deep-drawn sample from paperboard (VM/VAT, TU Dresden)



Deep-drawn sample



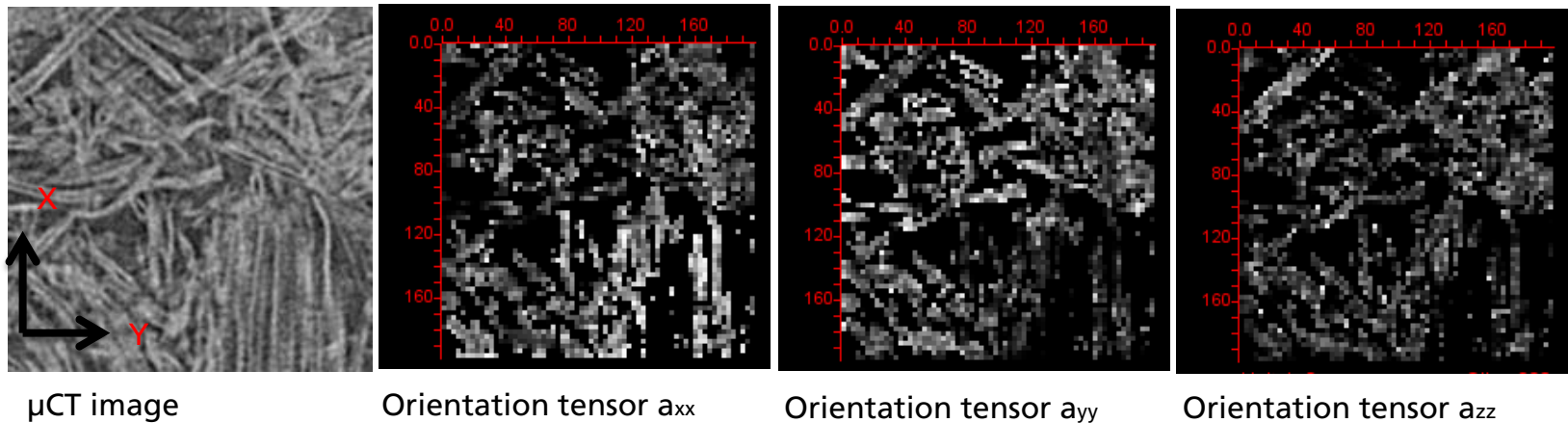
$\mu$ CT, Resolution 9.7  $\mu$ m



Synchrotron  $\mu$ CT, Resolution: 0.32  $\mu$ m

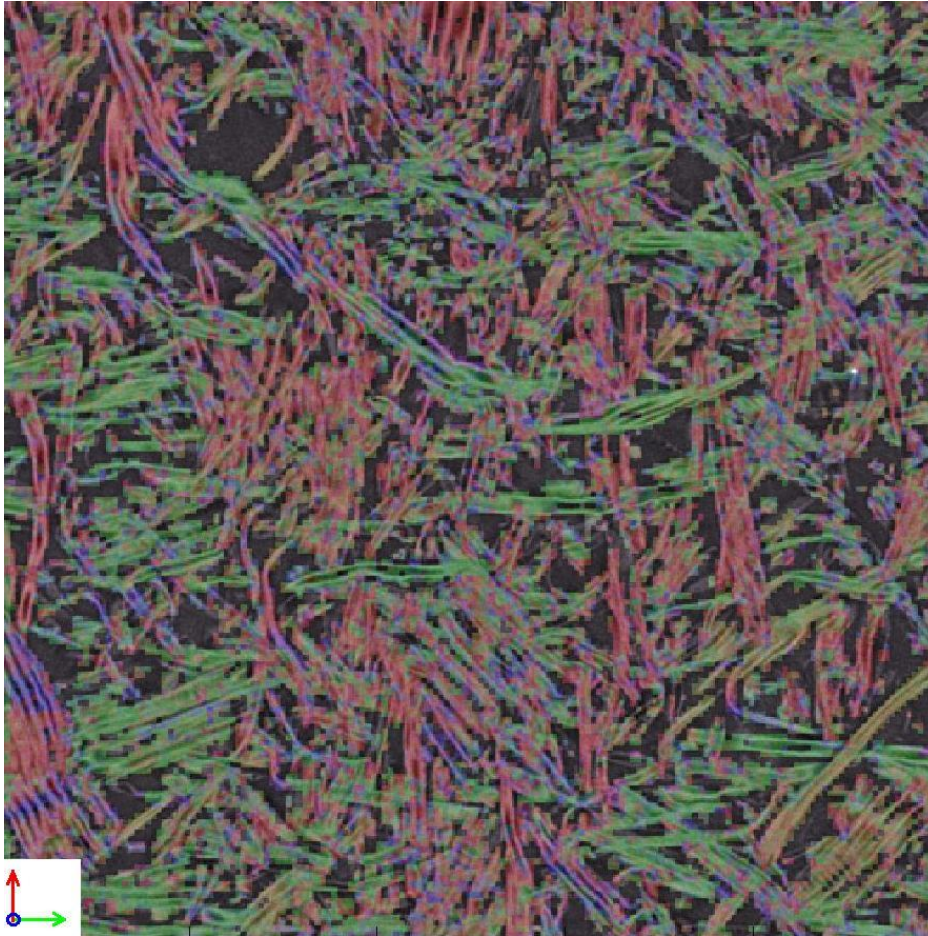
# Reconstruction of fiber orientation using direct approach

- We estimate the directional distribution by calculating the local fiber direction in each pixel.
- The eigenvector corresponding to smallest eigenvalue of the Hessian matrix is interpreted as local direction. Orientation tensor of fiber is obtained by averaging local directions over small sub-volumes.
- This is done using MAVI software.
- Because of complex fiber geometry and many fiber joints, this method overestimates fibers which are oriented in z direction.



Lighter color indicates higher value

# Reconstruction of fiber orientation

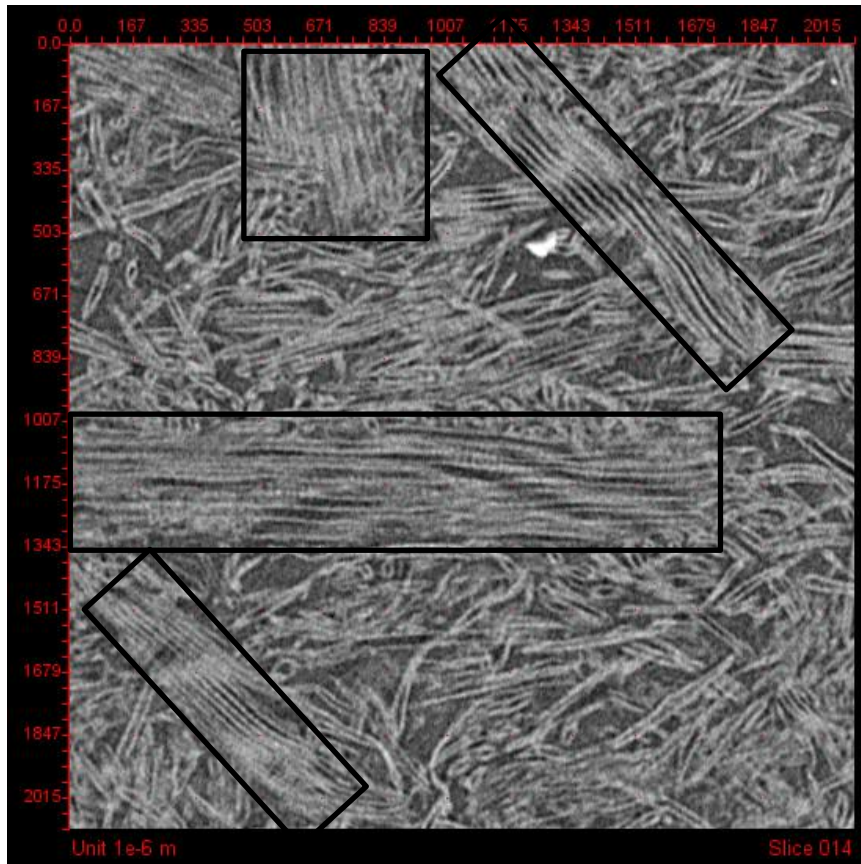


Local fiber direction map  
computed by using Hessian  
matrix.

Oliver Wirjadi



# Analysis of fiber bundles (non-separated fibers)



Non separated fibers (fiber bundles) are analyzed using  $\mu$ CT image.

Fiber bundles are detected by observing that the local fiber orientations are more homogeneous within fiber bundles than elsewhere.

The solid volume fraction of fiber bundles is less than 10 %.

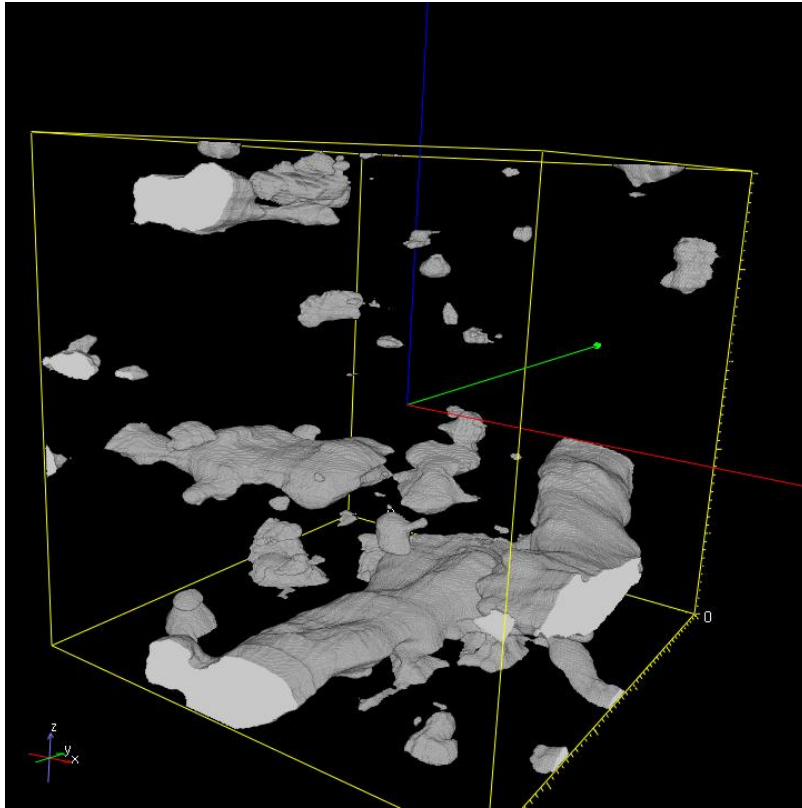
The average orientation of fiber bundles is similar to separated fiber orientation.

Resolution: 4  $\mu$ m

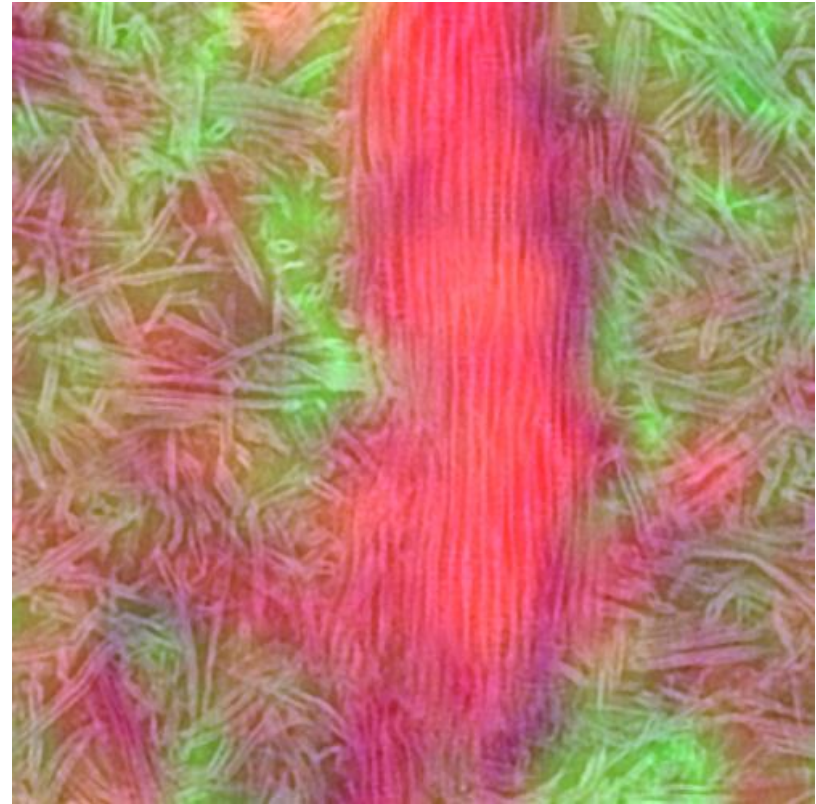
Diameter: 8 mm, height: 6 mm

Oliver Wirjadi

# Segmentation of fiber bundles



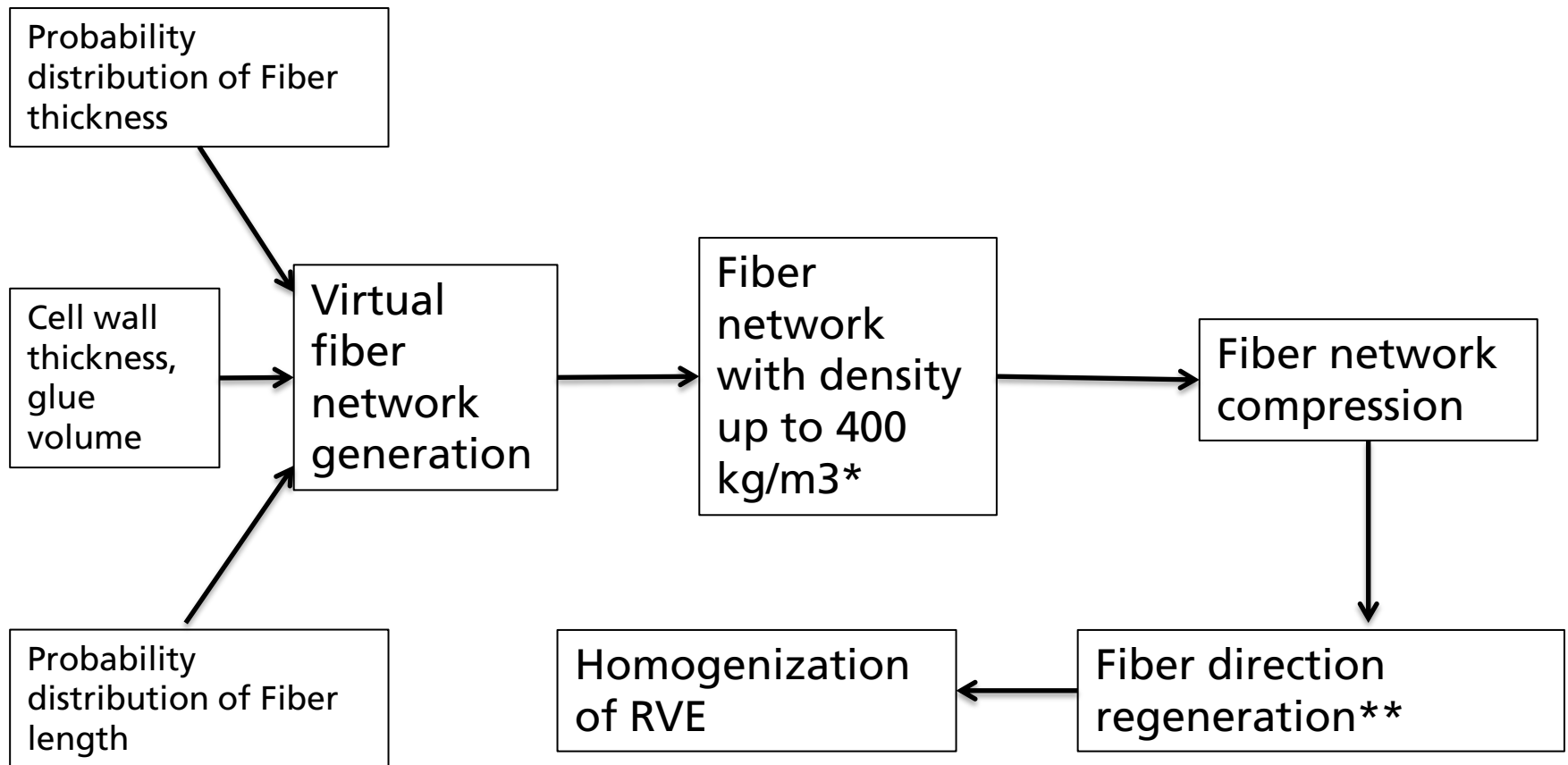
Fiber bundles in gray color



Fiber bundles in red color

Oliver Wirjadi

# Construction of representative volume elements (RVEs)

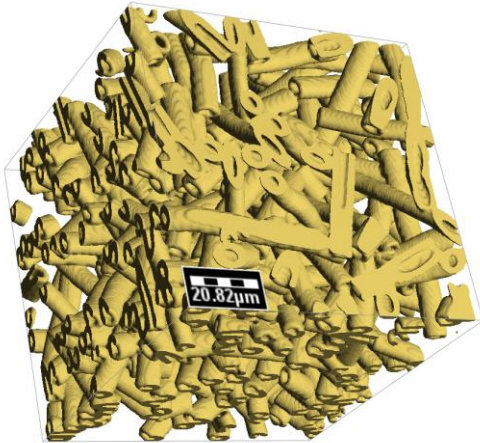


\*Fiber overlapping is not allowed,

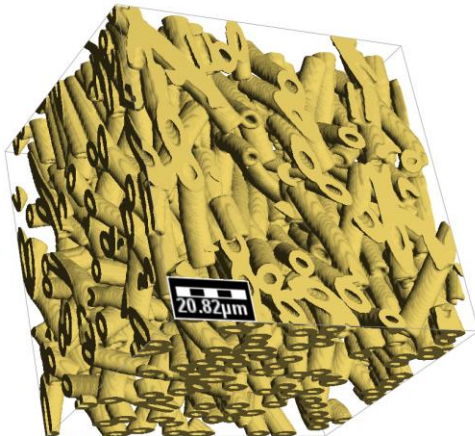
\*\*We assume that wood fibers are transversal isotropic



# Construction of representative volume elements (RVEs)

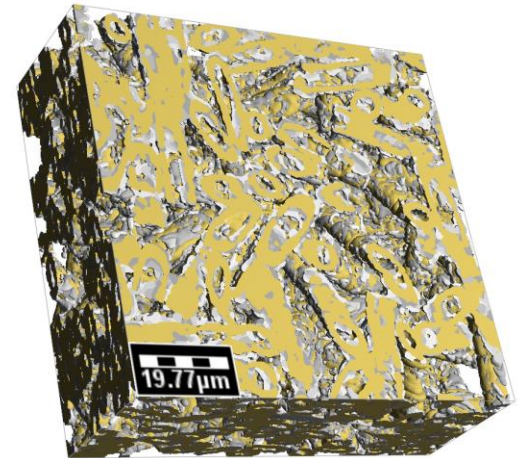


In-plane isotropic FO



In-plane anisotropic FO

Simulation of  
mechanical  
compression



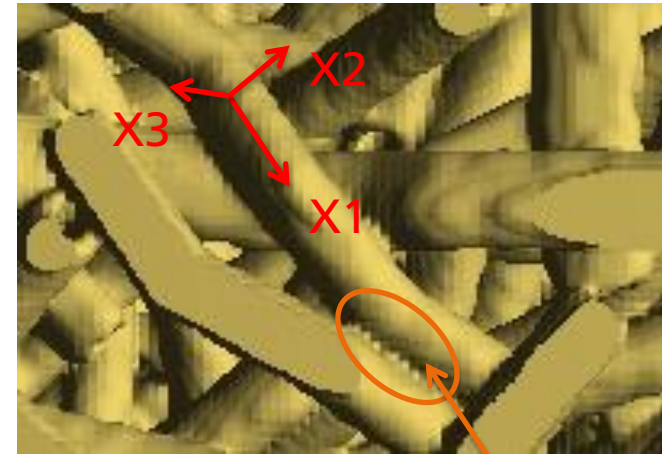
In-plane isotropic FO



In-plane anisotropic FO

# Failure criteria of wood fiber cell wall and glue

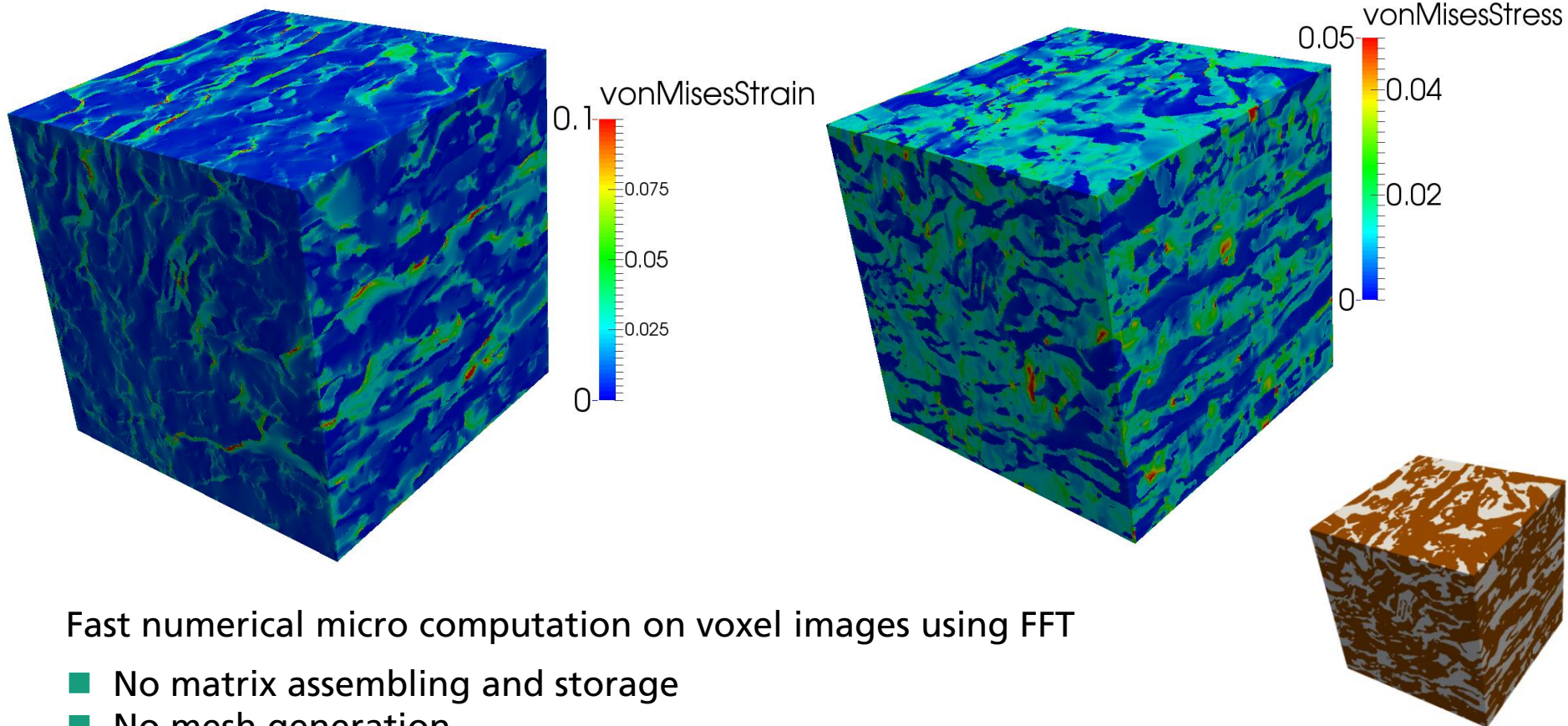
1. Axial strength criteria
2. Transversal strength criteria
3. Shear strength criteria



Fiber joint

If the strength criteria is not satisfied, then damage variables are computed and the stiffness is reduced using damage variables.

# Computation of local stress and strain fields

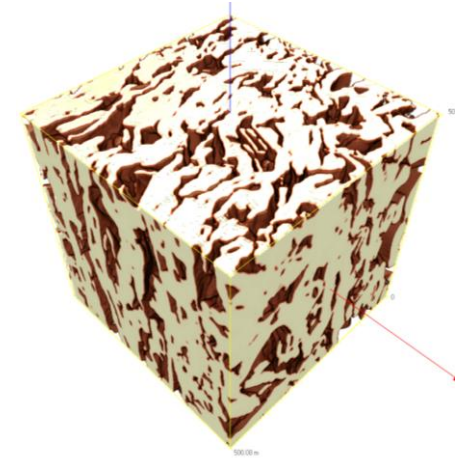
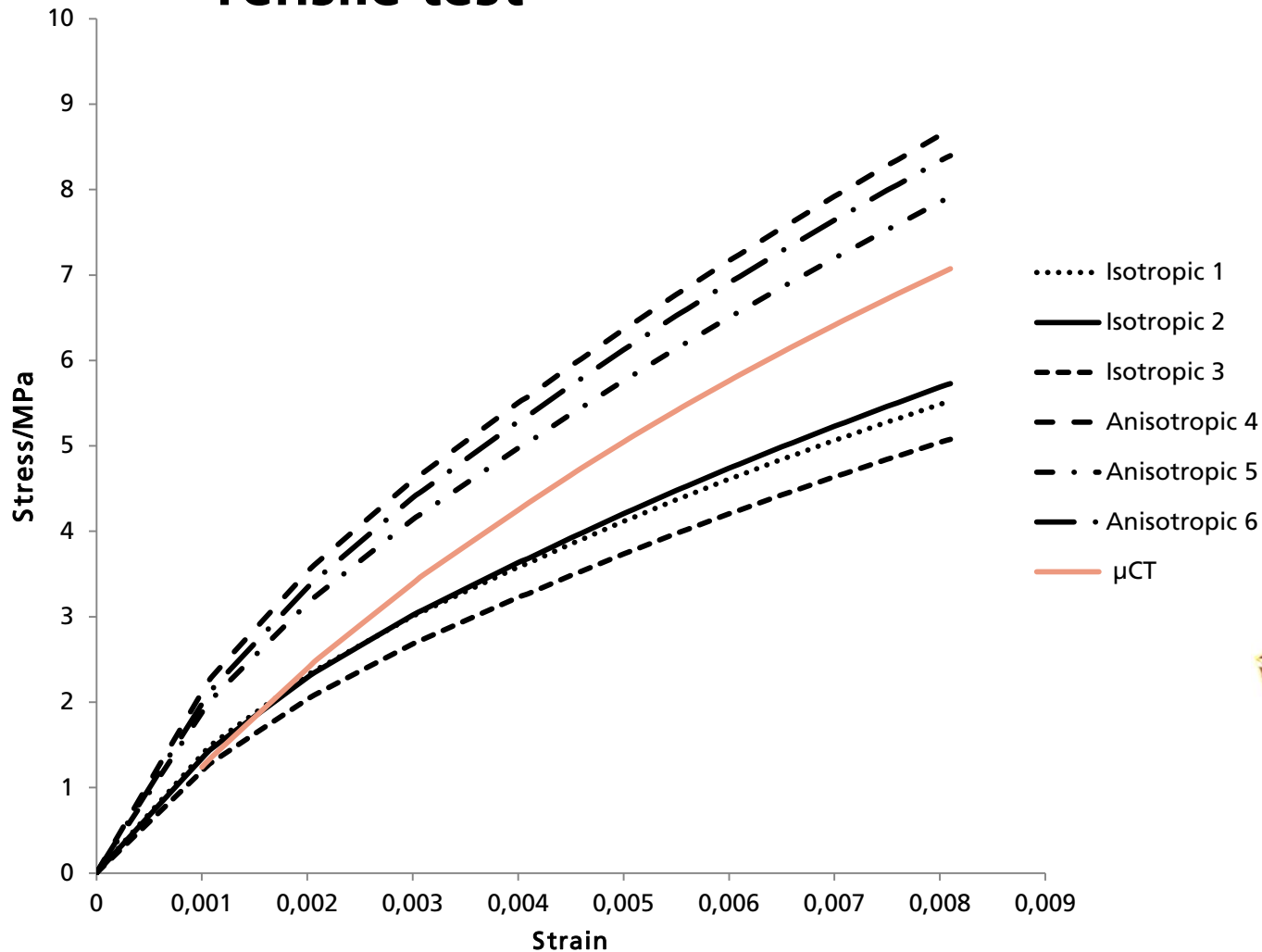


Fast numerical micro computation on voxel images using FFT

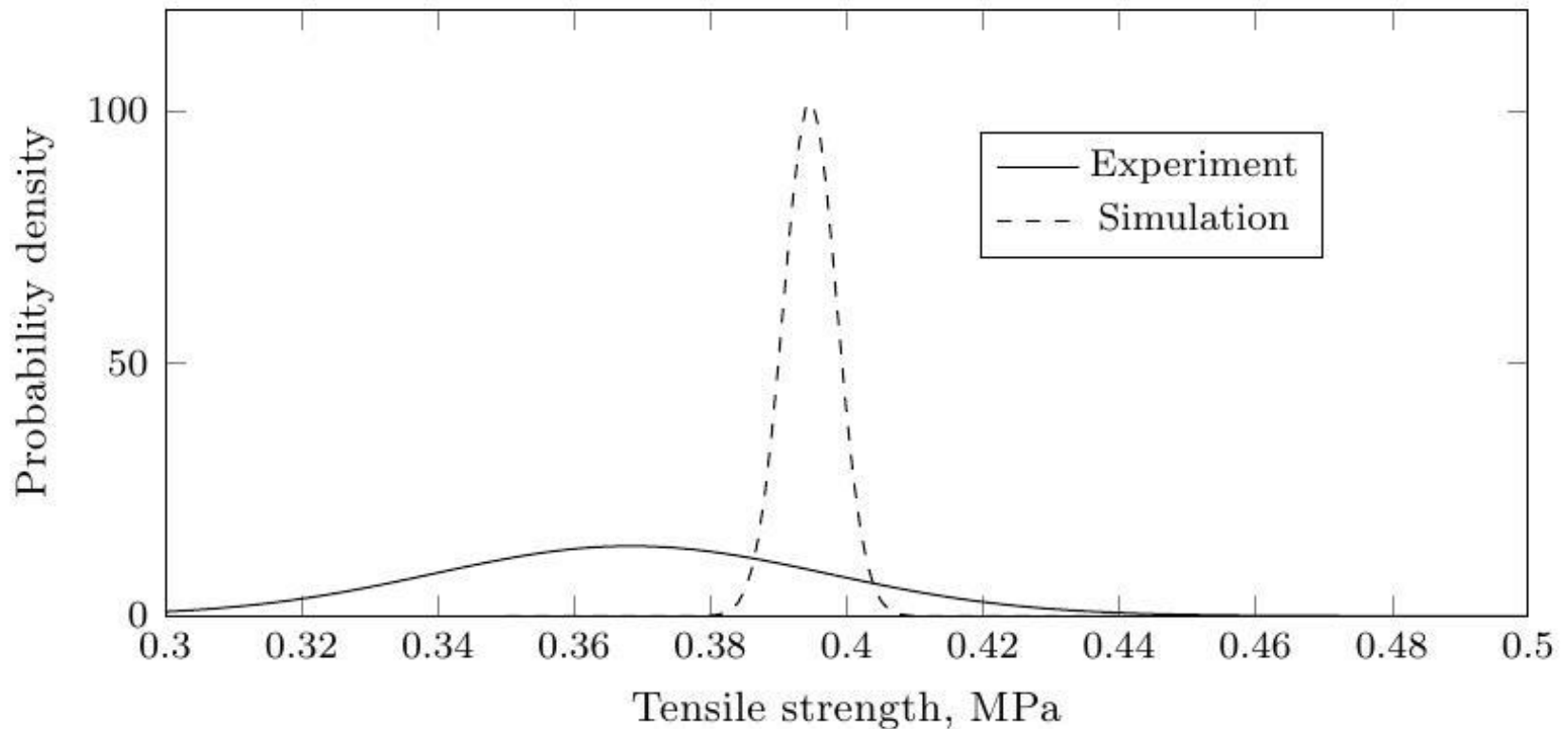
- No matrix assembling and storage
  - No mesh generation
  - PDE is reformulated as volume integral equation of Lippmann-Schwinger type
- ⇒ Efficient computation of large microstructures (512 x 512 x 512 voxels)



# Results of numerical homogenization: Tensile test

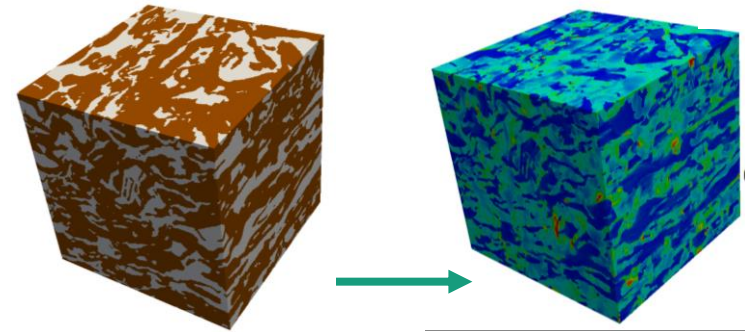
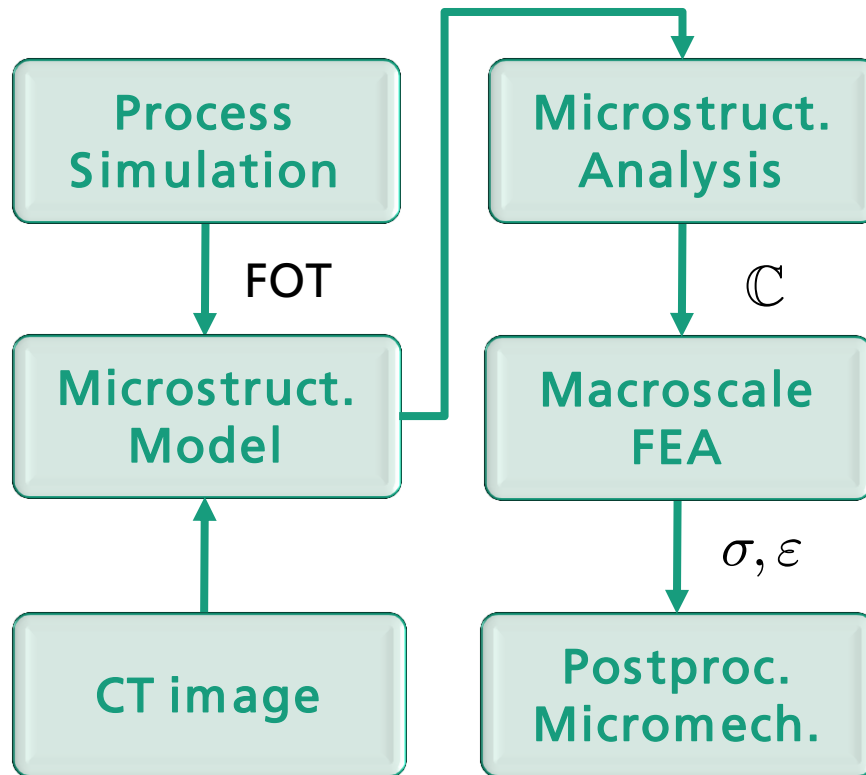


# Comparison of numerical and experimental results of tensile test (fiberboard)



Difference between average computed tensile strength and experimentally measured is less than 5%, however the standard deviations varies much more.

# Two-scale simulation

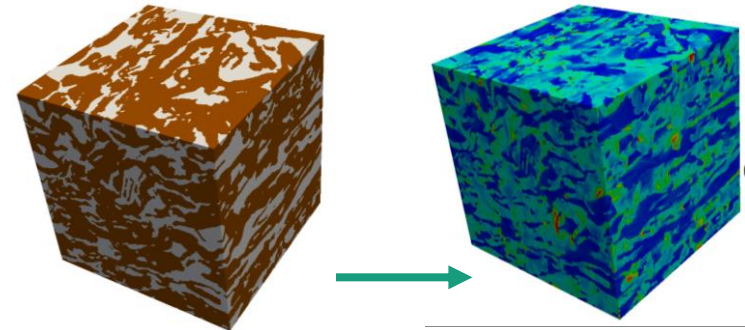
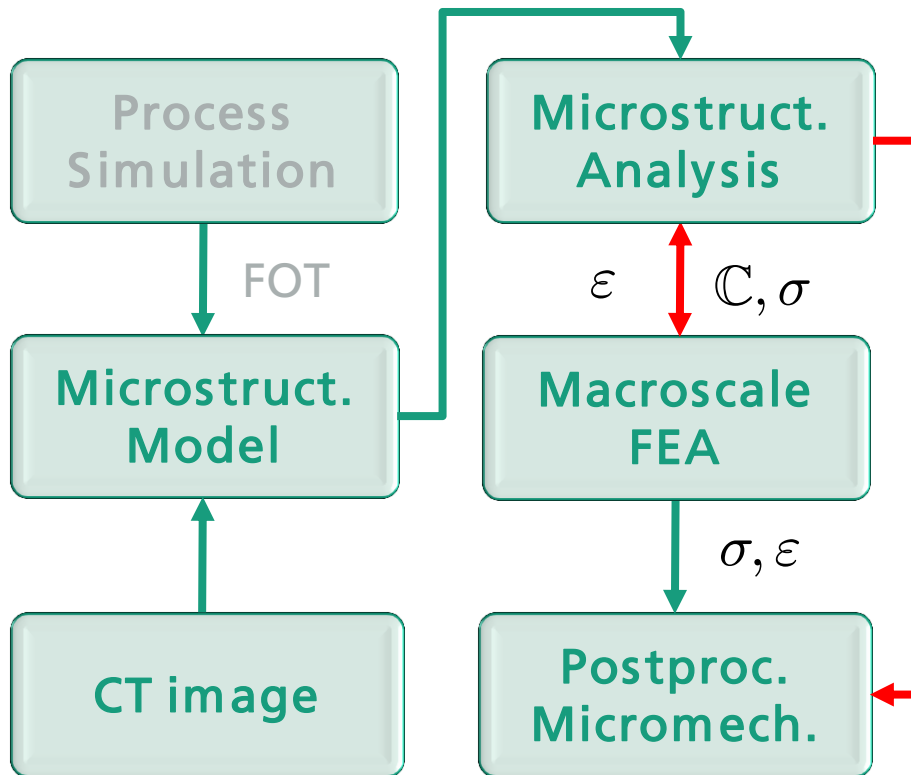


- micro. analysis in advance
- for arbitrary microstructures
- varying elasticity coefficients
- matrix damage, fiber fraction
- interface debonding
- no load history
- proportional loading

- Analytical or discrete geometrical model of the microstructure
- Analytical or numerical microstructural analysis (linear or nonlinear)



# Coupled two-scale simulation



- for arbitrary microstructures
- varying elasticity coefficients
- arbitrary loading
- progressive damage

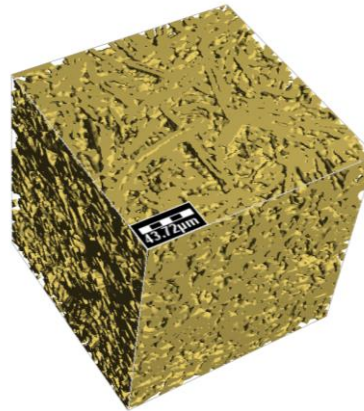
- Multiscale simulations are very expensive and therefore almost not accepted.
- → Fast “micro solvers” are needed.

# Two scale simulation of three point bending test (fiberboard)

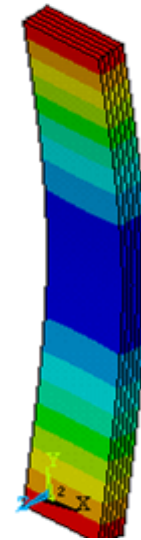
Density profile, fiber orientation according to  $\mu$ CT scans



Micromechanical model (GeoDict, FeelMath)

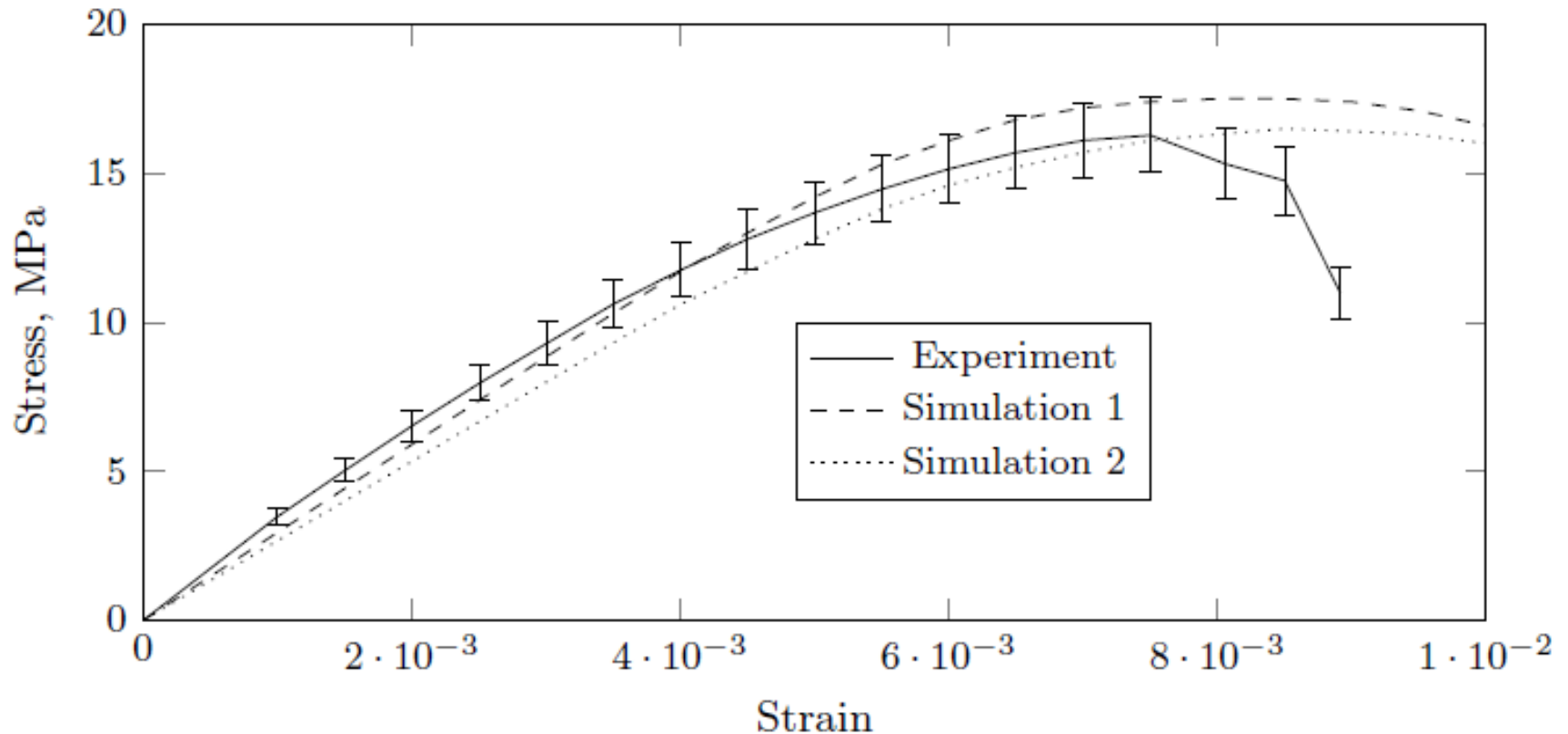


Macromechanical model



Database of stiffness tensor depending on strain tensor

# Two scale simulation of three point bending test (fiberboard)



# Applications of FeelMath

## ■ Porous materials

- Filter media (Oil and water filter)
- Metallic knitted fabrics
- Sanitary products
- Packaging
- Medium density fiberboards (MDF)
- Rocks
- Polymer foams

## ■ Composites

- Short and long fiber reinforced plastics (CFRP + GFRP)
- Metallic alloys (AlSi, MMC)
- Steel reinforced concrete

## ■ Nonlinear material behavior

- Plasticity
- Damage
- Plasticity + Damage
- Thermal expansion and shrinkage
- Residual stresses
- Creep
- UMAT-Interface

# The End

Sliseris J, Andrä H, Kabel M, Dix B, Plinke B, Wirjadi O, Frolovs G: Numerical prediction of the stiffness and strength of medium density fiberboards, Mechanics of Materials **79** (2014) 73-84

Thank you very much for your attention.

Visit us at

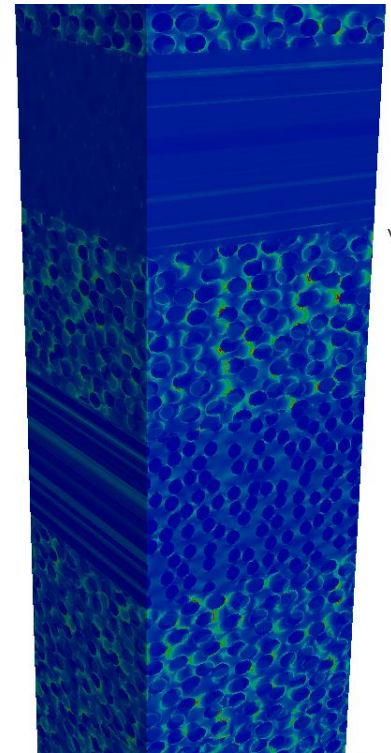
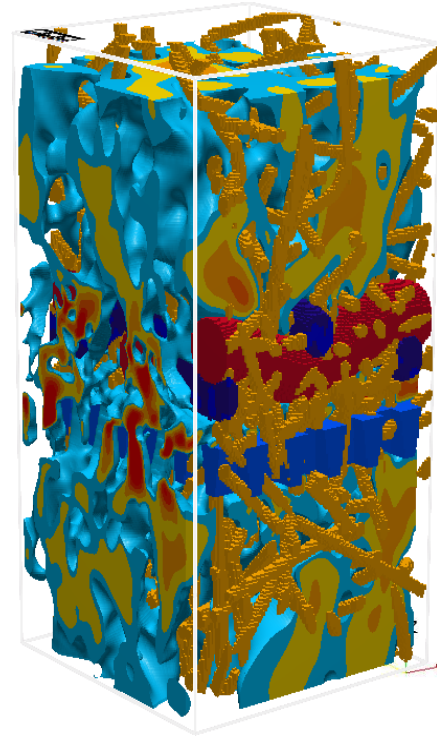
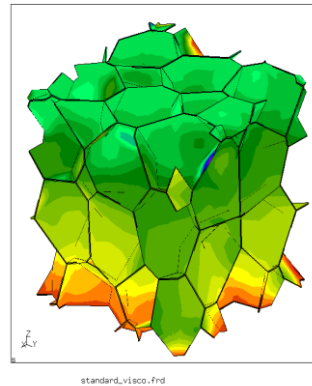
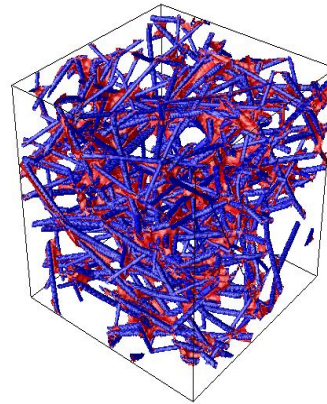
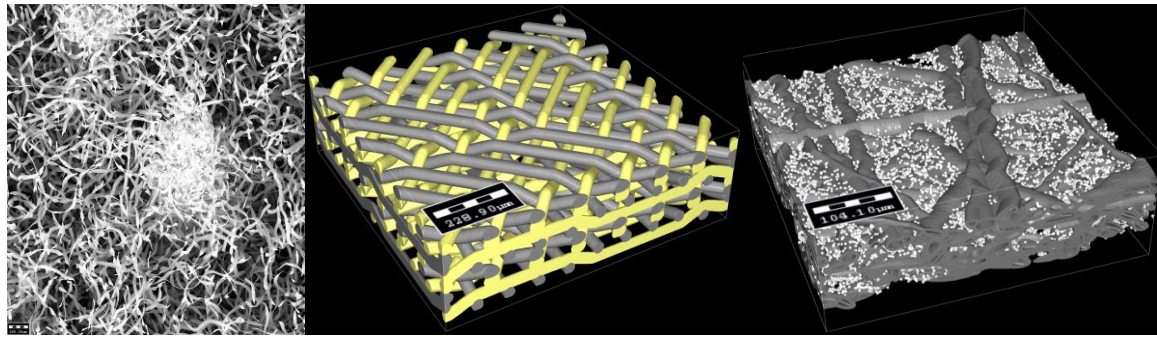
**[www.itwm.fraunhofer.de](http://www.itwm.fraunhofer.de)**

Generation of microstructures



# Porous and Composite Material design

- Paper, cellulose material: permeability, capillarity
- Non-wovens (textiles): filter efficiency
- Weaves: flow resistance
- Foam: Heat or acoustic insulation material
- Sinter material: ceramics, MMC thermo-mech. behaviour
- Fibre reinforced composites: visco-elastic behavior, creep, fatigue, damage





# Virtual Material Laboratory

## Modules of the **GeoDict** Software

### Material Models

- **Fiber**Geo
- **Sinter**Geo
- **Paper**Geo
- **Weave**Geo
- **Grid**Geo
- **Pack**Geo
- **Pleat**Geo
- **Paper**Geo
- **Layer**Geo
- **Foam**Geo
- **Gad**Geo

### Property Computation:

- **Flow**Dict (single phase flow properties)
- **Addi**Dict (particle transport)
- **Elasto**Dict (effective elastic properties)
- **Conducto**Dict (effective conductivity)
- **Diffu**Dict (effective diffusivity)
- **Filter**Dict (pressure drop, efficiency, life time)
- **Satu**Dict (two phase flow properties)
- **Poro**Dict (pore size measures)
- **Acousto**Dict (acoustic absorption)

**Demo version &  
Information:**

[www.geodict.com](http://www.geodict.com)

**GEO** DICT is the product of **MATH  
2 MARKET**

Math2Market (M2M)  
is a spin-off company from

