

The Influence of Variable Wettability on Mass Transport Properties of GDLs

Jürgen Becker, Christian Wagner, Sven Linden,
Andreas Wiegmann

ModVal Lausanne, 23.03.2016

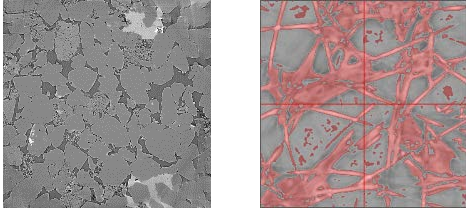
Who is Math2Market ?

- Math2Market GmbH was founded 2011 in Kaiserslautern.
- Spin-off of Fraunhofer Institute for Industrial Mathematics, ITWM.
- Today: 12 full-time, 6 part-time employees, turnover >2 Mio € / year
- Our product: GeoDict software
 - Sales
 - Development and Customization
 - Consulting



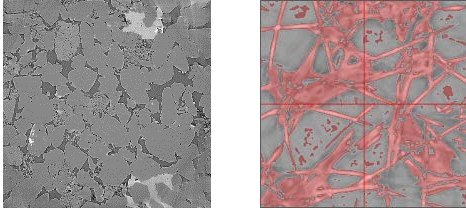
What can GeoDict do?

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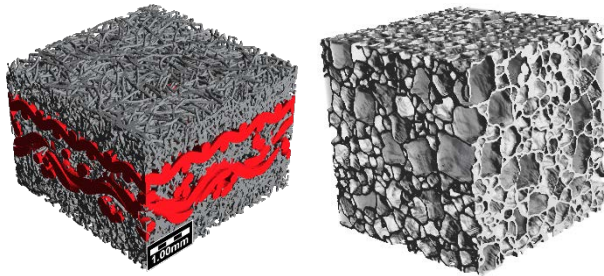


Import of CT Scans

What can GeoDict do?

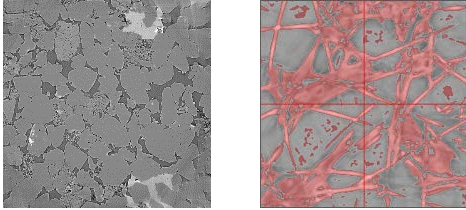


Import of CT Scans

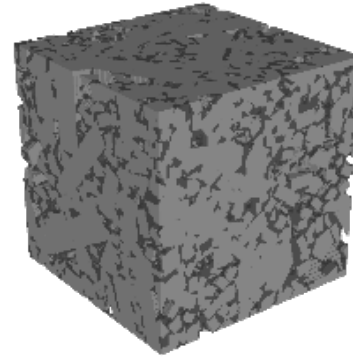


Create 3D Models of
Microstructures

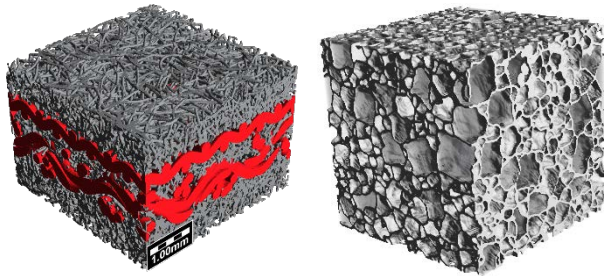
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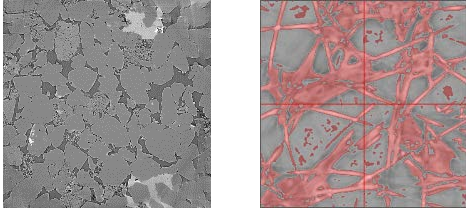


Geometric Analysis
of 3D Structures

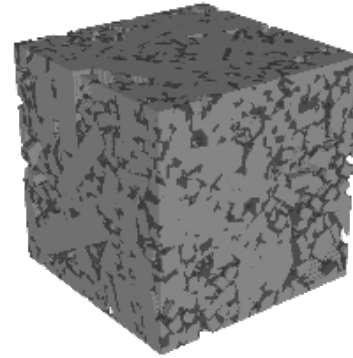


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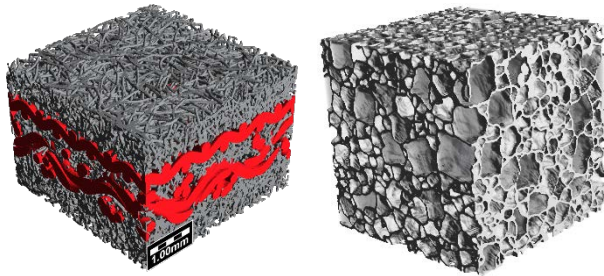
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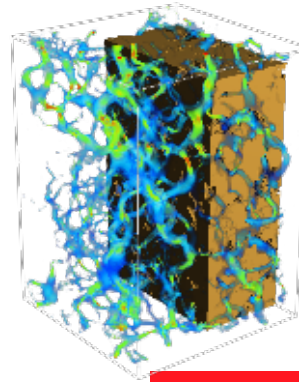
Import of CT Scans



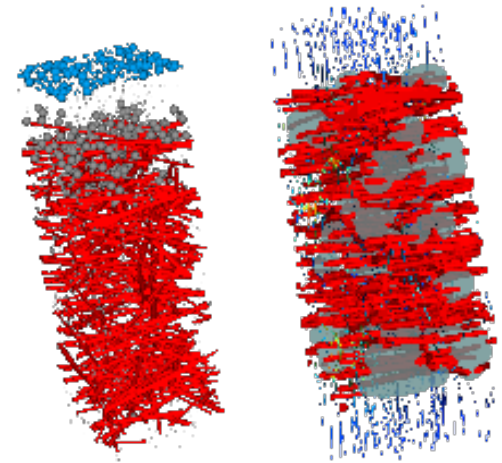
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Create 3D Models of
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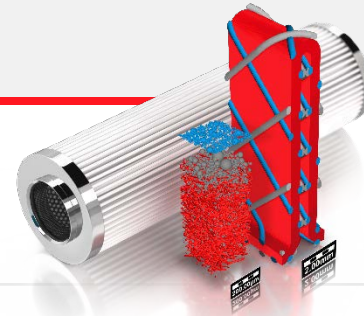
Simulate advection, diffusion
particle transport, stiffness



... with applications in:

Filtration

Mostly automotive,
filter media & filters



Personal Care

Wipes, Feminine
Care, Baby Care

Electrochemistry

Fuel cell media &
battery materials



Weaves and Paper

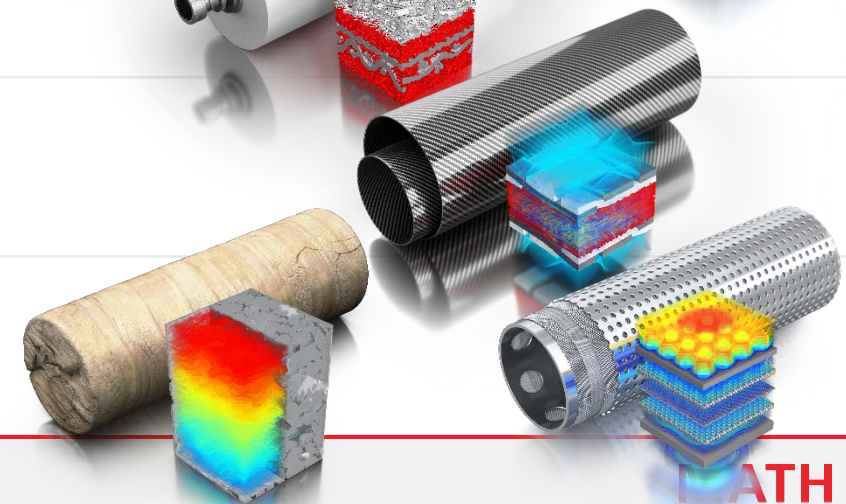
Paper forming and
dewatering, Metal
Wire Mesh

Composites

Mostly automotive,
lightweight materials

Oil and Gas

Digital rock physics,
digital sand control



GEO DICT

The Influence of Variable Wettability on Mass Transport Properties of GDLs

Overview:

1. 3D GDL model and compression
2. Computing permeability
3. Capillary pressure and saturation with variable wettability
4. Effect on relative permeability

3D GDL Model and Compression

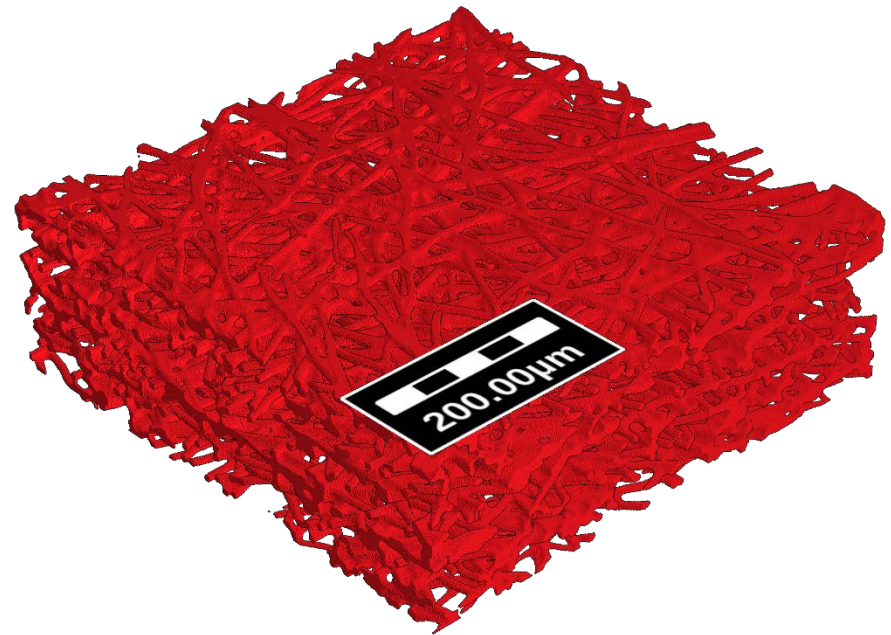
Structure Model

GDL:

- Carbon fibers, 7 μm diameter
- 20 wt% binder
- 200 μm thickness

Model

- 1 μm resolution
- Voxel grid
- $600 \times 600 \times 200 = 72$ Mio. cells
- Stochastic process



Compression Simulation

Fibers: linear elastic, transverse isotropic

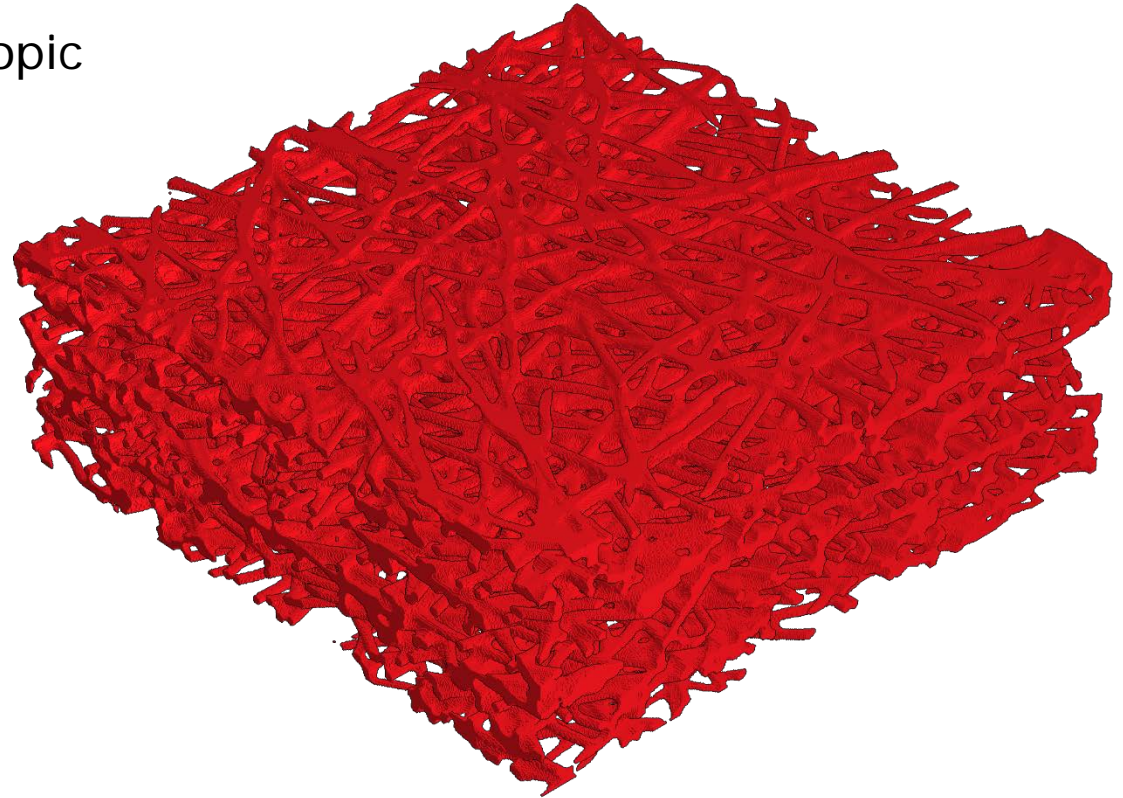
Binder: linear elastic, isotropic

Solver:

 **FeelMath**

 **Fraunhofer**
ITWM

Runtime: 1h 17 min (8x)



Compression

0

0.05

0.1

0.15

0.2

0.25

Compression Simulation

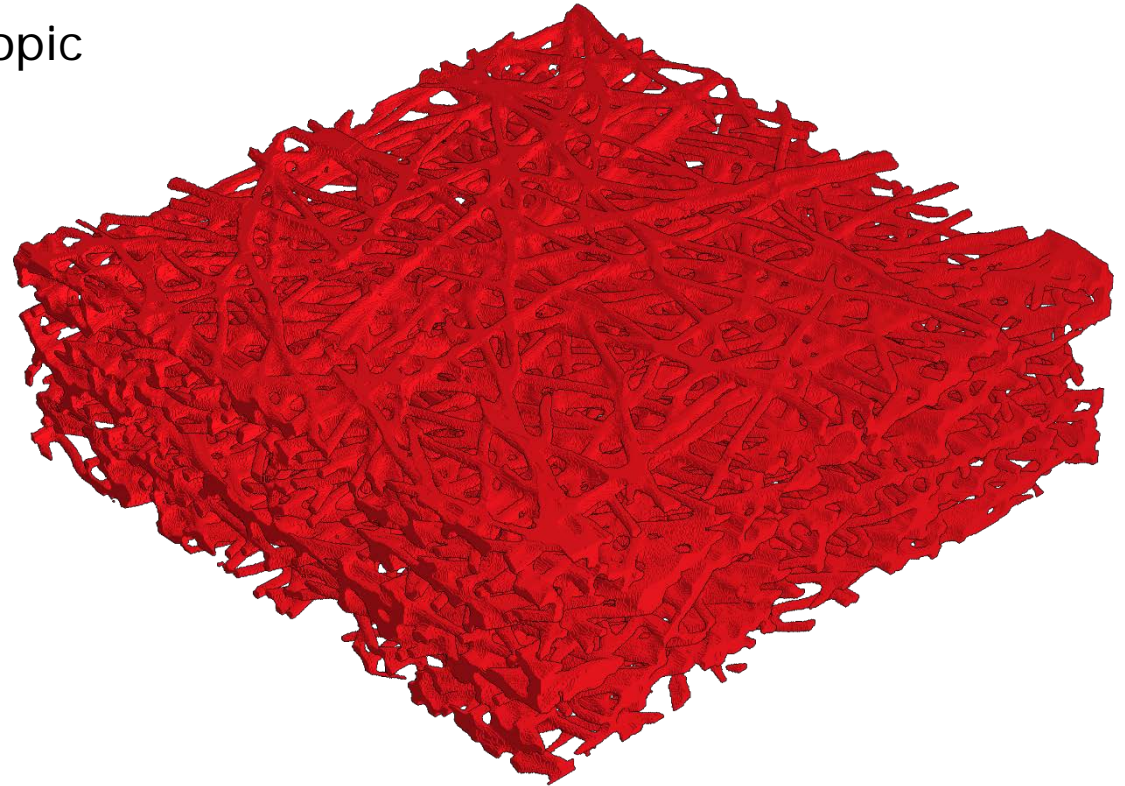
Fibers: linear elastic, transverse isotropic

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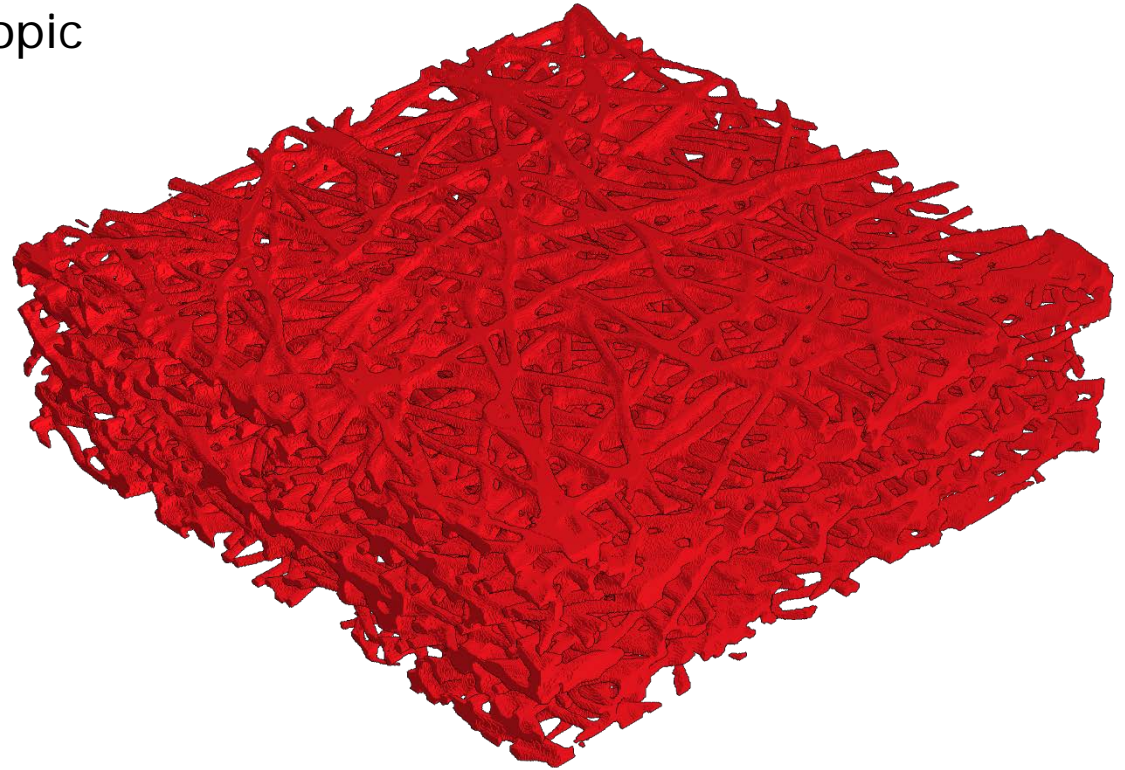
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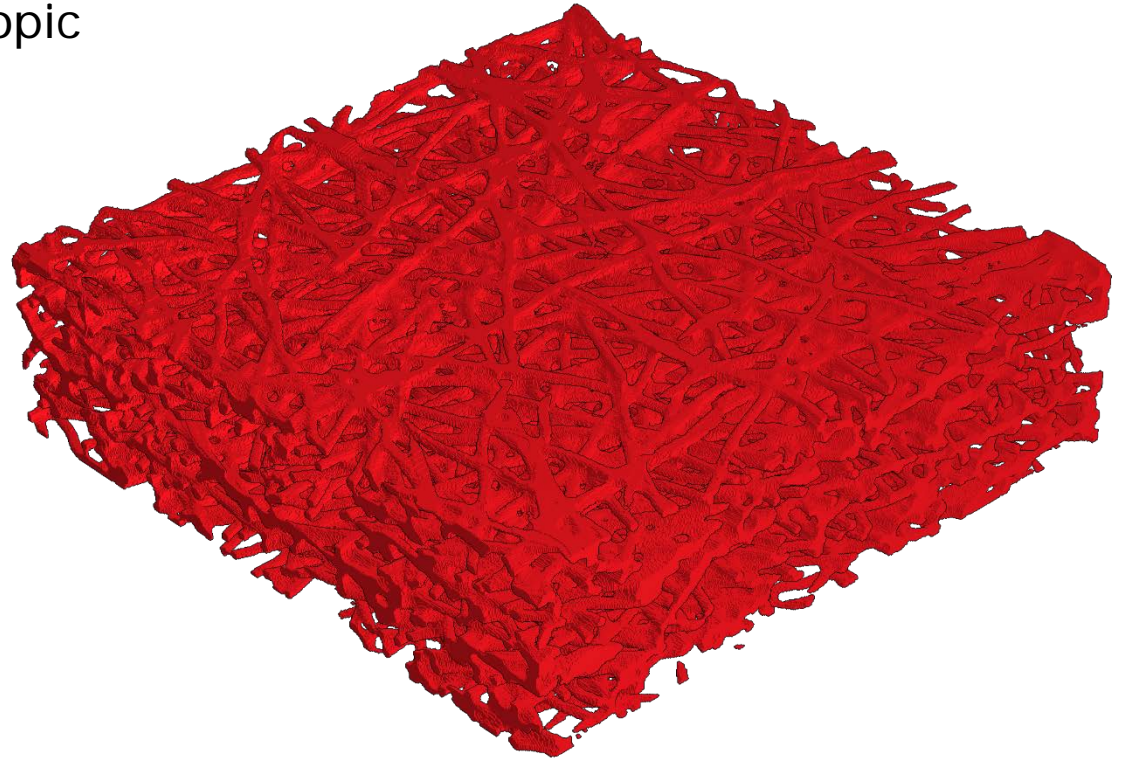
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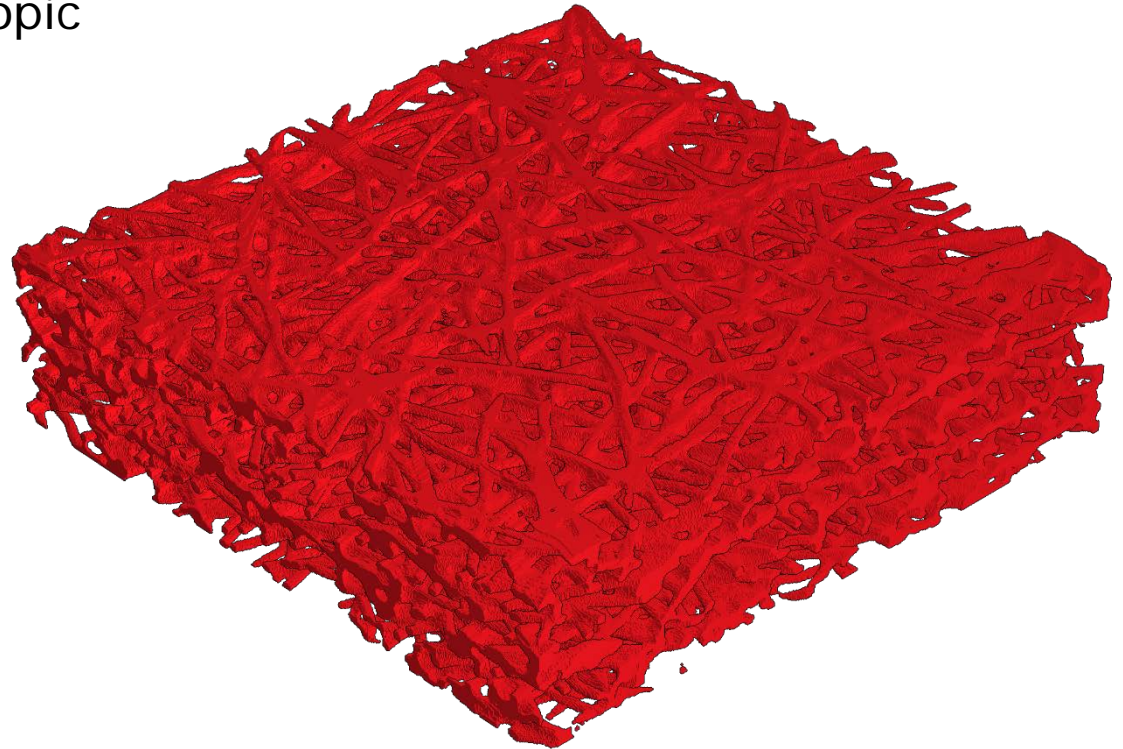
Fibers: linear elastic, transverse isotropic

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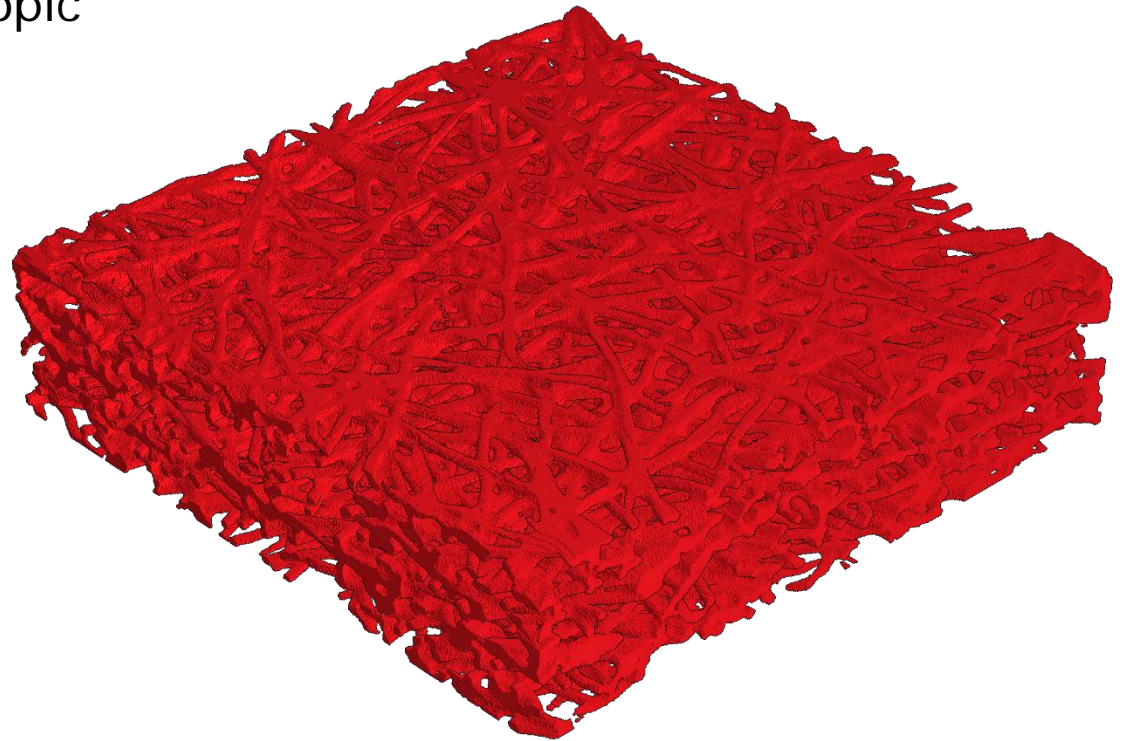
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Solver:



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Computing Permeability

Flow solver finds interstitial flow field \mathbf{u} .

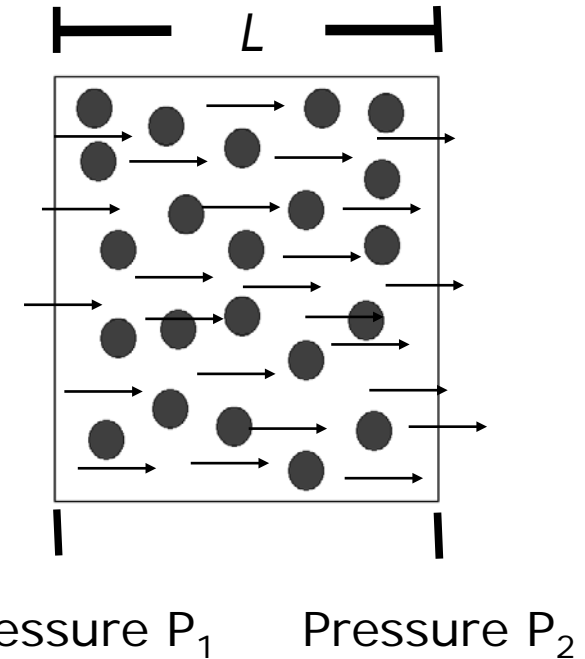
$\bar{\mathbf{u}}$: Average (superficial) flow velocity

P_1 : Pressure average over inflow plain

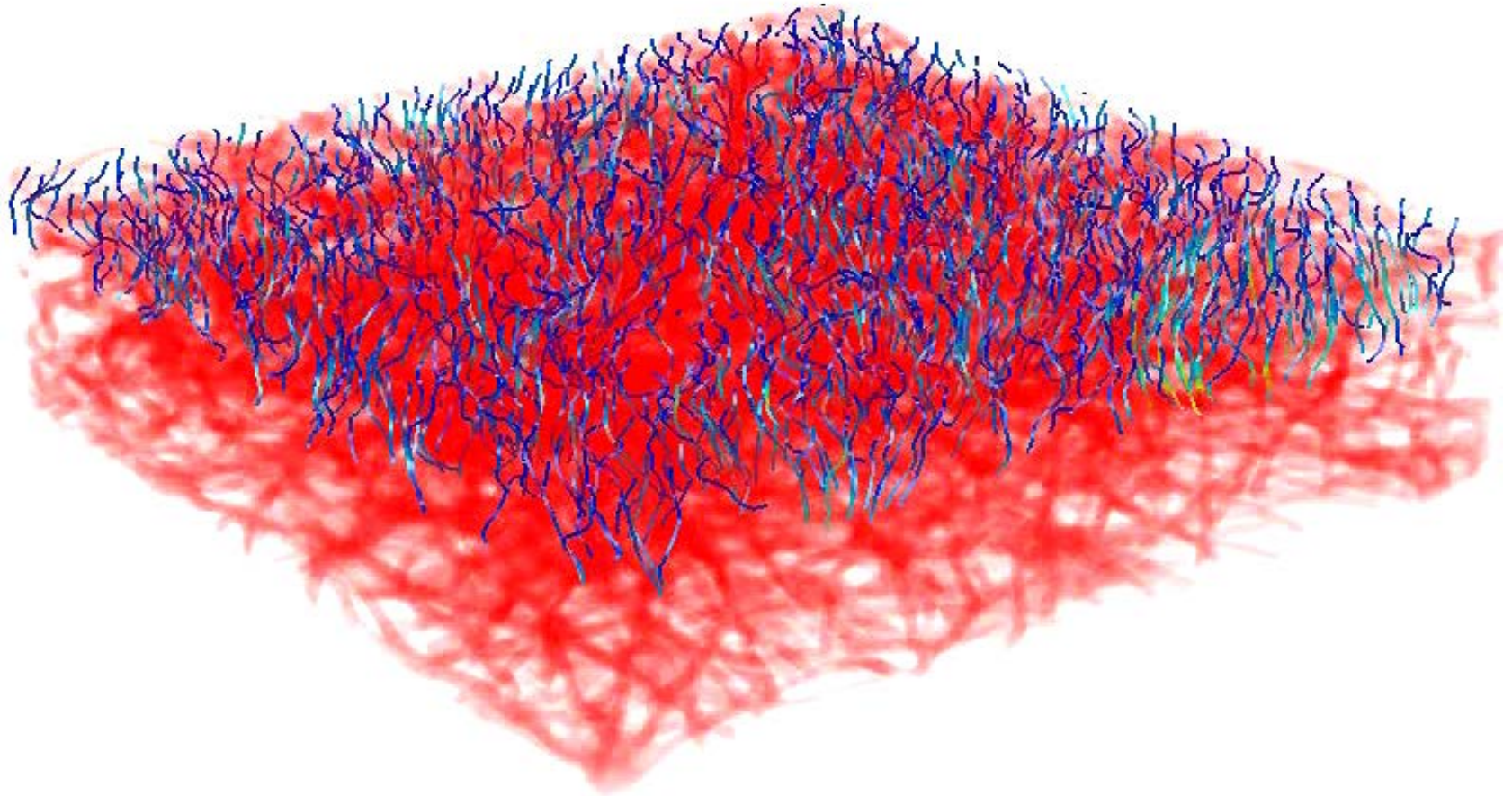
P_2 : Pressure average over outflow plain

\mathbf{K} : Permeability tensor

$$\text{Darcy-Law: } \bar{\mathbf{u}} = -\frac{\mathbf{K}}{\mu} \frac{(P_2 - P_1)}{L}$$

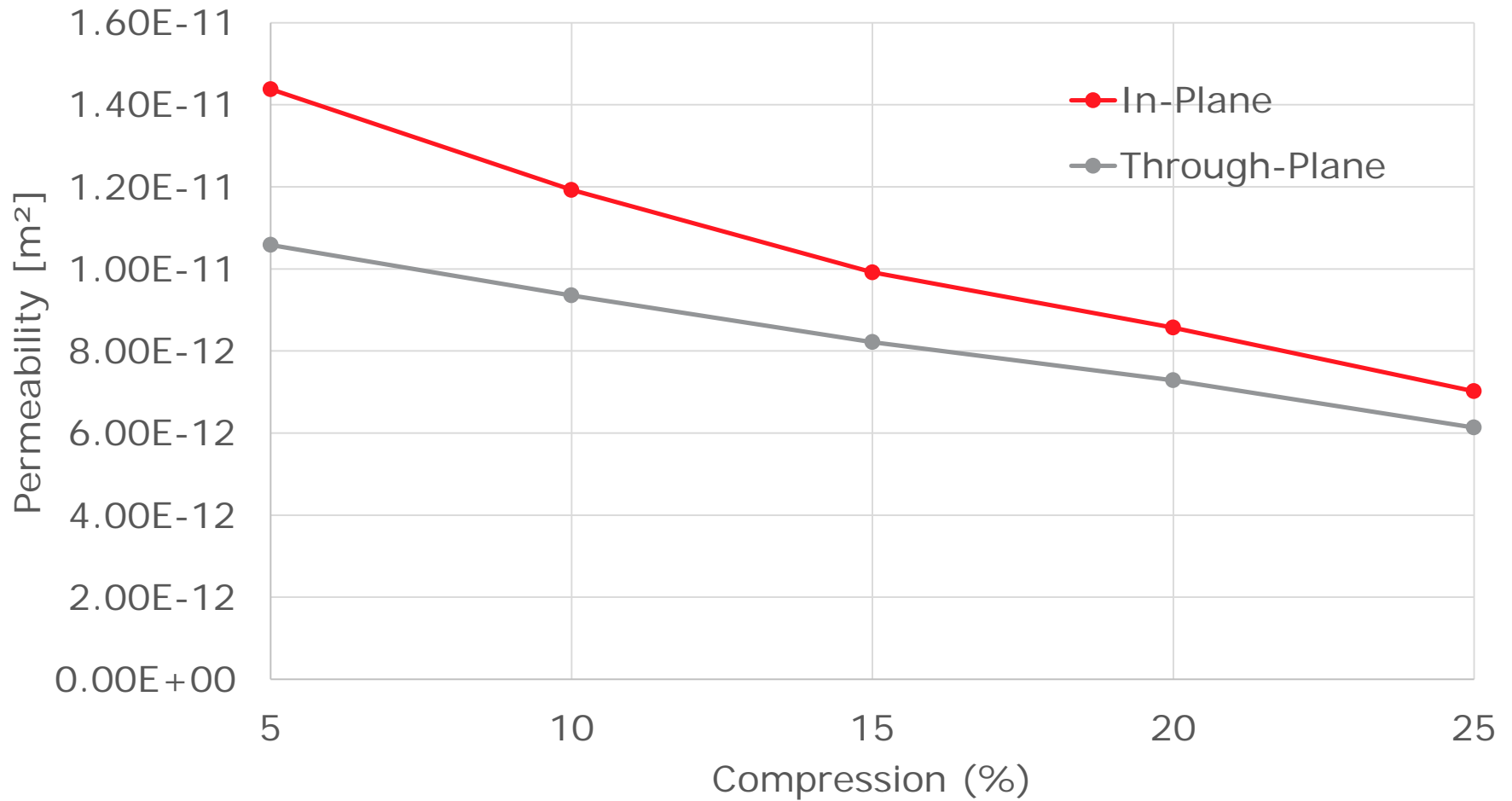


Flow Simulation



Solver runtime (12x parallel): 5 min 41 s

Compression and Permeability



Capillary Pressure and Saturation with Variable Wettability

Capillary Pressure

When does the gas enter a cylindrical capillary?

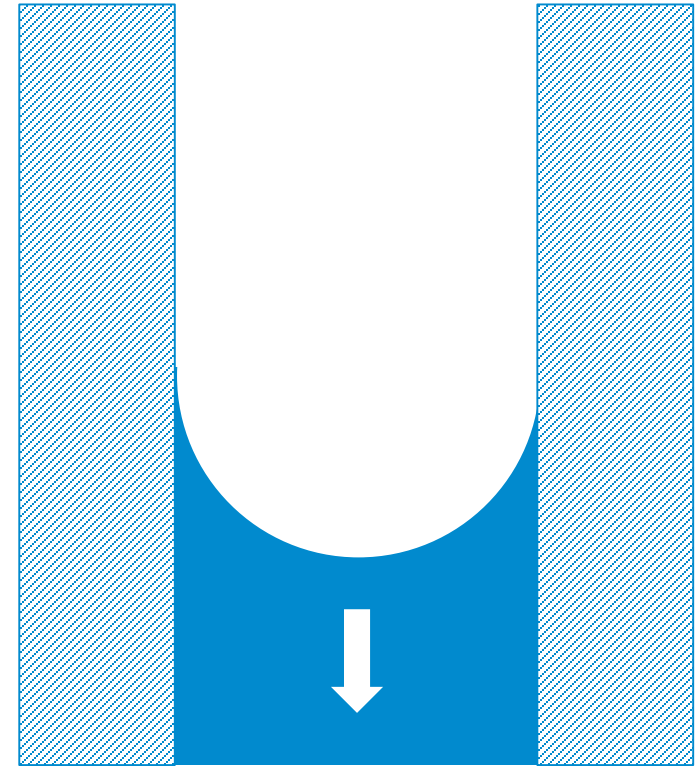
$$p = \frac{4 \sigma}{d}$$

p differential pressure

d pore diameter

σ surface tension

complete wetting $\beta = 0$



Capillary Pressure

When does the gas enter a cylindrical capillary?

$$p = \frac{4 \sigma}{d} \cos \beta$$

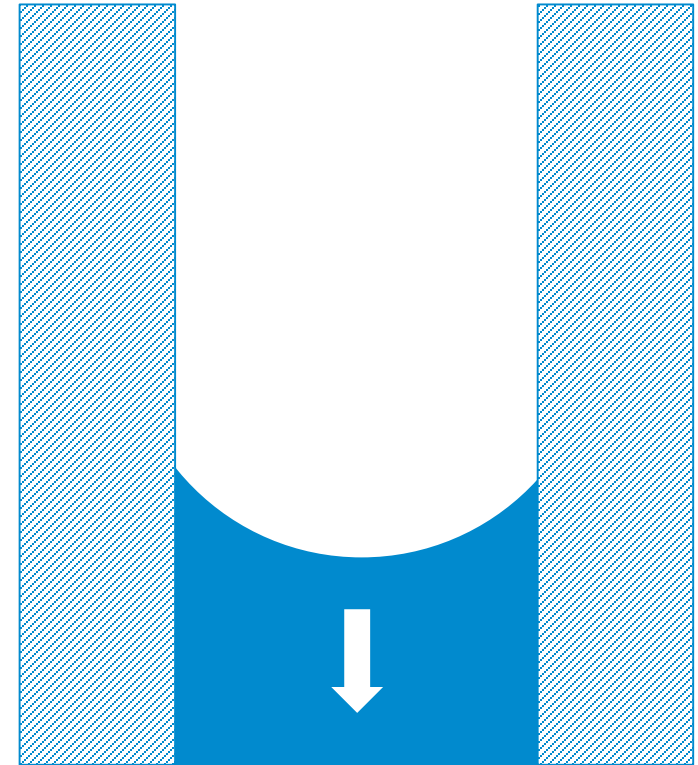
p differential pressure

d pore diameter

σ surface tension

β contact angle

partial wetting $0^\circ < \beta < 90^\circ$



Can we have variable contact angles?

Idea (Schulz et al, 2014)

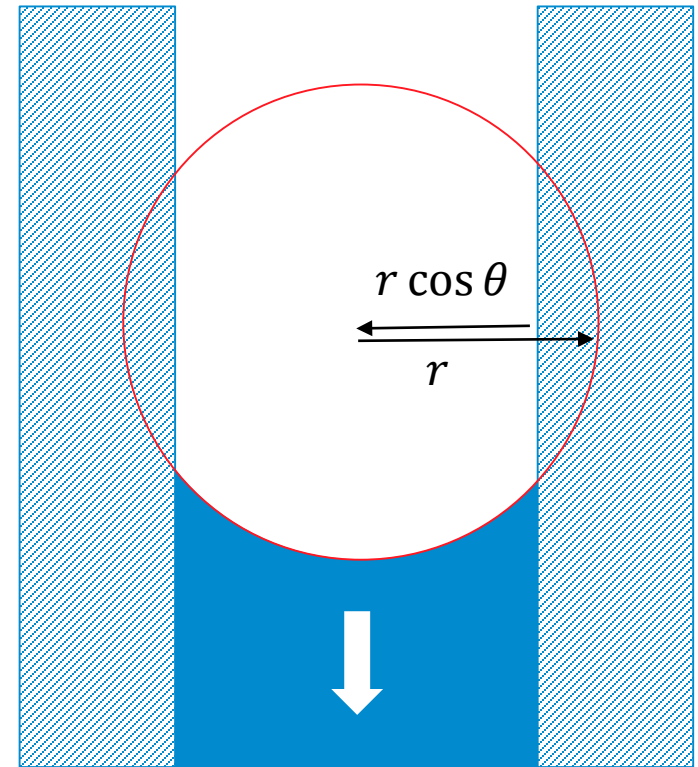
- dilate by $r \cos \theta$
- erode by r

Result: contact angle θ on pore wall

Young-Laplace: $p = \frac{2 \sigma}{r}$

r : sphere radius (\neq pore radius)

V.P. Schulz, E. A. Wargo, E. Kumbur, Pore-Morphology-Based Simulation of Drainage in Porous Media Featuring a Locally Variable Contact Angle, [Transport in Porous Media](#), 2014.

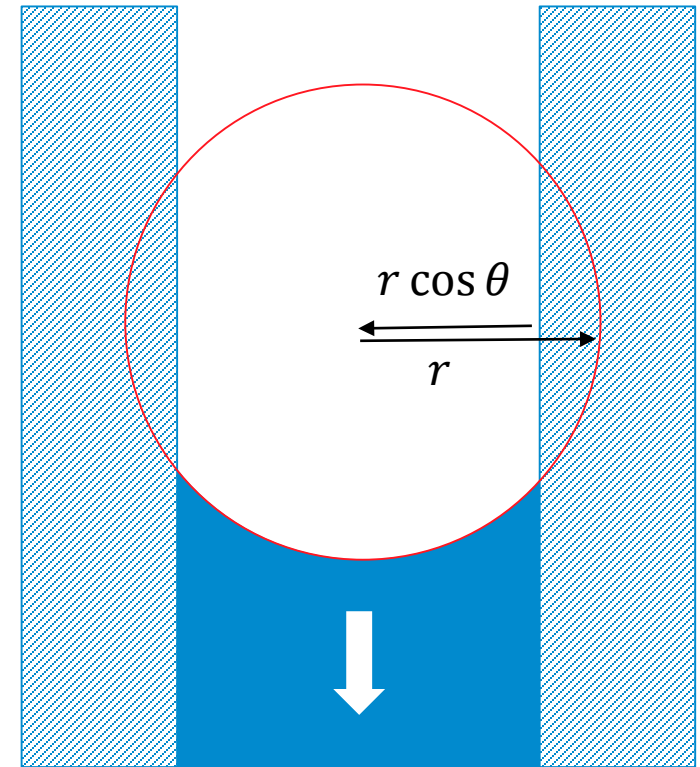


Can we have variable contact angles?





Restriction on possible contact angles:

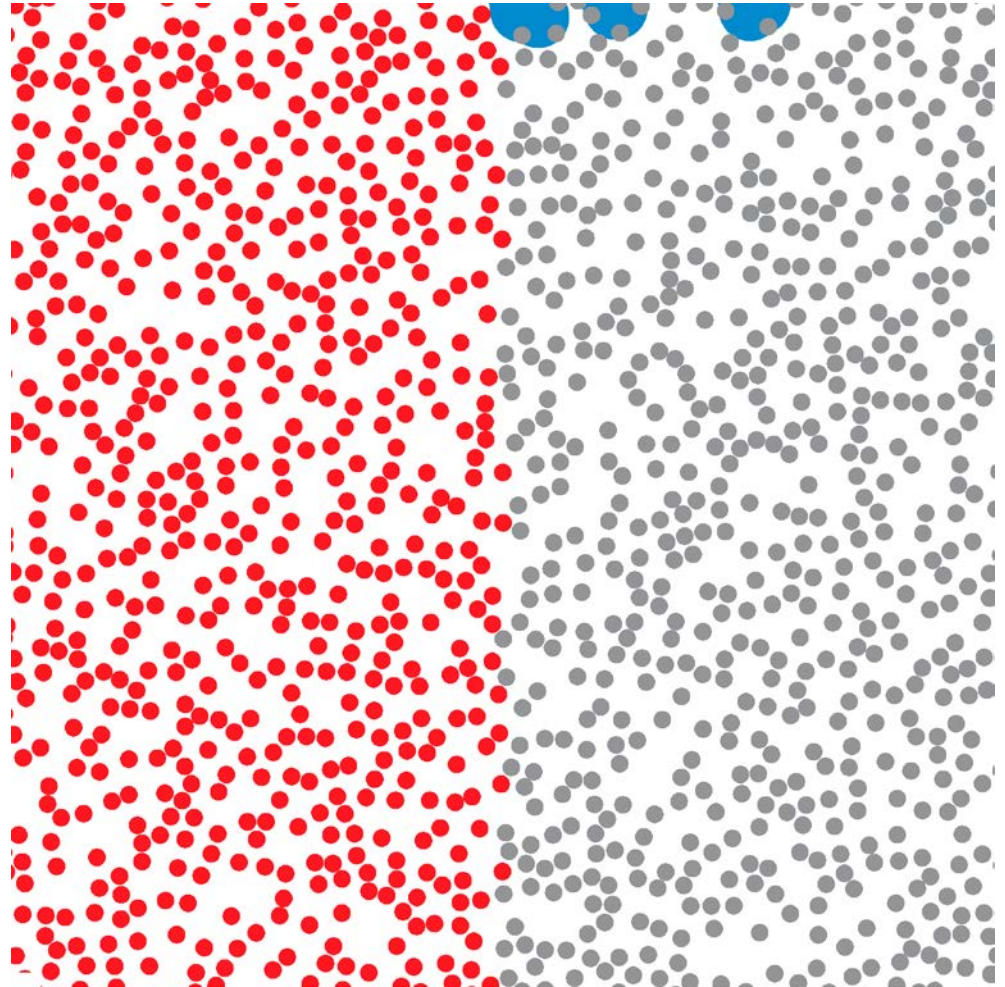
- If the difference between $r \cos \theta$ and r is larger than the fiber diameter (or wall thickness), the method produces artifacts.
⇒ Contact angles should not be too close to 90°
- No mixed (hydrophobic-hydrophilic) wettability possible.

V.P. Schulz, E. A. Wargo, E. Kumbur, *Pore-Morphology-Based Simulation of Drainage in Porous Media Featuring a Locally Variable Contact Angle*, [*Transport in Porous Media*](#), 2014.







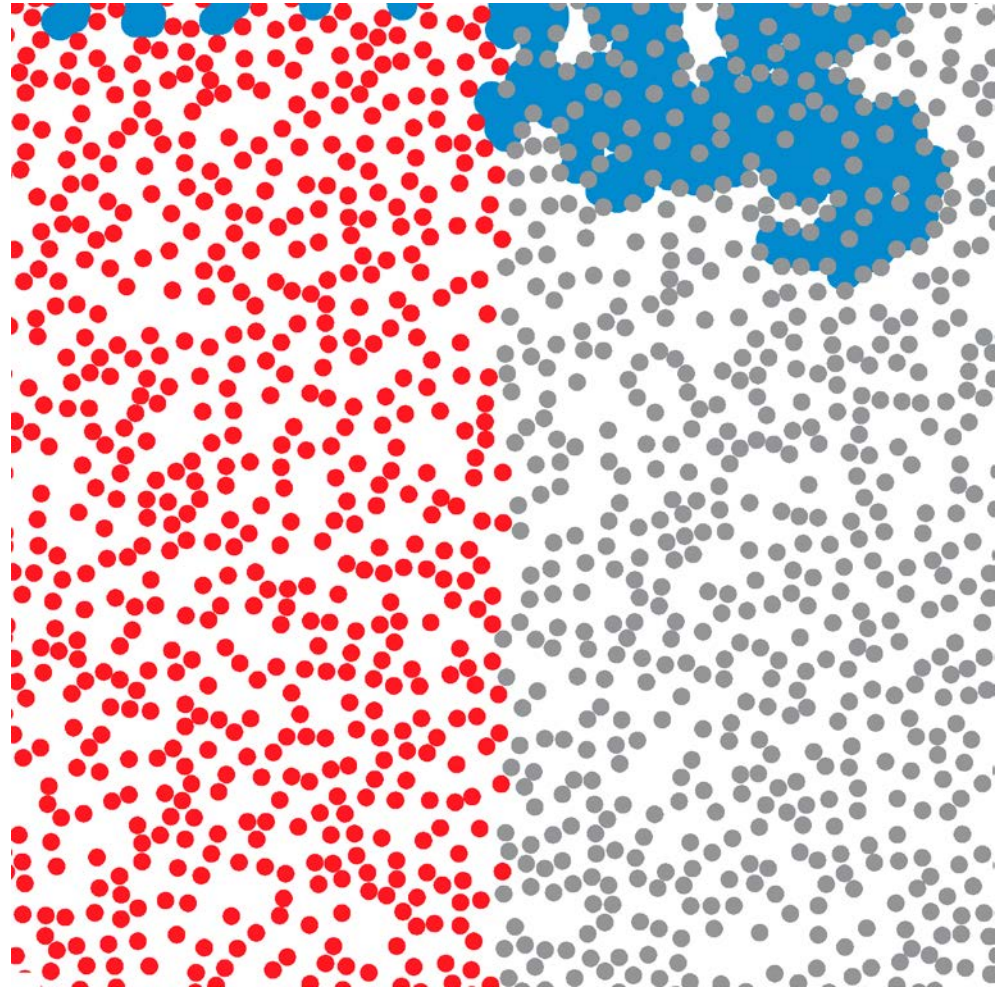
2D Example

-  Contact angle 0°
-  Contact angle 40°
-  Water (non-wetting)
-  Air (wetting)







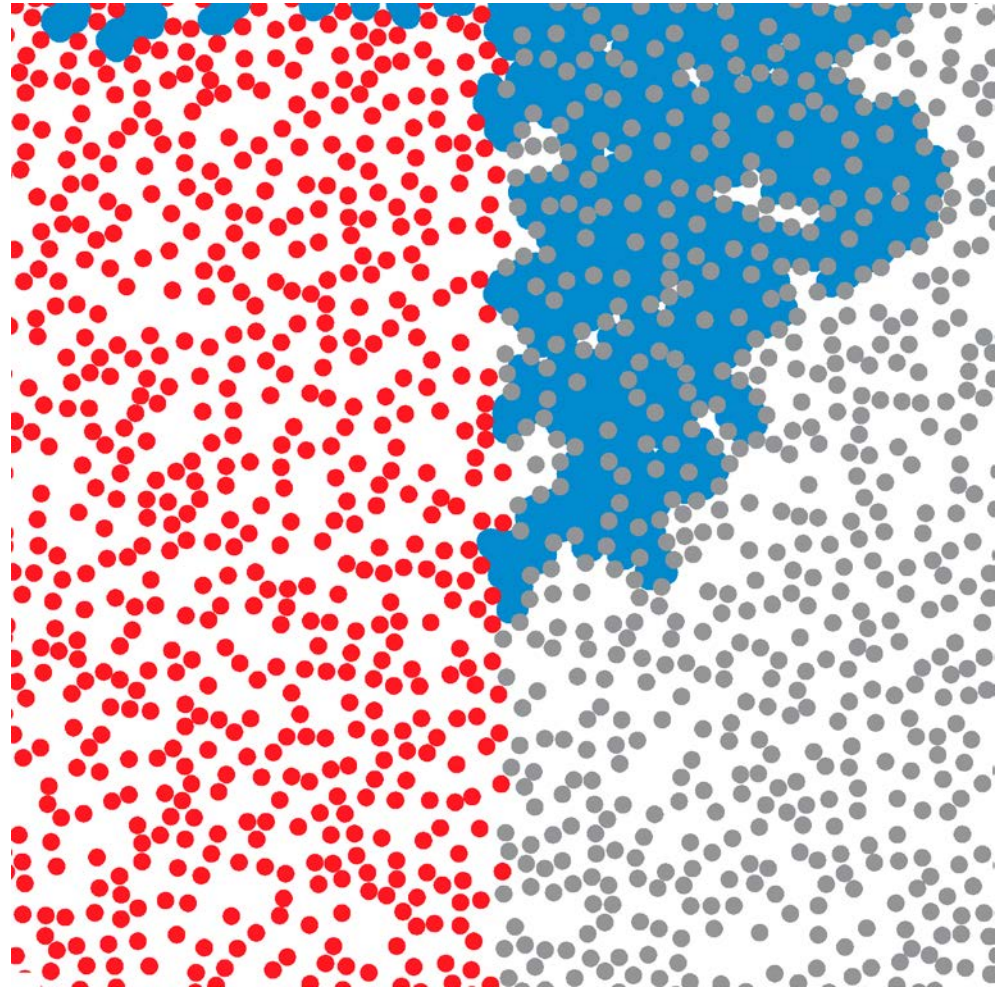
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





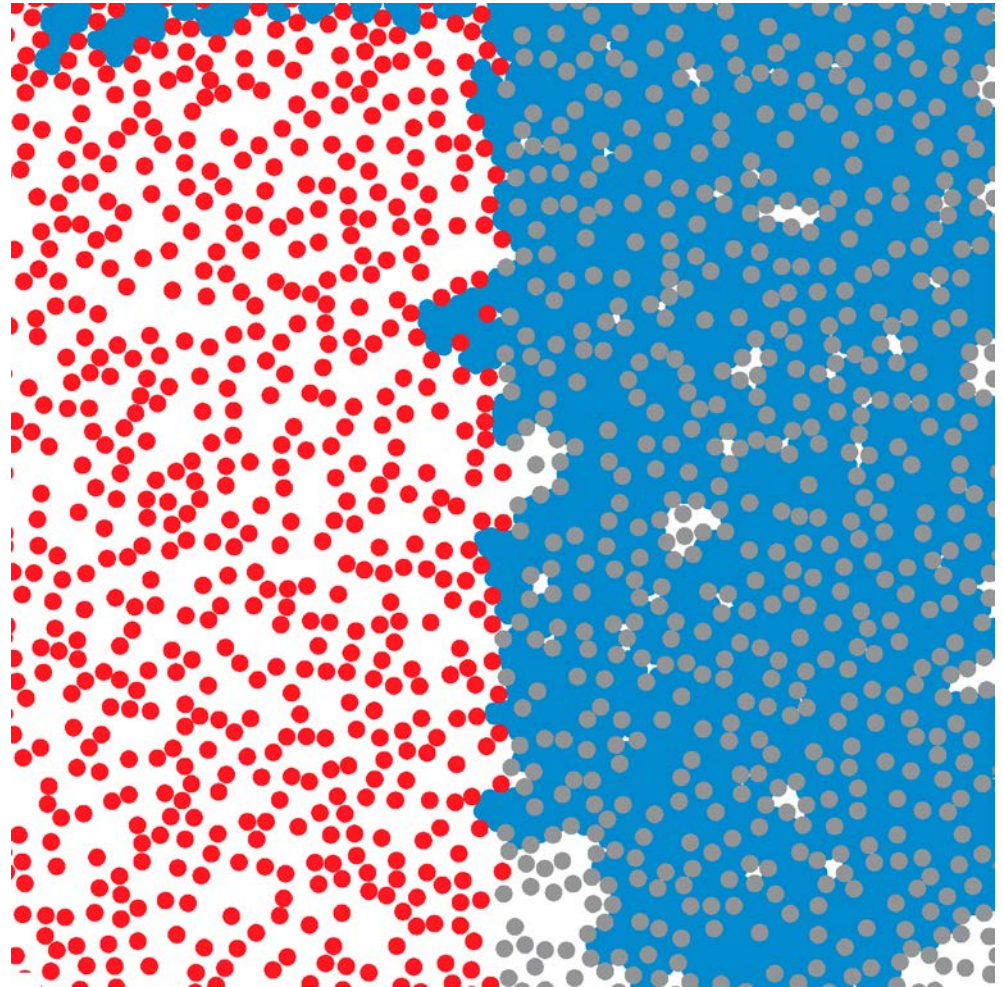
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





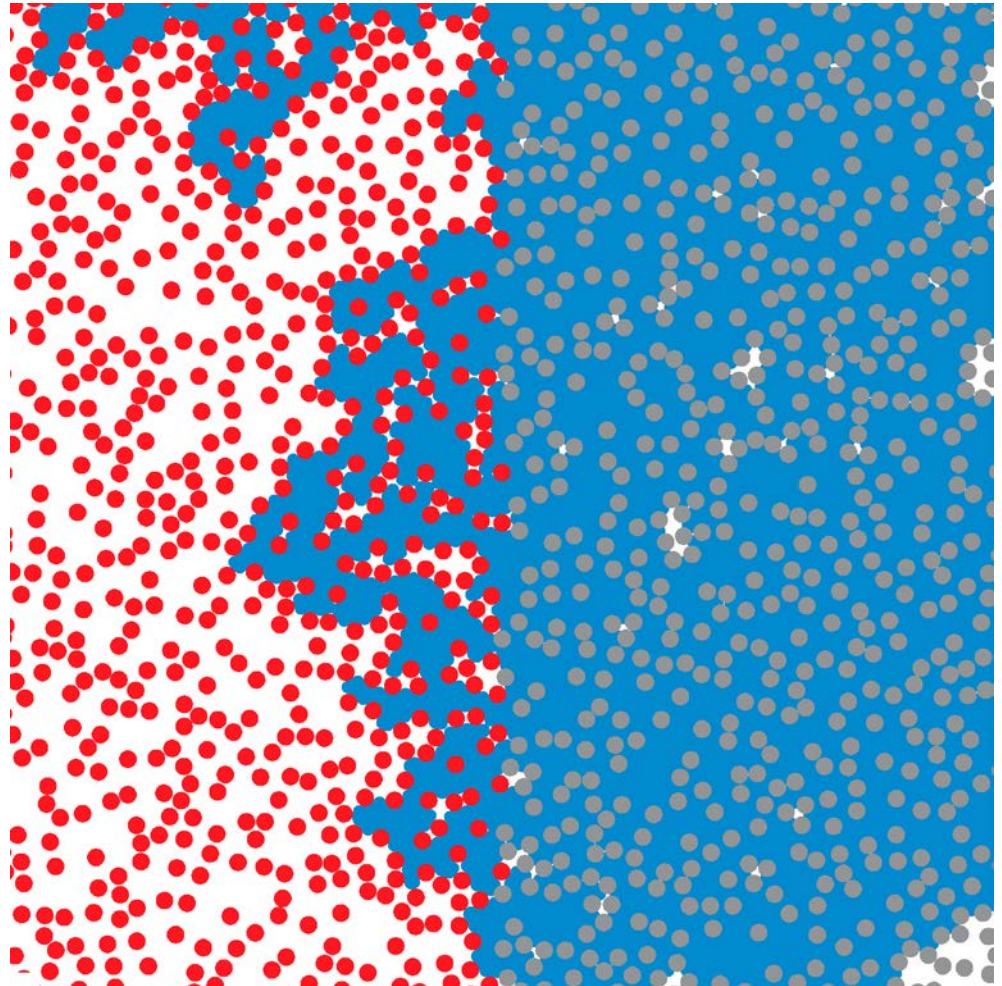
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





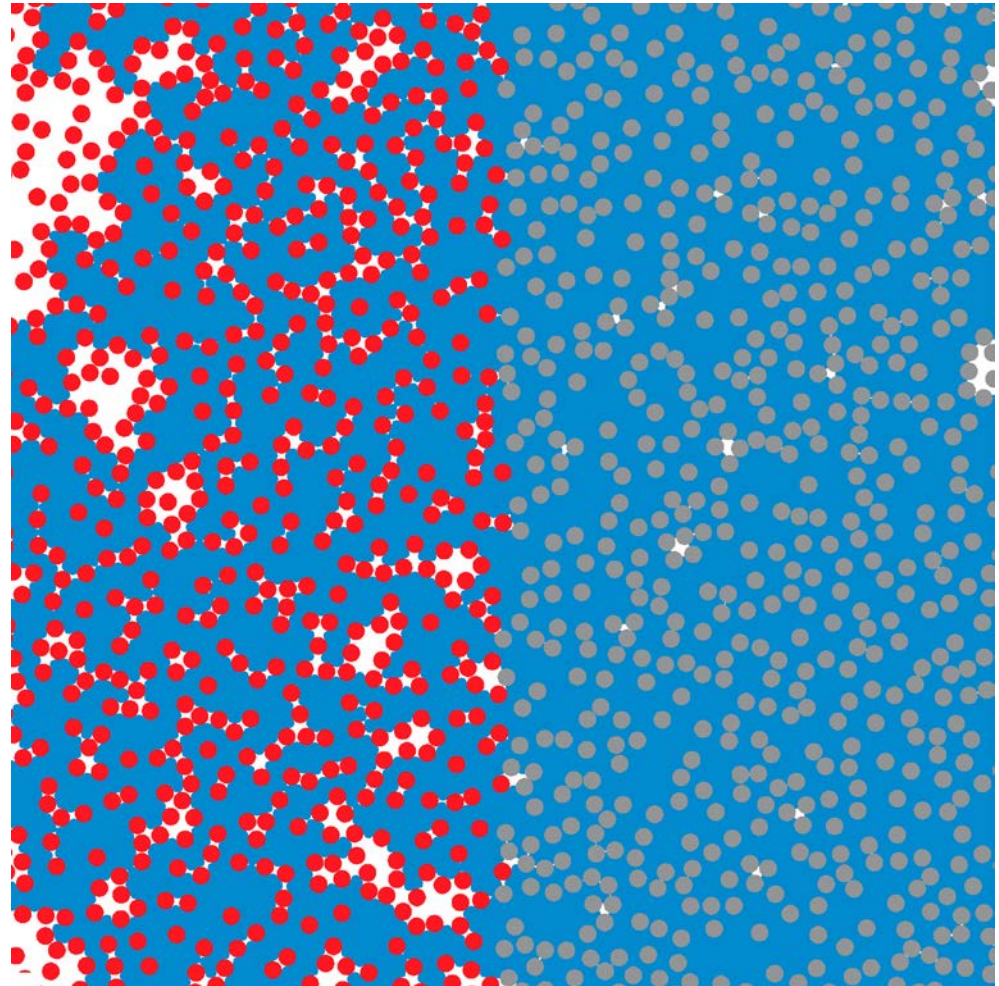
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





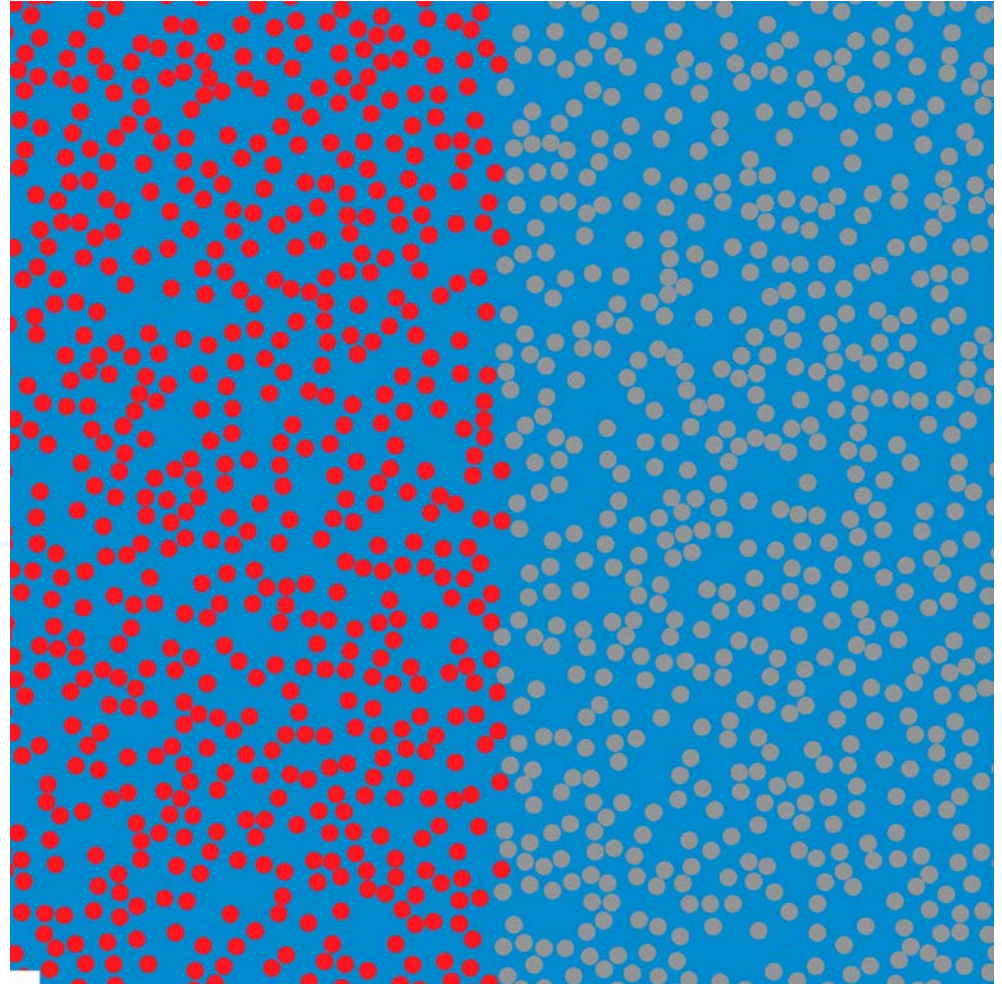
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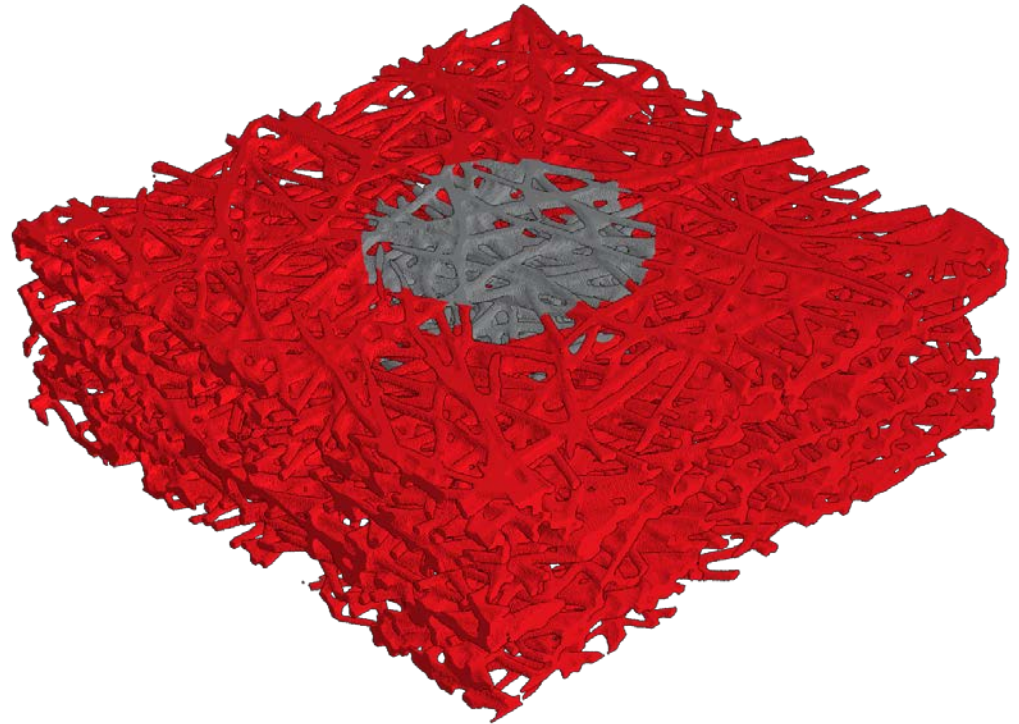
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Structure with Variable Wettability

- Marked a cylinder as area with higher wettability

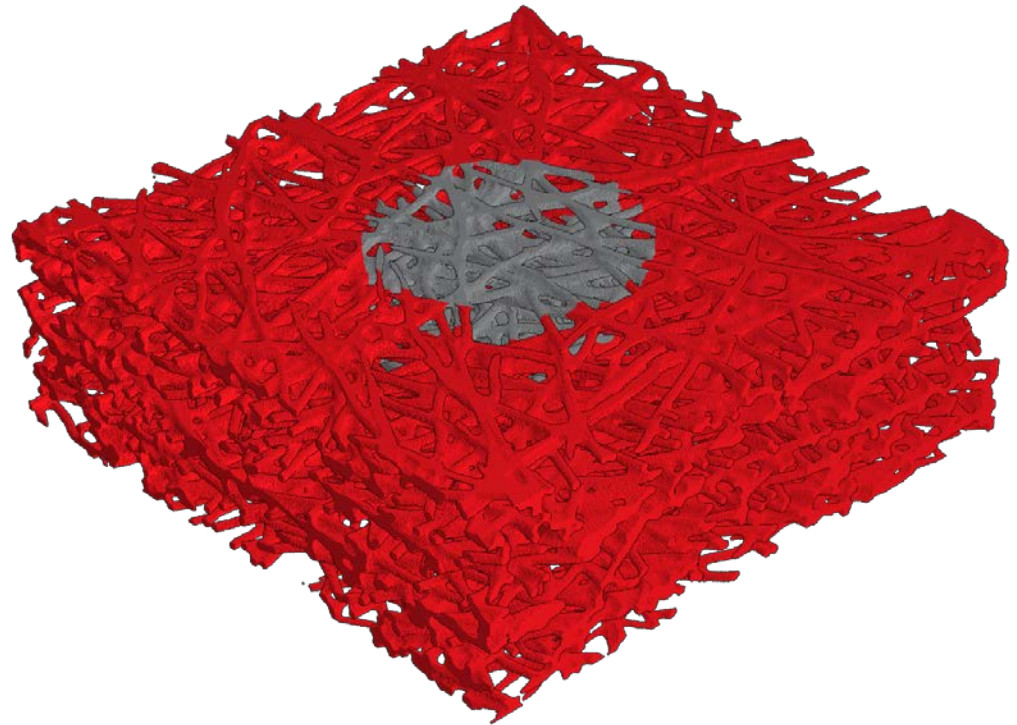


Structure with Variable Wettability

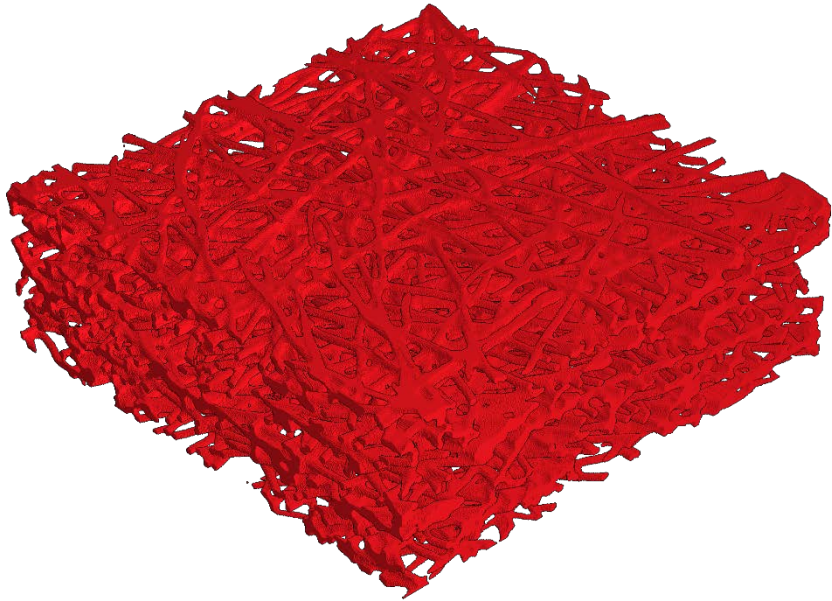
- Marked a cylinder as area with higher wettability

Other options:

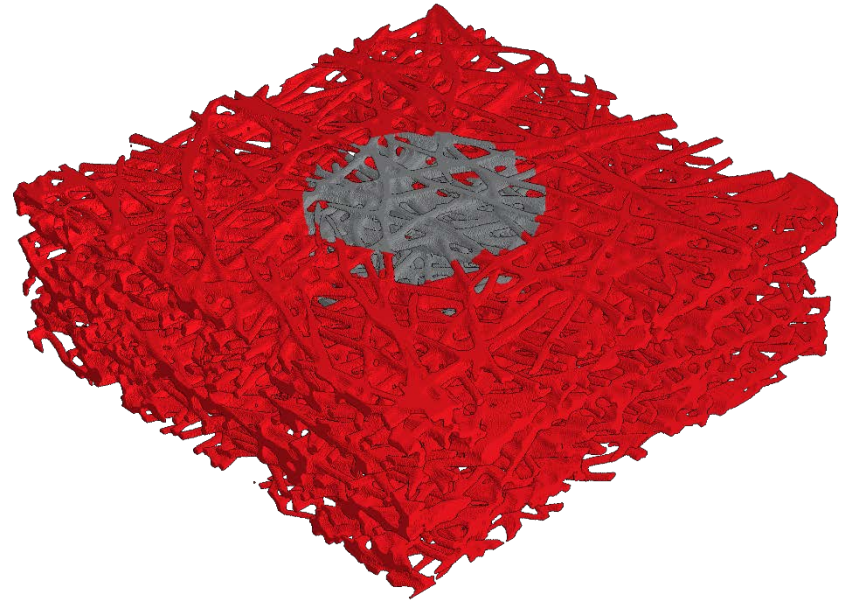
- distinguish between binder and fibers
- mark individual fibers
- ...



GDL Models



Constant Contact Angle



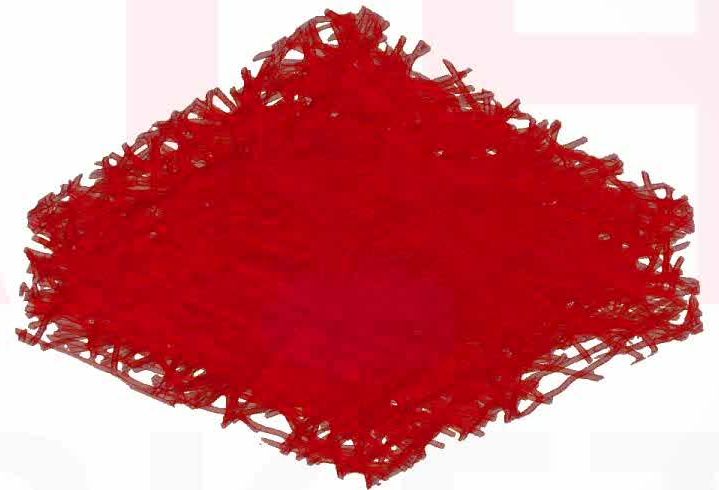
Two Different Contact Angles

Water Entering into the GDL

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Top View



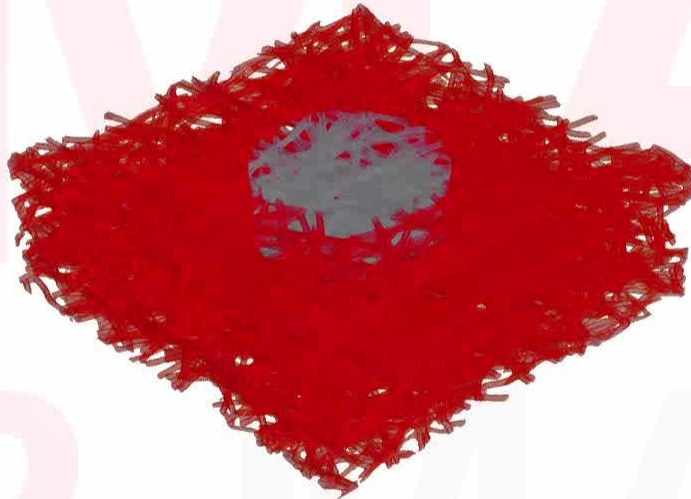
Bottom View

SatuDict Simulation with constant contact angle; uncompressed

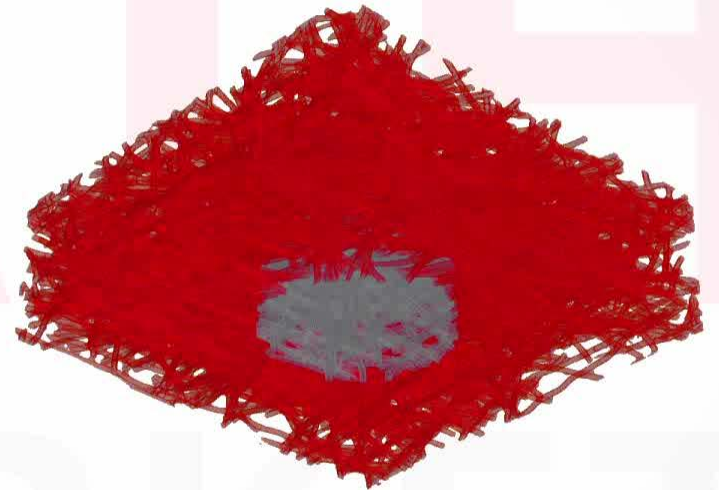
GEO DICT

Water Entering into the GDL

GEO DICT



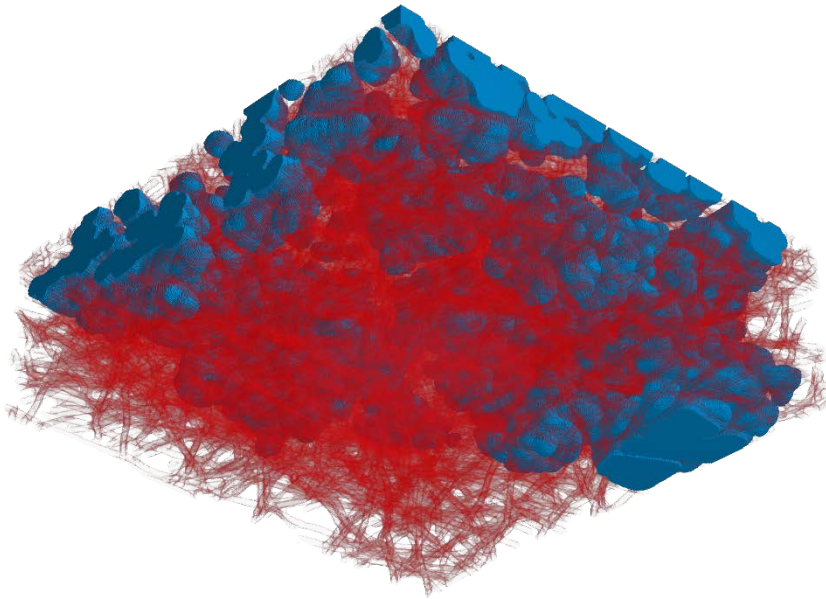
Top View



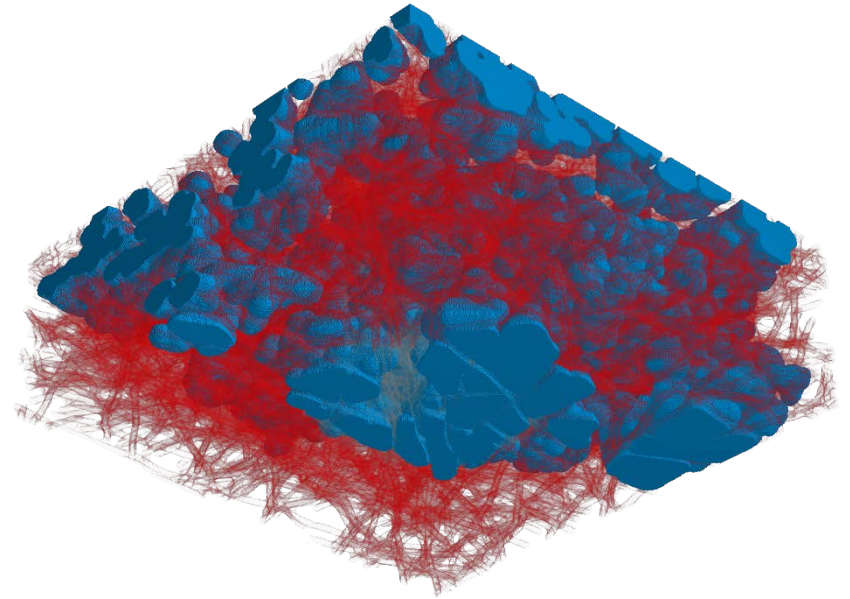
Bottom View

SatuDict Simulation with two different contact angles; uncompressed

Comparison



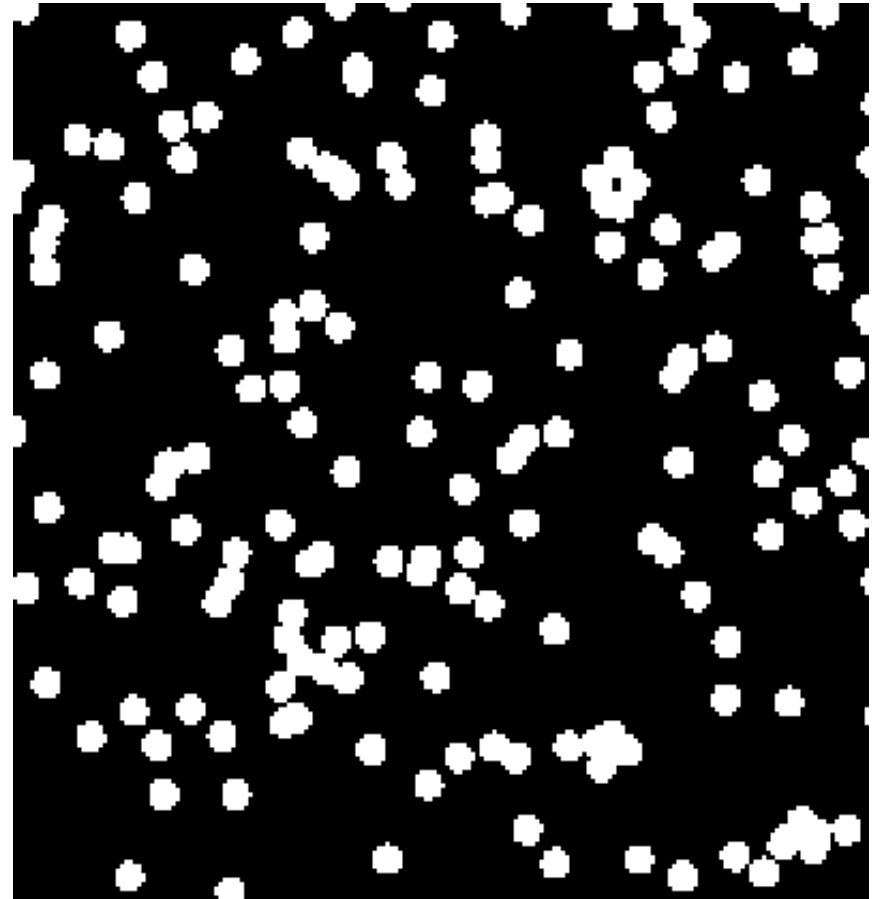
Constant Contact Angle



Two Different Contact Angles

Relative Permeability

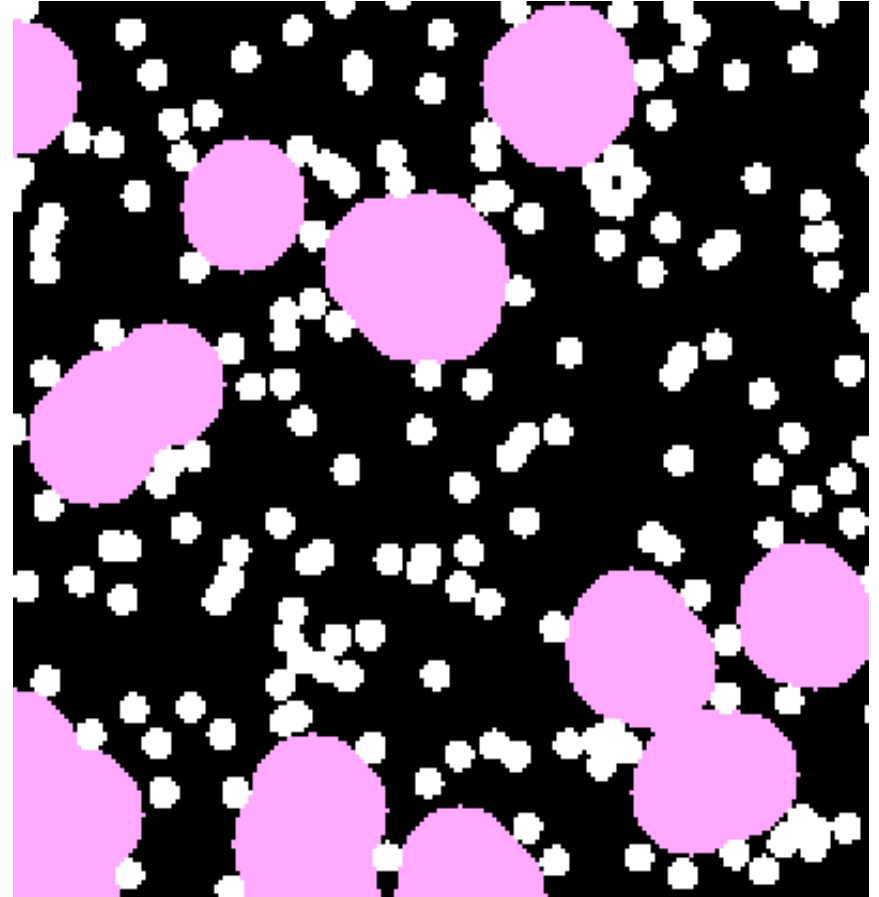
Saturation Dependent Permeability



Saturation Dependent Permeability

For each saturation:

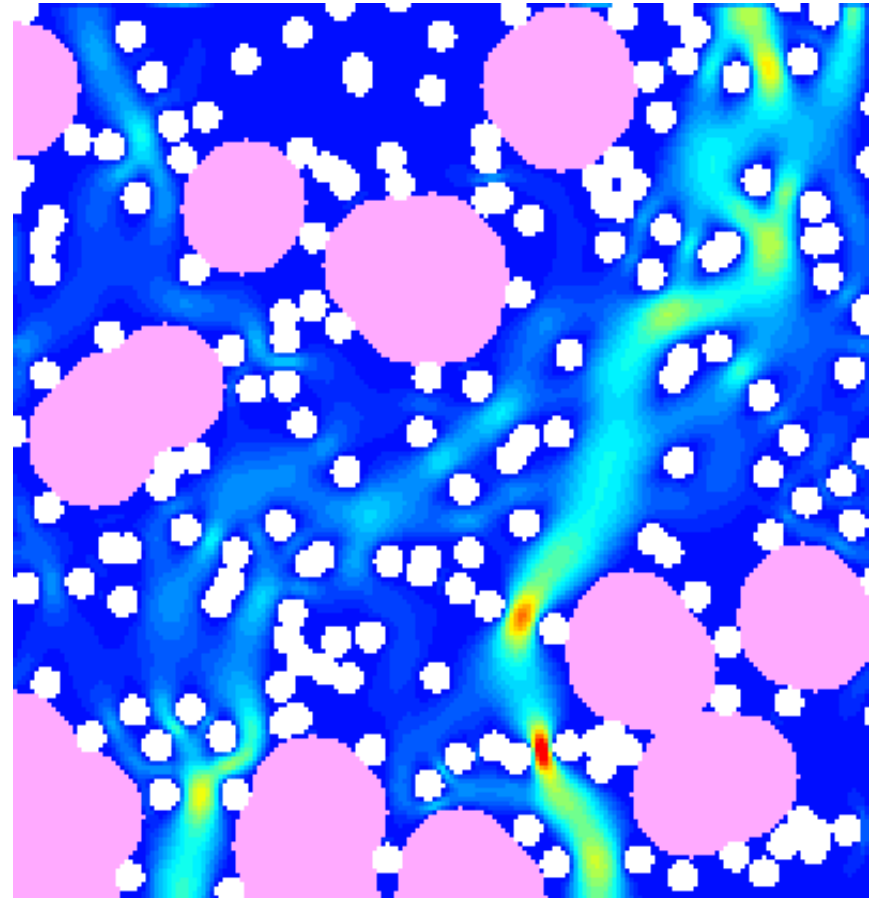
1. Determine phase distribution



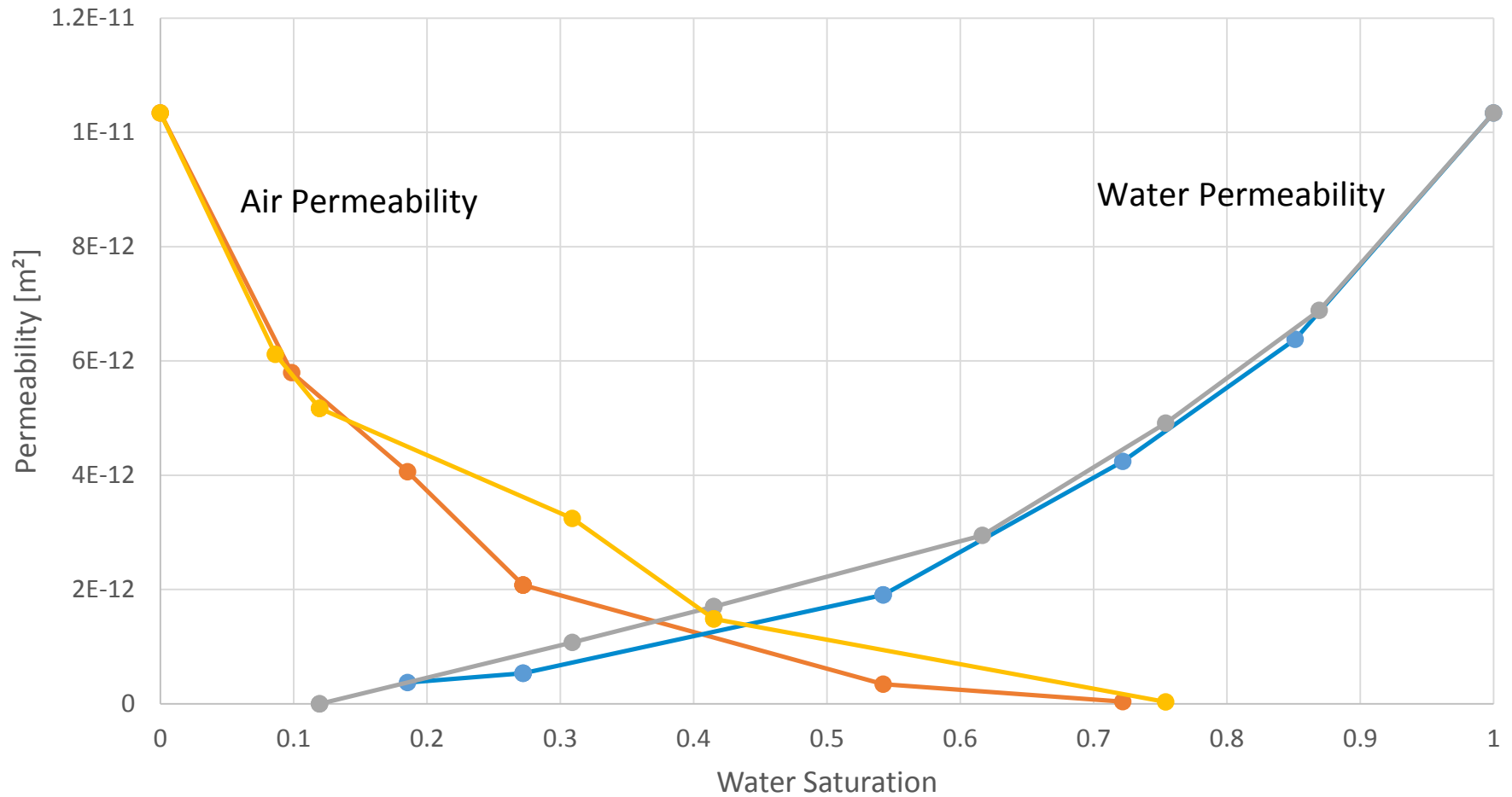
Saturation Dependent Permeability

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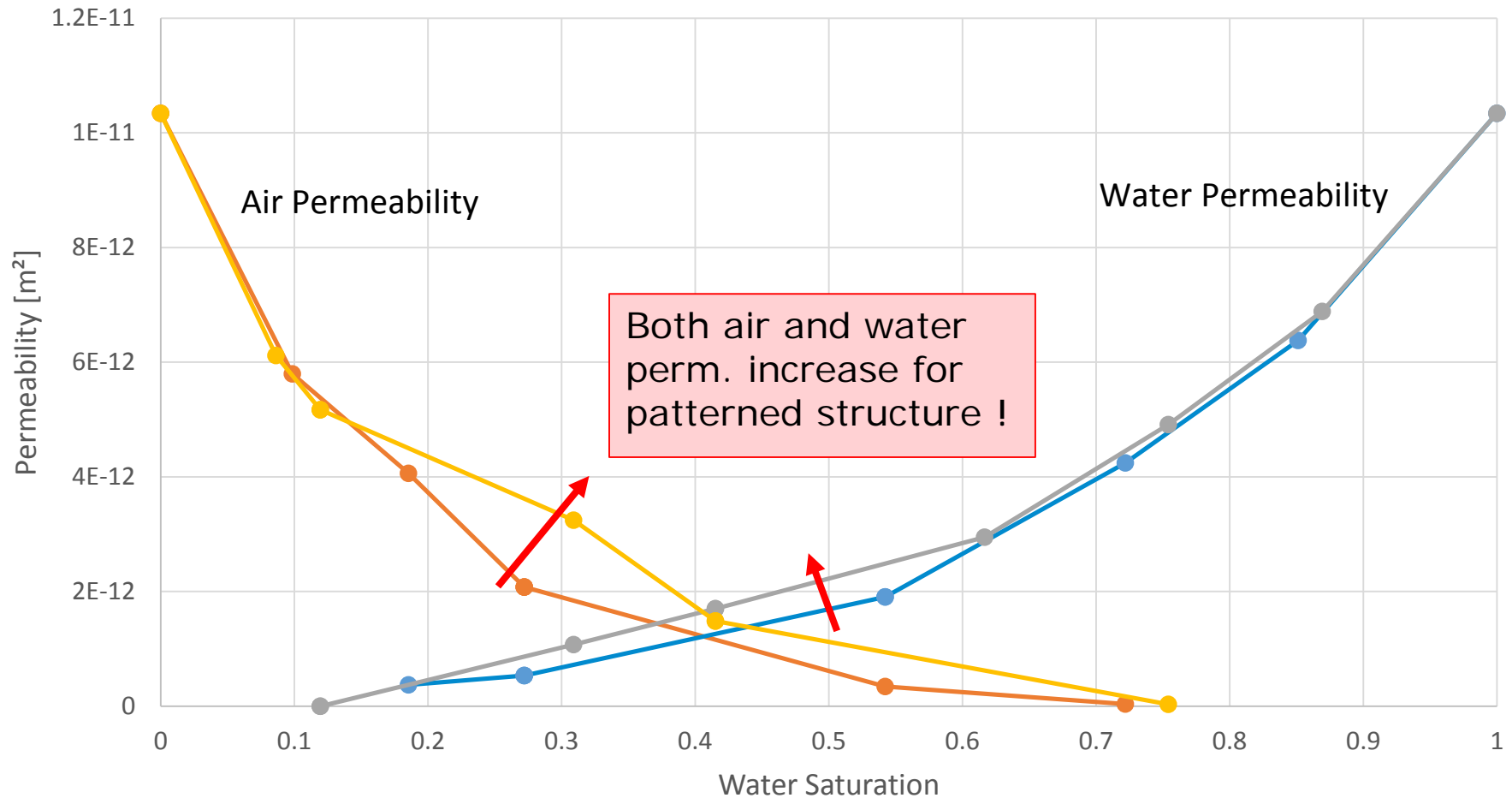
1. Determine phase distribution
2. Calculate single-phase flow (solve Stokes equation)
3. Find permeability (average flow velocity)



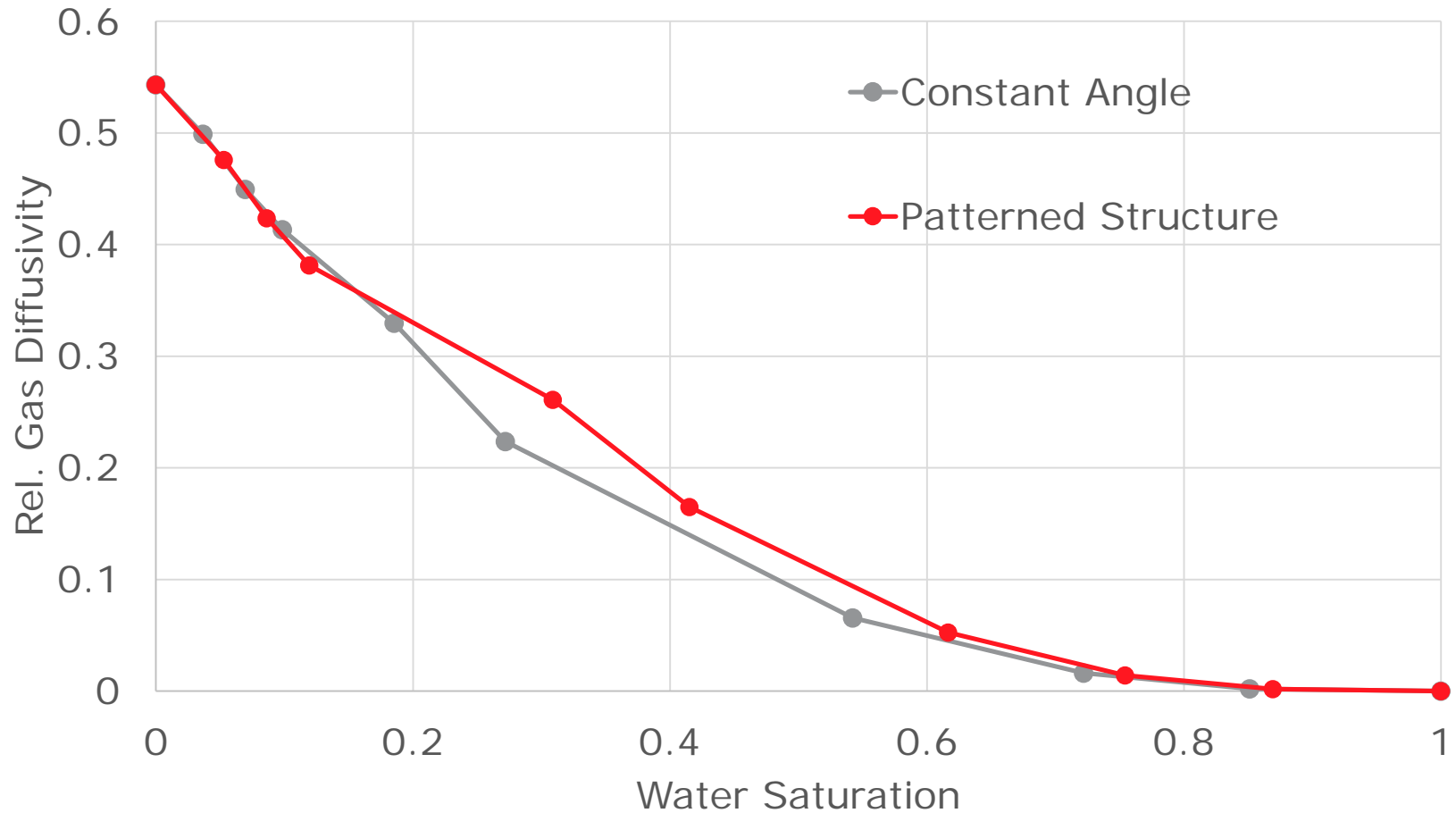
Through-Plane Permeability (Uncompressed GDL)



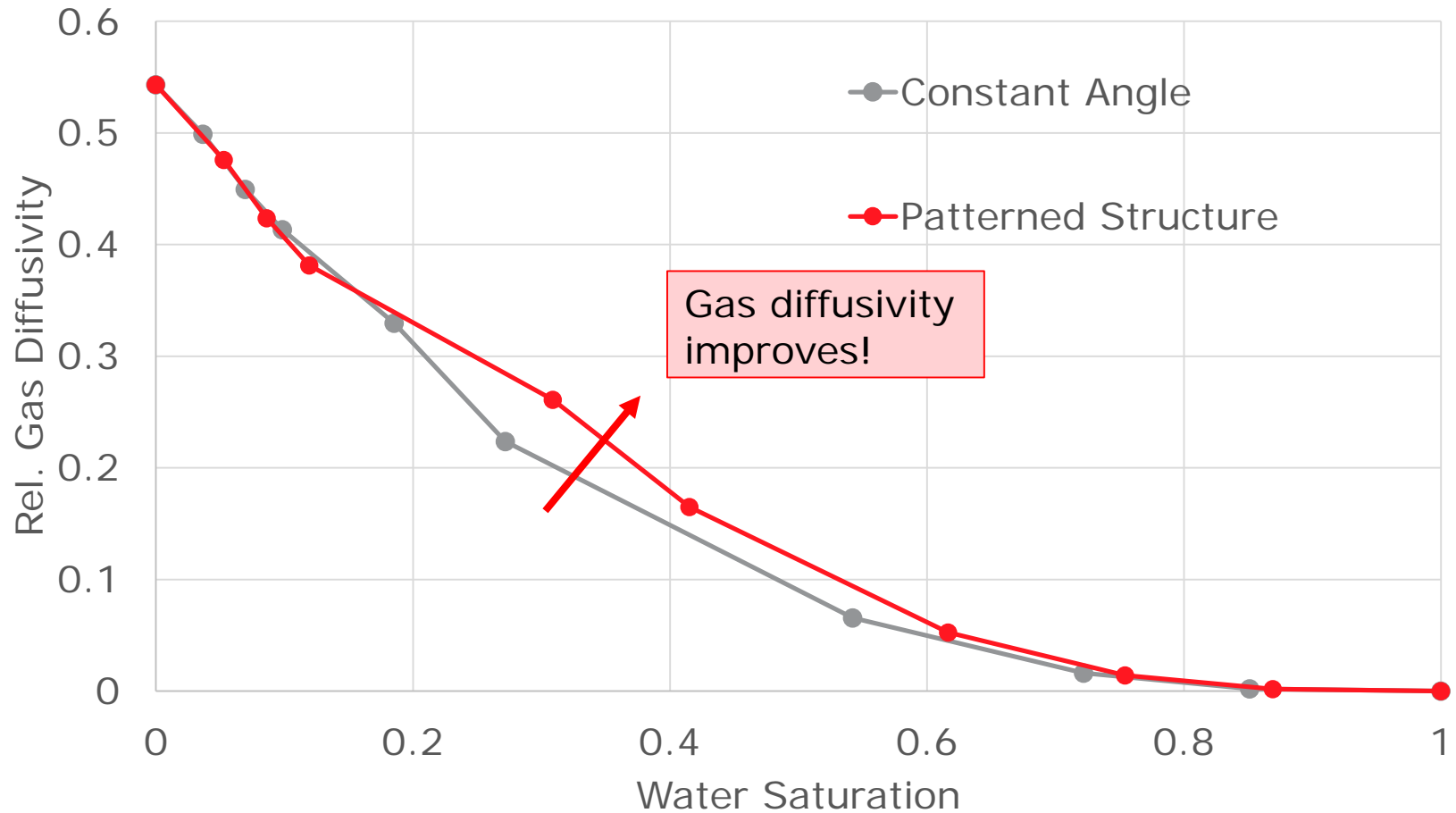
Through-Plane Permeability (Uncompressed GDL)



Through-Plane Diffusivity (Uncompressed GDL)



Through-Plane Diffusivity (Uncompressed GDL)



Relative Permeability – Computational Costs

Challenge:

- Parameter that is most expensive to compute:
 - Requires to solve one flow problem per saturation level

Observation:

- Low saturation states are computationally most expensive

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Improvements:

- Restart of computations
 - Compute permeability from highest to lowest saturation state
 - Use result from previous computation to speed up the next one

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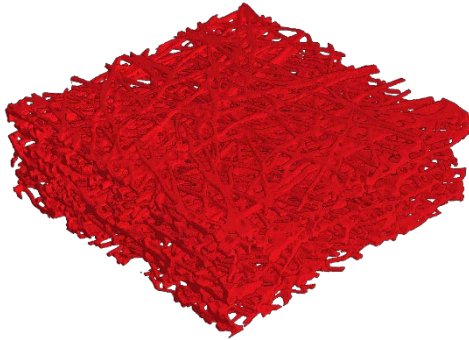
Observation:

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Improvements:

- Restart of computations
 - Compute permeability from highest to lowest saturation state
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- New stopping criterion:
 - Relative error compared to the permeability of the fully saturated state

Speed-Up

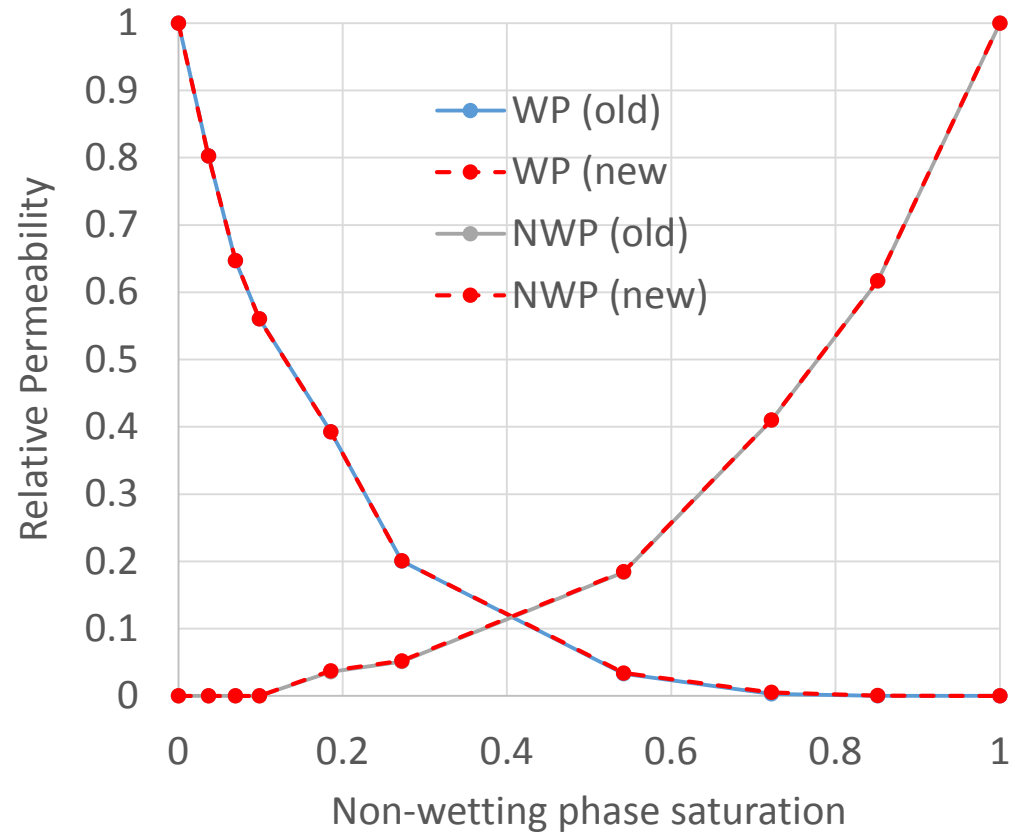


Comparison:

- Uncompressed GDL
- 600 x 600 x 200 Voxels
- 10 Saturation levels each
- Parallelization: 12x

Runtime needed:

- Old: 6h 22 min
- New: 58 min



Summary

1. Generated a 3D GDL model
2. Computed compressed structure
3. Computed permeability
4. Computed water saturation with different contact angles
5. Computed transport properties for different water saturations
6. Speed-up of permeability computations

Thank You!

Thanks to:

- Steffen Schwichow (Math2Market)
- Volker Schulz (DHBW Mannheim)
- Funding through OptiGaaII project

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