Recent Improvements to the Pore-Morphology Method for Capillary Pressure and Relative Permeability Simulations

GeoCT Workshop
University of Bremen

#### Sven Linden

Andreas Wiegmann Jens-Oliver Schwarz Erik Glatt



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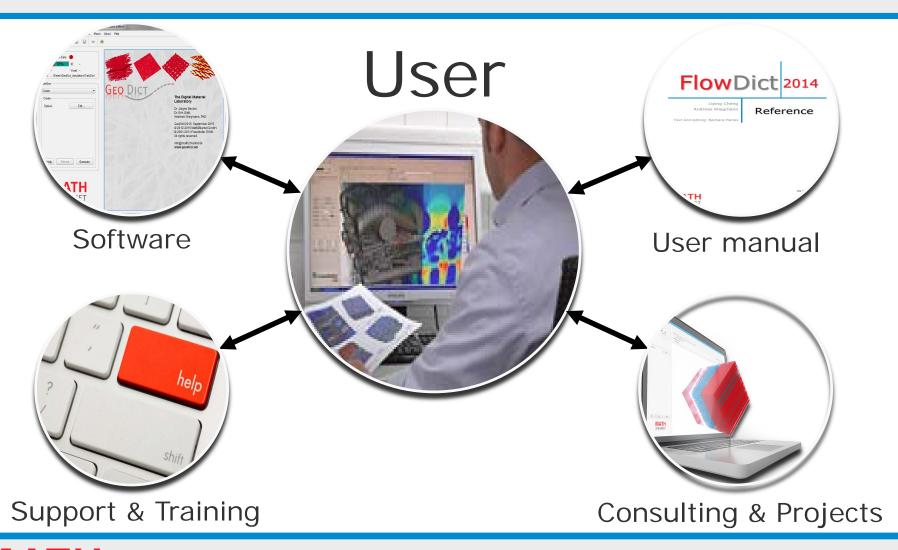
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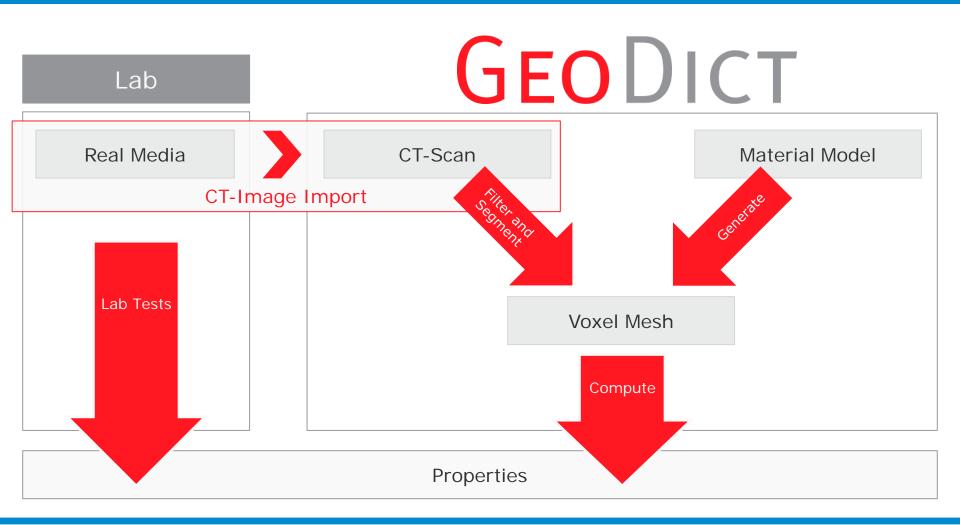
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#### **GeoDict**

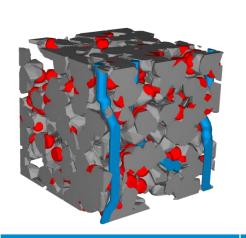
### Material Characterization & Engineering

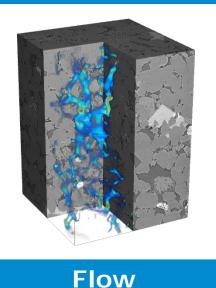


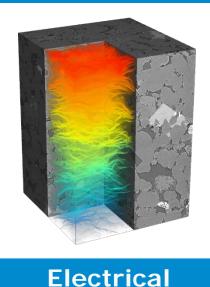


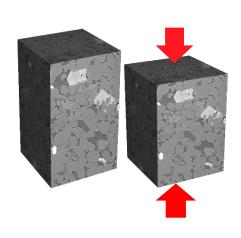
#### **GeoDict**

### Math2Market Digital Rock Physics Portfolio









Geometrical
parameters

Pore size distribution

Absolute permeability

parameters

- Multi-scale flow
- Two-phase flow
- Relative permeability
- Cap. pressure curve

### Formation factor

- Resistivity index
- Saturation exponent

**Parameters** 

Cementation exponent

### Mechanical parameters

- Elastic moduli
- Stiffness
- In-Situ conditions



Porosity

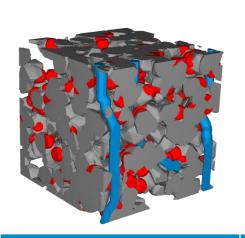
Percolation

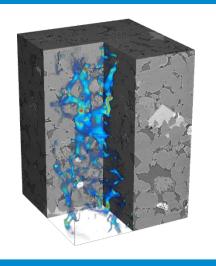
Tortuosity

Surface area

#### **Geo**Dict

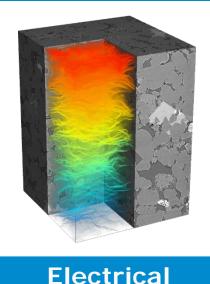
## Math2Market Digital Rock Physics Portfolio

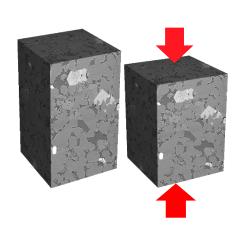




**Flow** 

parameters





## Geometrical parameters

Pore size distribution

- PorosityAbsolute permeability
  - Multi-scale flow
  - Two-phase flow
  - Relative permeability
  - Cap. pressure curve

### Formation factor

**Parameters** 

- Resistivity index
- Saturation exponent
- Cementation exponent

## Mechanical parameters

- Elastic moduli
- Stiffness
- In-Situ conditions



Percolation

Tortuosity

Surface area

### Two Phase Flows



### ■ Two-phase flow

- "In fluid mechanis, two-phase flow occurs in a system containing gas and liquid with a meniscus separating the two phases." [Wiki]
- One fluid wets the surface, the less affinity is non-wetting
- SatuDict uses the **Pore Morphology method** to determine the distribution of the two phases inside the porous media.

#### Here

- Imbibition:
  - wetting fluid displaces non-wetting fluid
- Drainage:
  - non-wetting fluid displaces wetting fluid



### Capillary Pressure

#### Young - Laplace equation

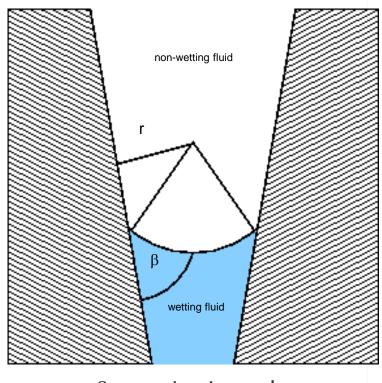
- Describes the capillary pressure difference across interfaces between two fluids
- Relates pressure difference to the shape of the surface

#########
$$p_c = \gamma \operatorname{div} \vec{n}$$
########## $p_c = 2 \gamma H$ 
########### $p_c = \gamma (\kappa_1 + \kappa_2)$ 
###############

Assumption: cylindrical pores with radius r

#######
$$p_c = \frac{2\gamma \cos \beta}{r}$$

capillary pressure ⇔ pore radius



β: contact angle



### Pore Morphology Method Basic Idea

Use this relation between pore size and capillary pressure to predict the distribution of the phases

### Advantage:

- No partial differential equation (PDE) is solved
- Purely geometrical operations
- Very low runtime and memory requirements

#### Assumption:

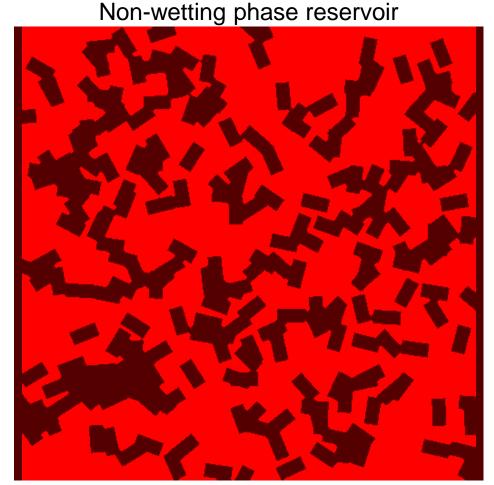
- Quasi-stationary phase distribution
- Cylindrical pores





- Connectivity of NWP to reservoir
- Move in spheres
  - Start: completely wet
  - Start: large radius (i.e. small p<sub>c</sub>)
  - Steps: smaller radius (higher p<sub>c</sub>)
- No residual WP



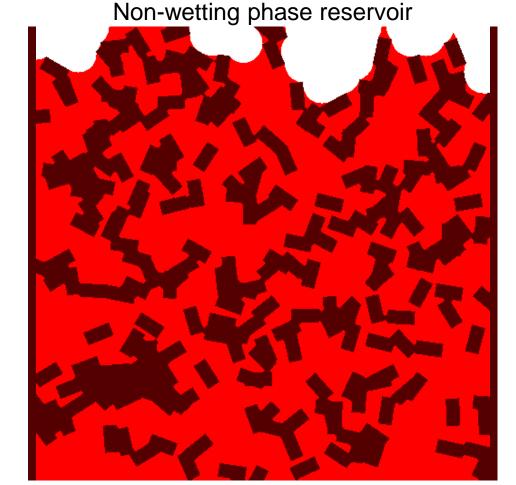


Wetting phase reservoir





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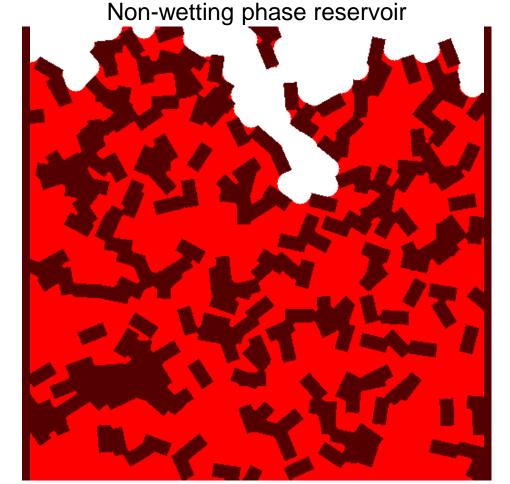
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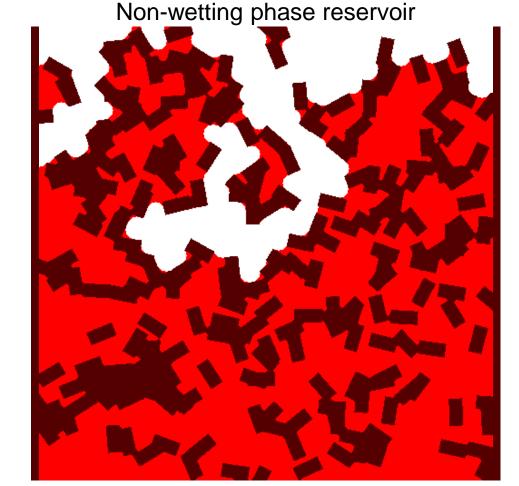
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Non-wetting phase reservoir

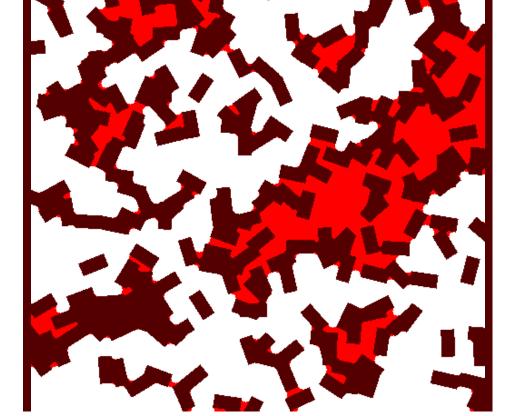
Wetting phase reservoir



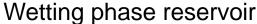




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Non-wetting phase reservoir

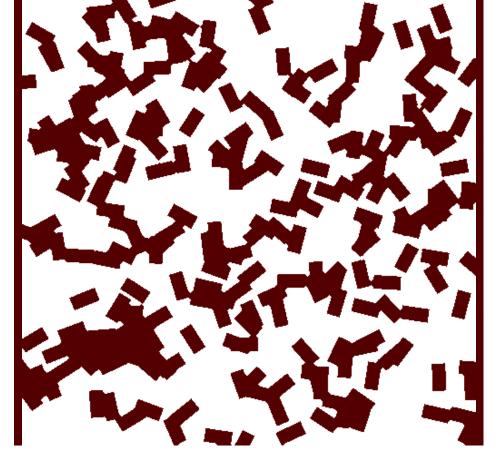








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Non-wetting phase reservoir

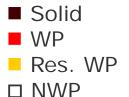


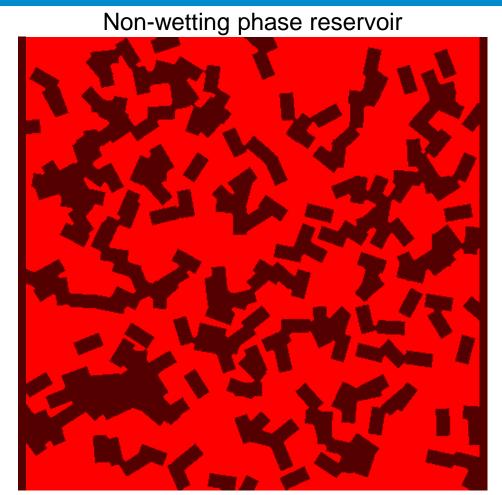






- Ahrenholz et al. 2008
- WP must be connected to reservoir
- Residual WP (orange)



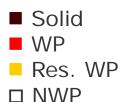


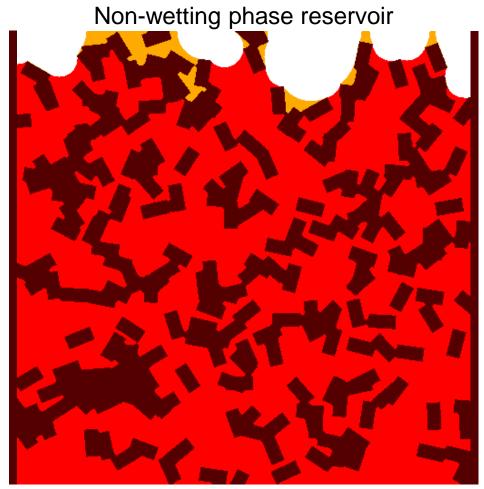
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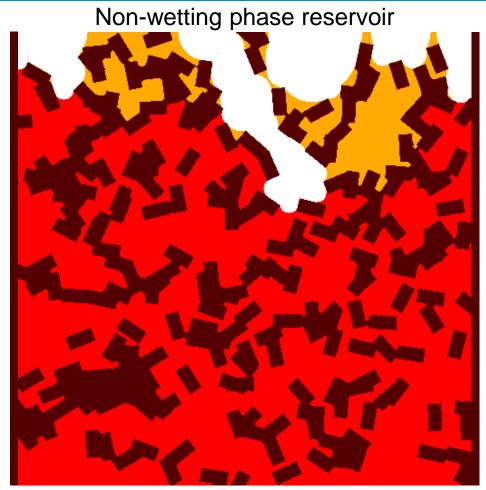
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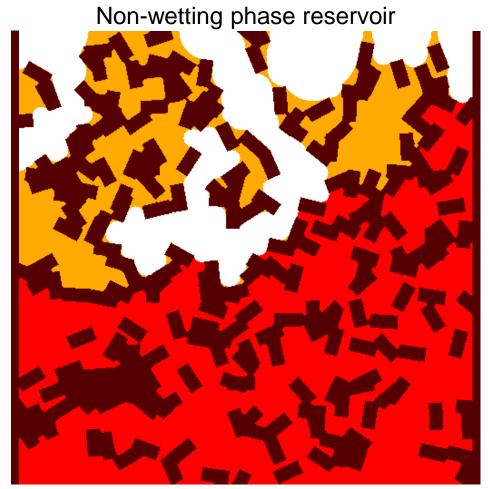
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Wetting phase reservoir



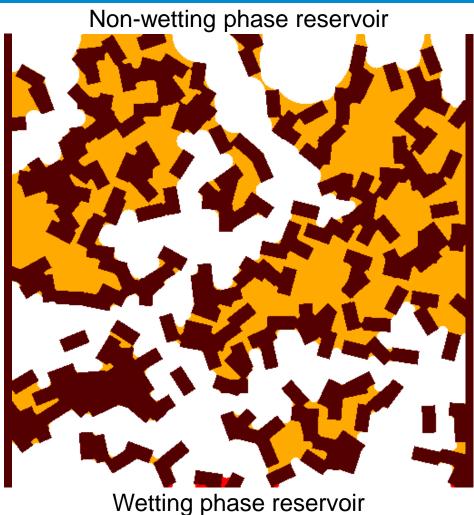


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■ Solid ■ WP

□ NWP







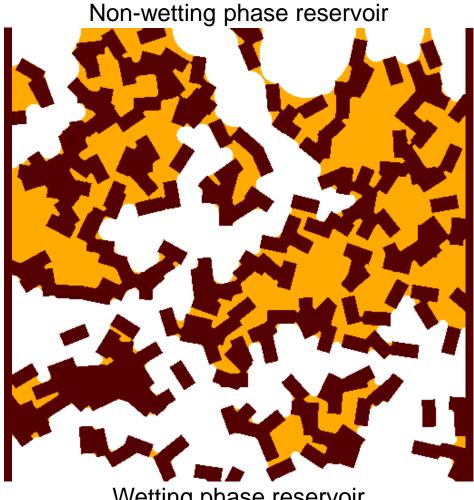


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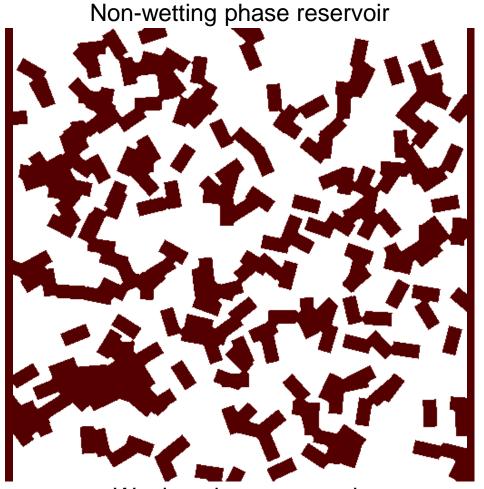






# Imbibition III wetting displaces non-wetting phase

- WP must be connected to reservoir
- NWP must be connected to NWP reservoir
- Move out spheres
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  - Start: small radius (i.e. large p<sub>c</sub>)
  - Steps: larger radius (smaller p<sub>c</sub>)
    - Solid
    - WP
    - □ NWP
    - Res. NWP

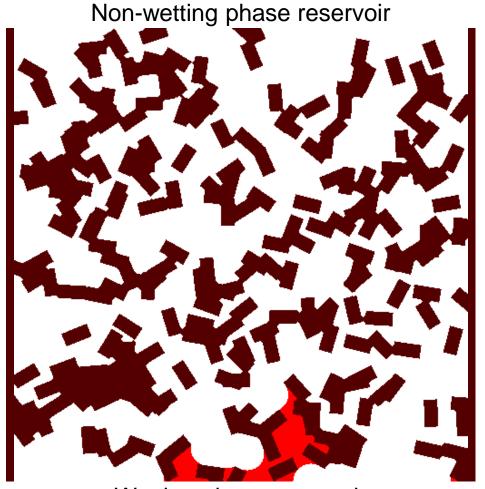






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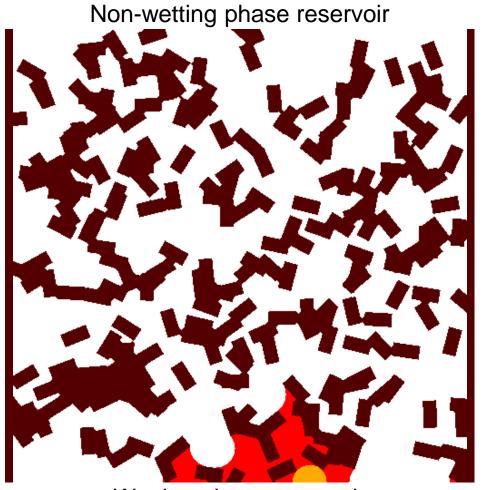






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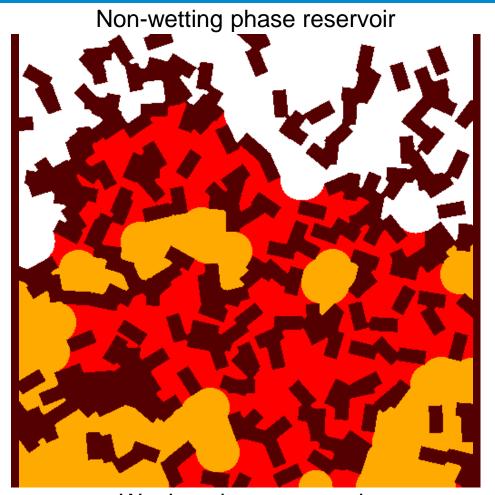
Wetting phase reservoir





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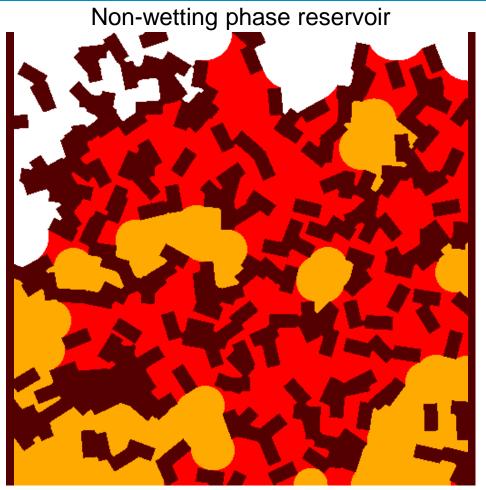


Wetting phase reservoir



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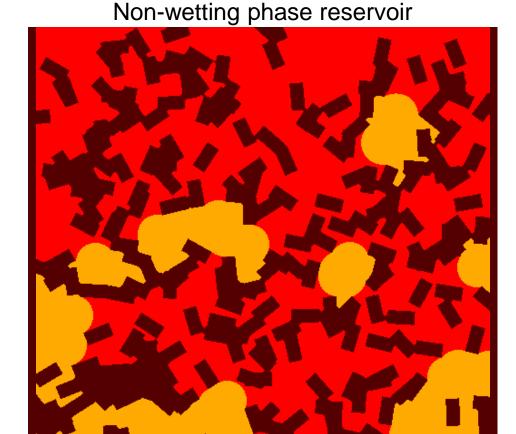


Wetting phase reservoir



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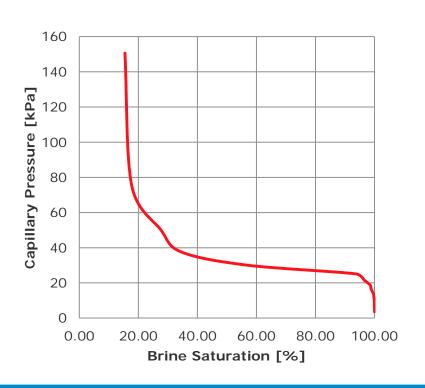


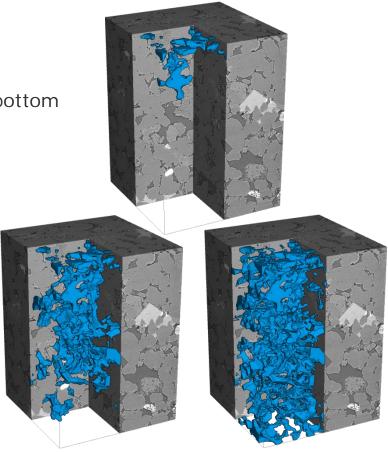
Wetting phase reservoir



## Example: Capillary Pressure for Berea Sandstone

- Drainage experiment
  - Air (NWP) drains brine (WP)
  - 40° contact angle
  - NWP reservoir at the top and WP reservoir at the bottom





Air drains brine and we visualize air saturations of 25%, 50% and 75%.



### Pore Morpholoy Method



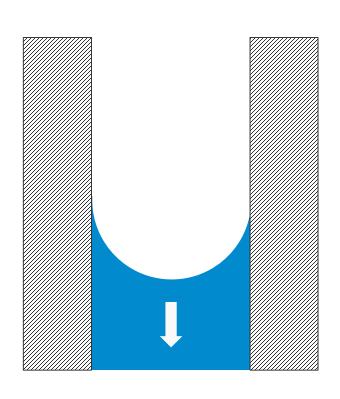
#### Limitations

- Contact angle is always zero for computed phase distributions
- Constant contact angle for the whole domain



### Saturation with Variable Wettability





When does the NWP (air) enter a cylindrical capillary?

$$p = \frac{2\gamma}{r}$$

p differential pressure

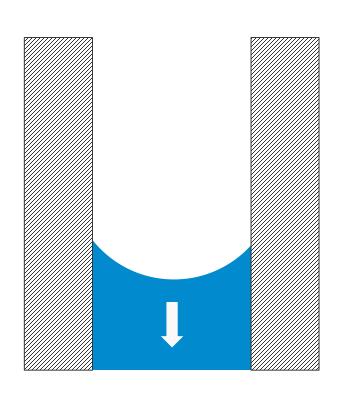
r pore radius

γ surface tension

complete wetting  $\beta = 0$ 

### Saturation with Variable Wettability





When does the NWP (air) enter a cylindrical capillary?

$$p = \frac{2\gamma}{r} \cos \beta$$

p differential pressure

r pore radius

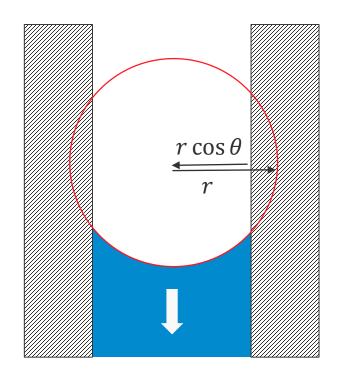
 $\gamma$  surface tension

 $\beta$  contact angle

partial wetting  $0^{\circ} < \beta < 90^{\circ}$ 



### New Idea: Can we have variable contact angles?



Idea (Schulz et al, 2014)

- $\blacksquare$  dilate by  $r \cos \theta$  (pore radius)
- $\blacksquare$  erode by r (sphere radius)

Result: contact angle  $\theta$  on pore wall

Young-Laplace: 
$$p = \frac{2\gamma}{r}$$



### Multiple Contact Angles



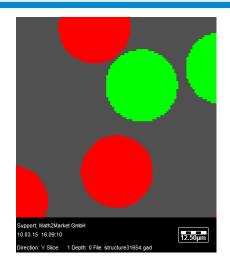


- Material 1
- Material 2
- NWP
- □ WP



### Multiple Contact Angles







1. Dilate material 1

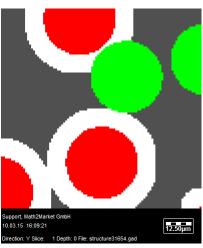
- Material 1
- Material 2
- NWP
- □ WP



### Multiple Contact Angles

#### SatuDict







- Dilate material 1
- 2. Dilate material 2

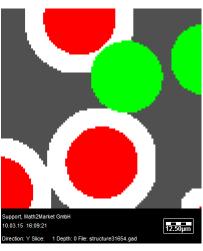


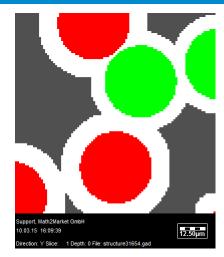


### Multiple Contact Angles

#### SatuDict







- Dilate material 1
- 2. Dilate material 2
- 3. Check connectivity

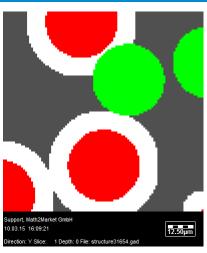






### Multiple Contact Angles







- . Dilate material 1
- 2. Dilate material 2
- 3. Check connectivity
- 4. Erode



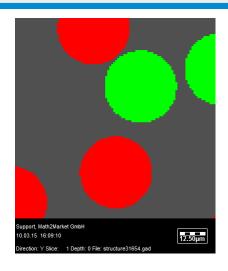




□ WP



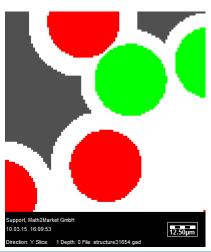
## Multiple Contact Angles



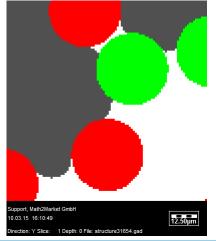




- . Dilate material 1
- 2. Dilate material 2
- 3. Check connectivity
- 4. Erode
- 5. Final result







- Material 1Material 2NWP
- □ WP



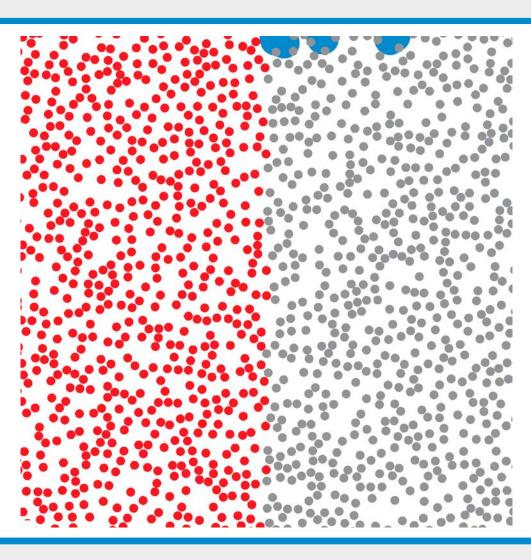
# 2D Example

SatuDict

Contact angle 0°

Contact angle 40°

Water (non-wetting)





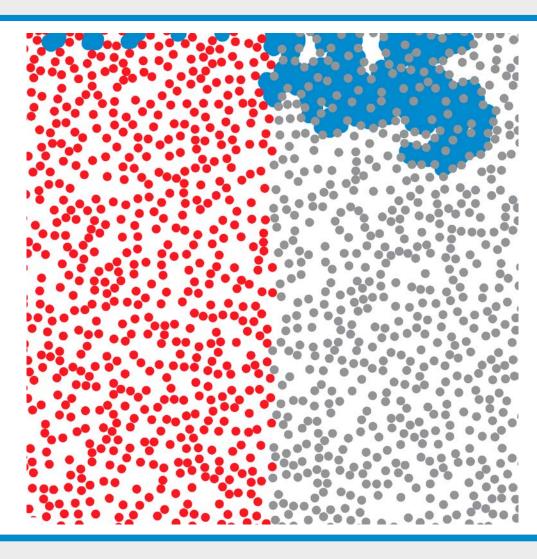
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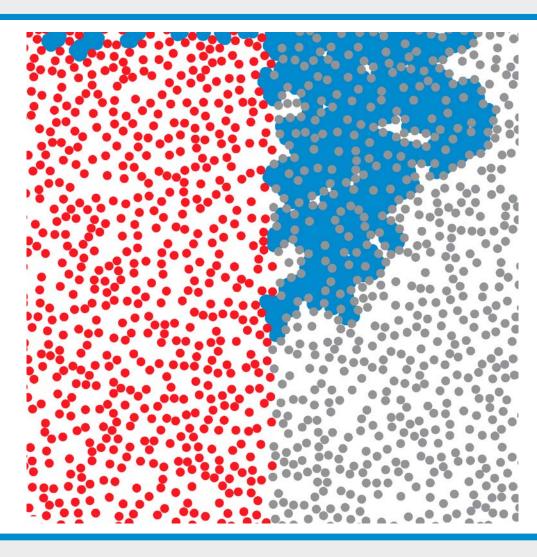
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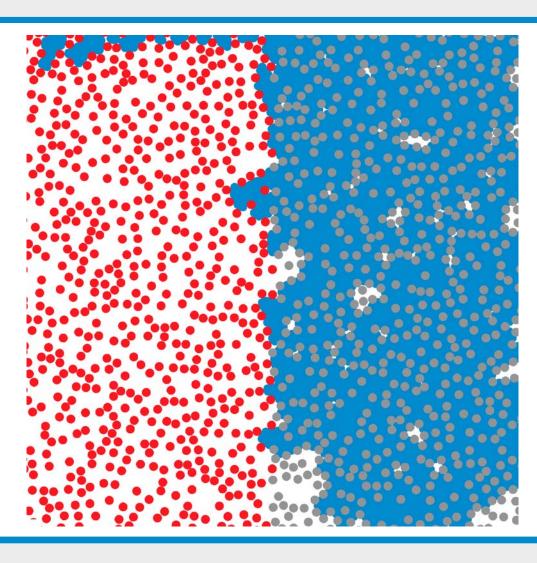


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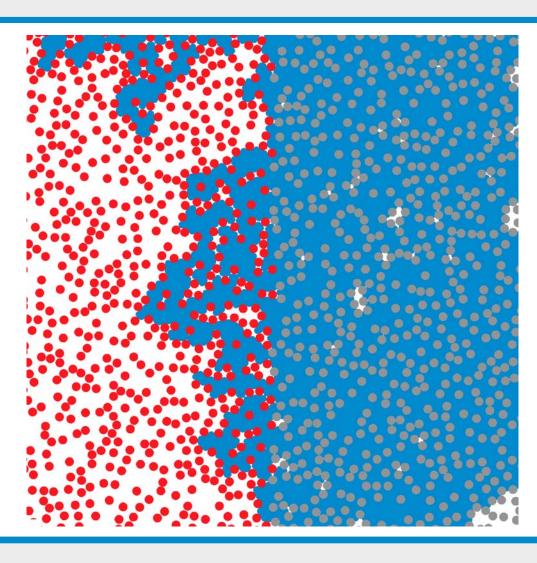


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Contact angle 0°

Contact angle 40°

Water (non-wetting)



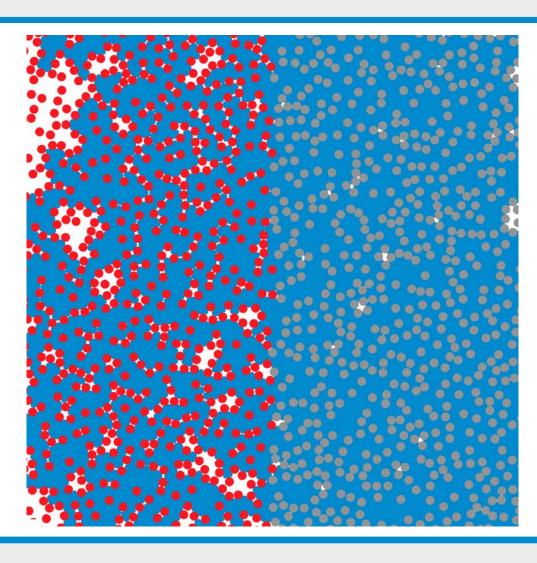


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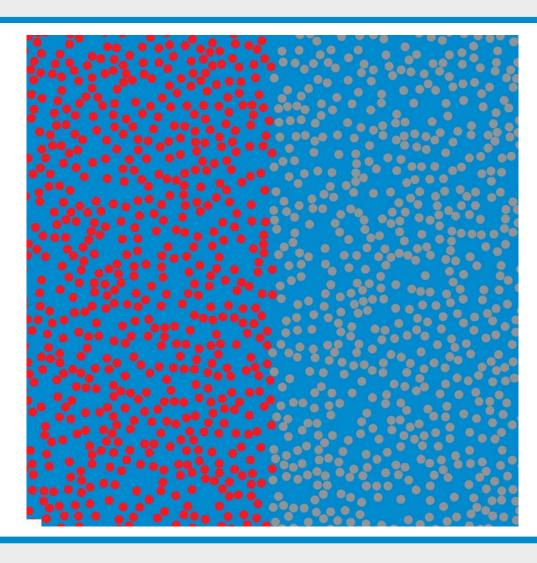
Water (non-wetting)





## 2D Example

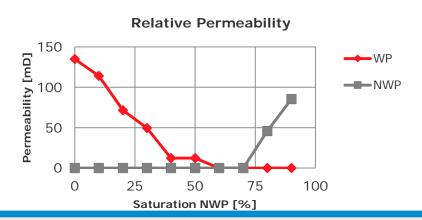
- Contact angle 0°
- Contact angle 40°
- Water (non-wetting)
- Air (wetting)

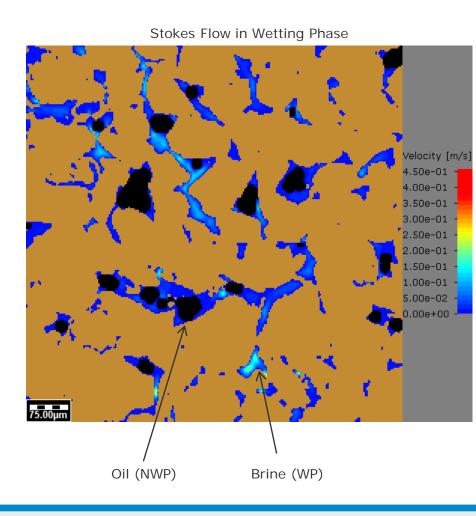




### Relative Permeability Basic Idea

- Choose
  - Saturation level and
  - Wetting model
- Find
  - Oil distribution (black) and
  - Brine distribution
- Solve Stokes equations in
  - Brine phase and treat oil phase as solid
  - Oil phase and treat brine phase as solid







### Relative Permeability



### Challenges

- DRP Parameter that is most expensive to compute
- Low saturation states are most expensive but results are the smallest

#### **Improvements**

- Speedup of solvers
- Restart of computations
  - Compute permeability from highest to lowest saturation state
  - Use result from previous computation to speed up the next one
- New stopping criterion
  - Relative difference to the permeability of the full saturated state





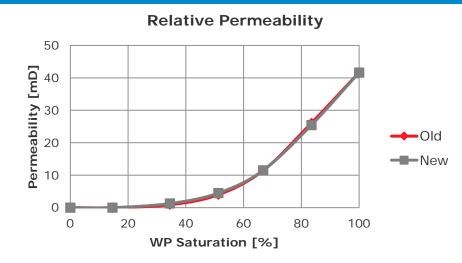
# Relative Permeability Example: Berea Sandstone

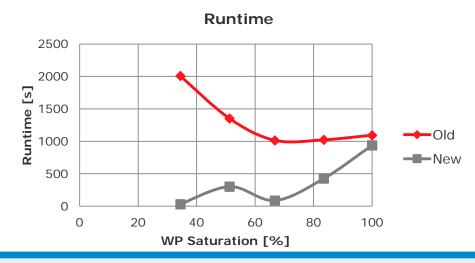
#### **Benchmark**

- Structure: Berea Sandstone
- Compute Relative Permeability for WP
- Compare old and improved computations



Segmented Berea Sandstone with 2563 voxels and 0.74 µm voxel length







Thank you for your attention!

