



# The Prediction of Mechanical Properties of Composites and Porous Materials Based on Micro-CT-Scans and 3D Material Models

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Math2Market GmbH



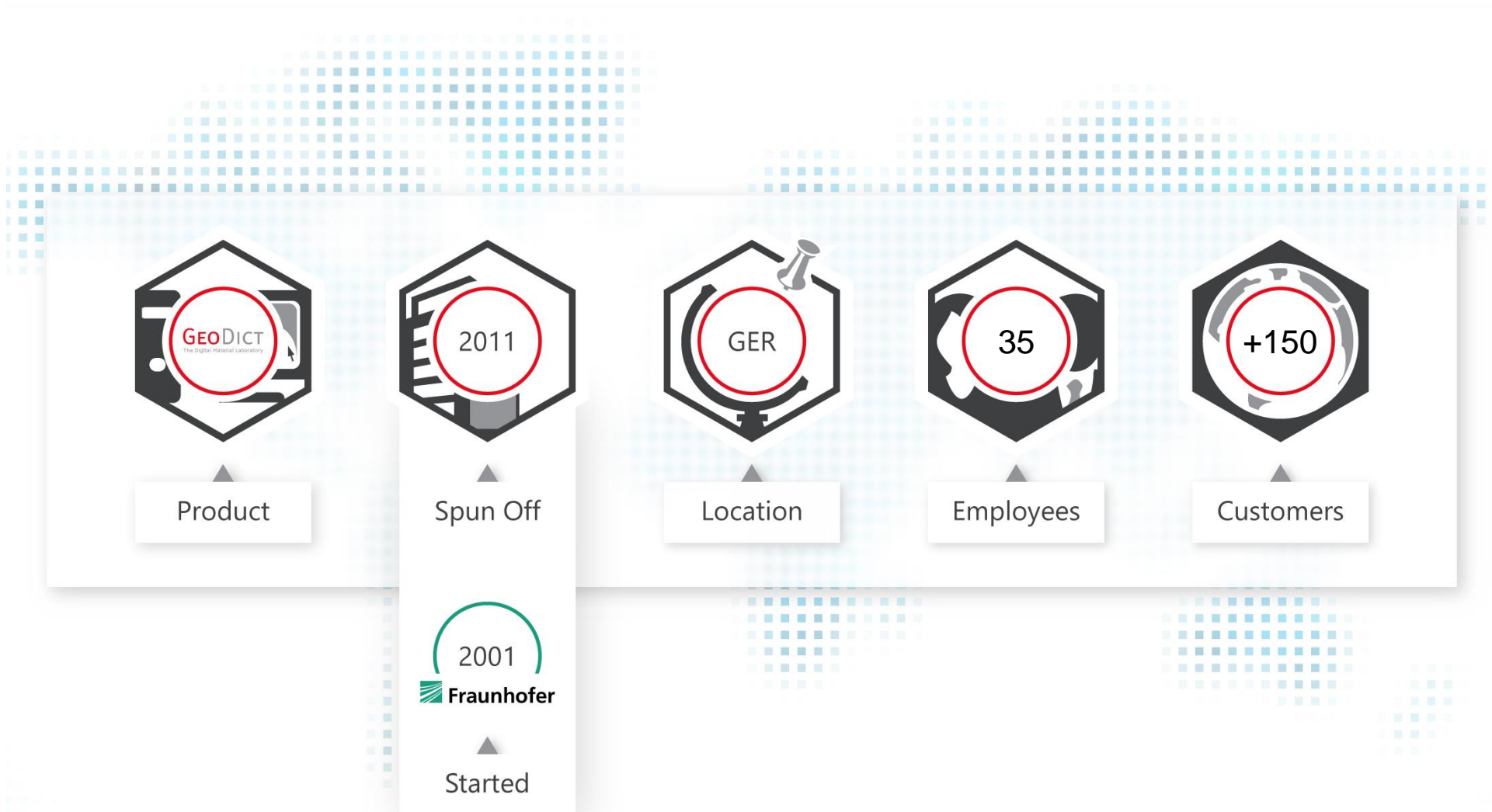
# Content

- Company Overview
- What is the Digital Material Laboratory GeoDict?
- Characterization of a Short Glass Fiber Reinforced Plastic



# Company Overview

## Math2Market GmbH - Company Overview





# Company Overview

## Math2Market GmbH Company – Location and Contact



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# Company Overview

## Math2Market GmbH Company – our Mission and Goals

We help our clients to profitably engineer better materials and processes through digital solutions.

We believe that to understand is to improve.



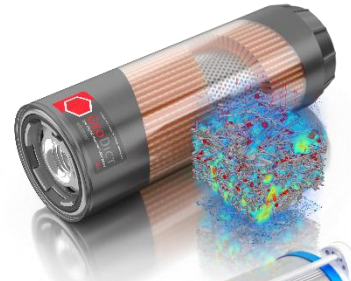
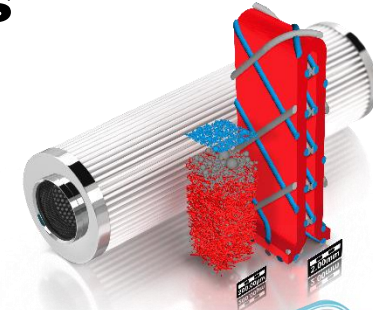


# Company Overview

## Math2Market GmbH Company – Promoted Industries

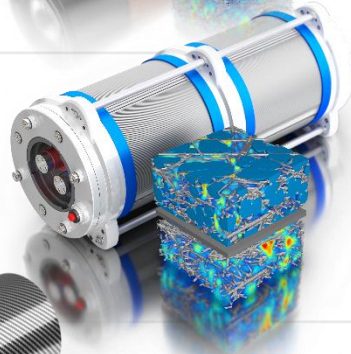
### Filtration

Mostly automotive,  
filter media & filters  
for water, sludge, oil,  
air and fuel



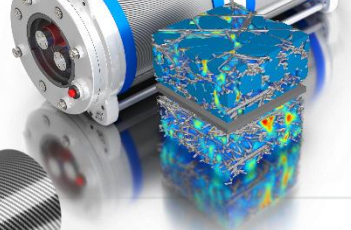
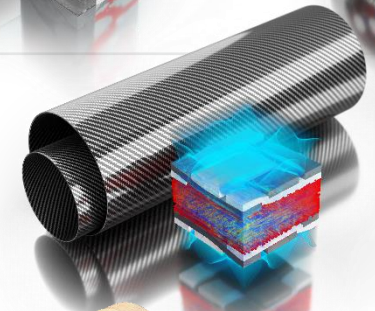
### Electrochemistry

Fuel cell media &  
battery materials,  
catalyst materials



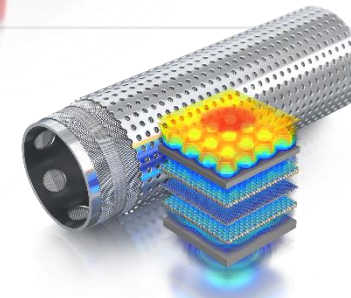
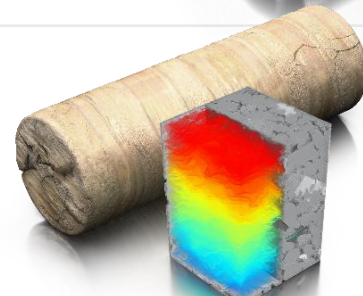
### Composites

CFRP, GFRP,  
mostly automotive,  
lightweight materials



### Oil and Gas

Digital rock physics,  
digital sand control







# What is the Digital Material Laboratory GeoDict?



# GeoDict – Digital Material Laboratory

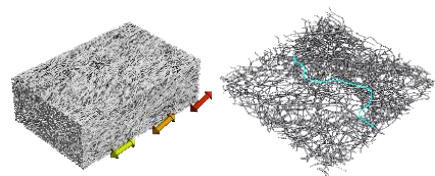
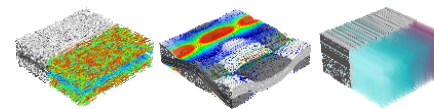


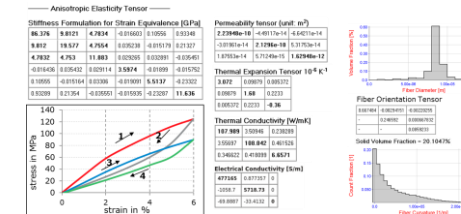
Image Analysis



Modelling  
Microstructures



Microstructure  
Simulation



Macroscopic Material  
Parameters

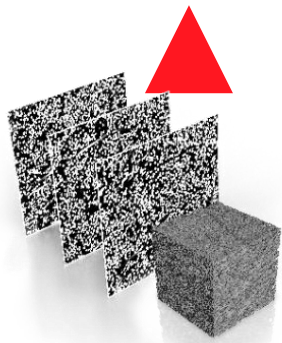
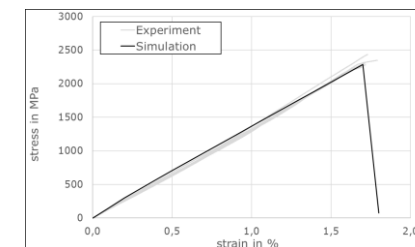


Image Acquisition

Change Geometry

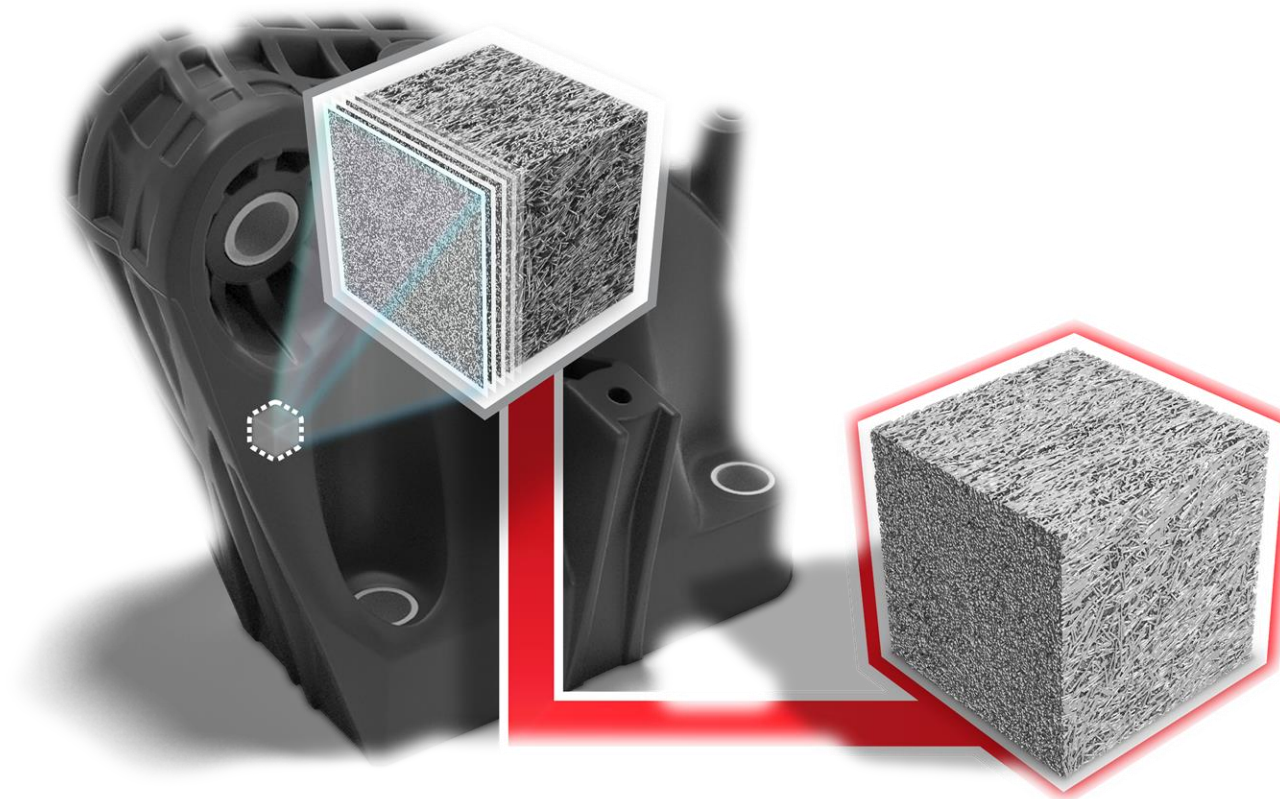
Material Property



Experimental  
Verification

Development of Materials



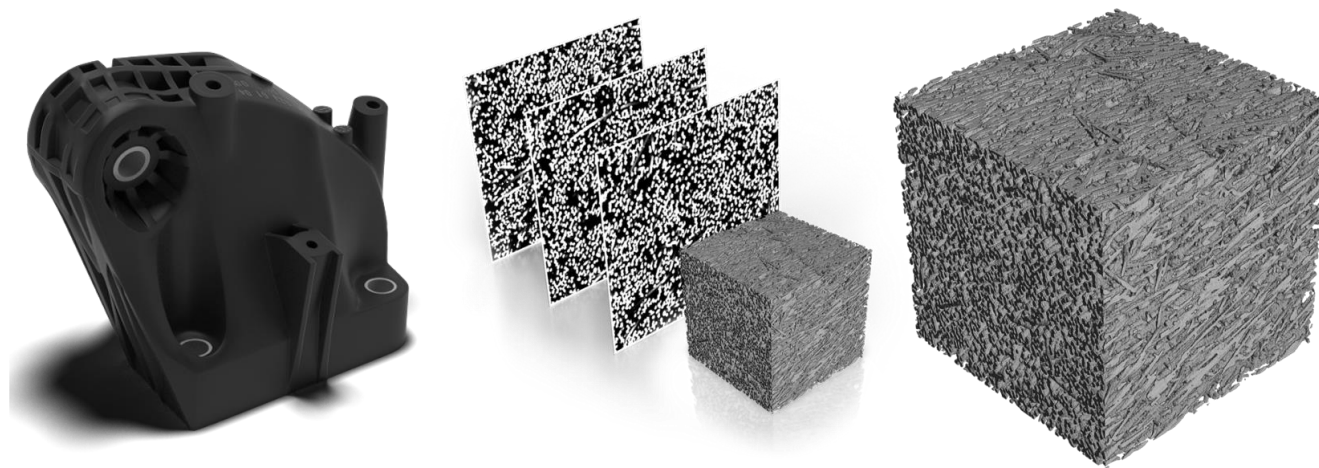


# Characterization of a Short Glass Fiber Reinforced Plastic



# Short Glass Fiber Reinforced Plastic

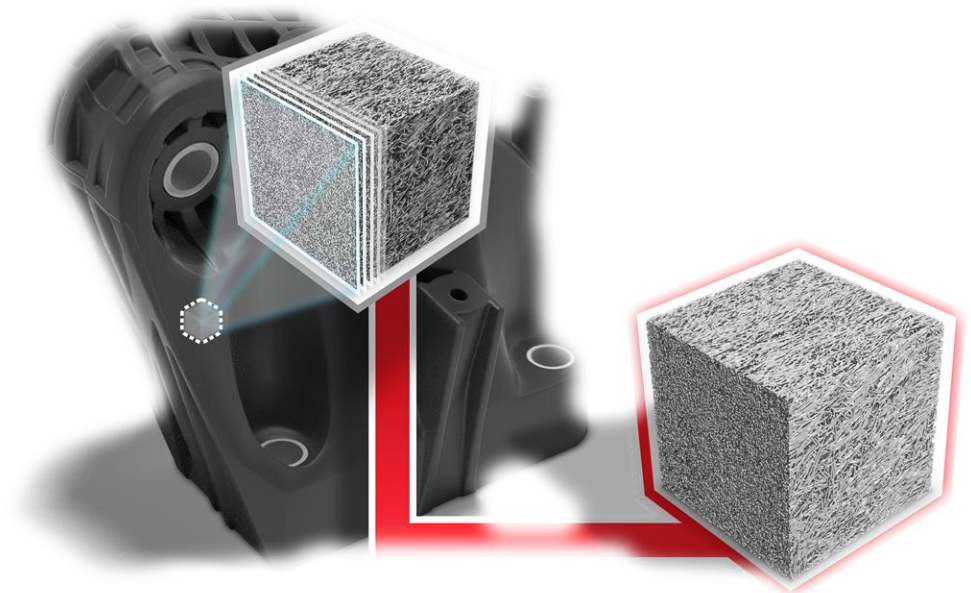
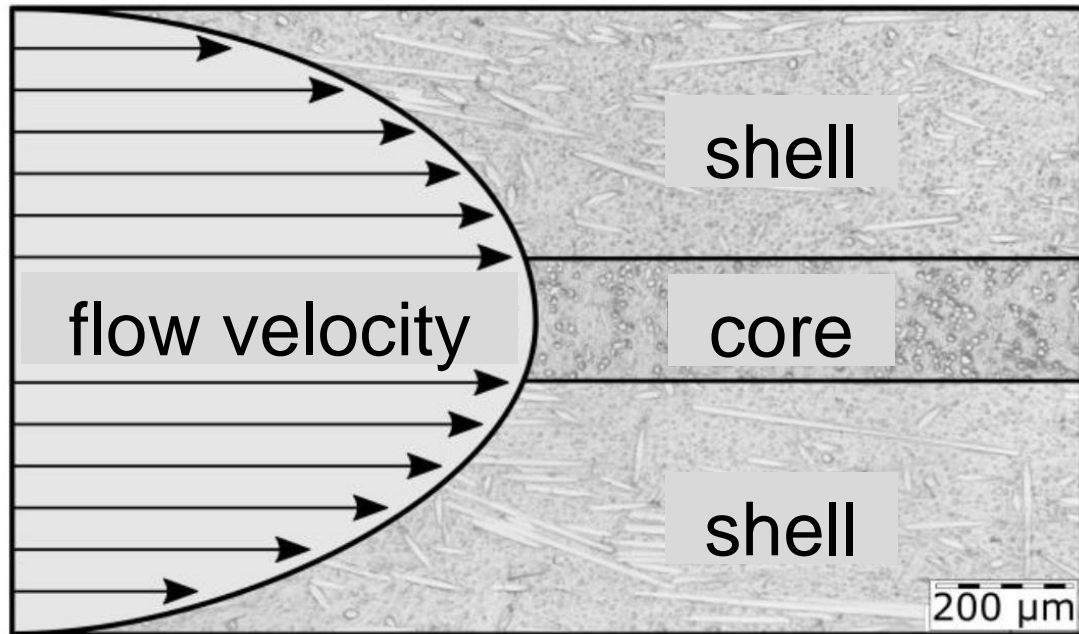
- Material used in an engine bearer
  - produced by injection molding
  - matrix material
    - thermoplastic
    - polyamide 6
  - fiber reinforcement
    - glass fibers
    - percentage: 50 % by weight
    - length: 100  $\mu\text{m}$  – 500  $\mu\text{m}$
- $\mu\text{CT}$  scan of the material with a resolution of 1.4  $\mu\text{m}$





# Short Glass Fiber Reinforced Plastic

- Fiber orientation in injection molded materials
  - example of molded plate



for complex geometries no analytical methods are accurate enough





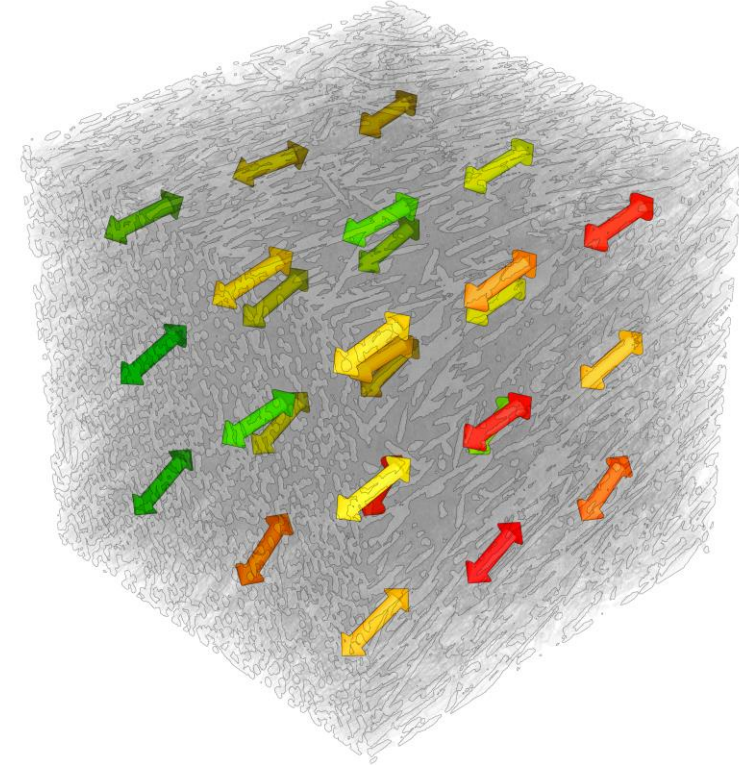
# Short Glass Fiber Reinforced Plastic

- Determination of the fiber orientation using FiberGuess
  - dividing the RVE into user defined blocks
  - PCA: principal component analysis
    - subdivides the domain into windows to eliminate the influence of fiber crossings
    - identifies single fiber fragments and analyzes the direction
  - SLD: star length distribution
    - working on voxel basis
    - analyzes the chord length through the voxel
  - averaging the defined blocks to determine the average orientation tensor



# Short Glass Fiber Reinforced Plastic

- Visualization for each block
  - main fiber orientation
  - degree of orientation
  - solid volume fraction
- Results for each block

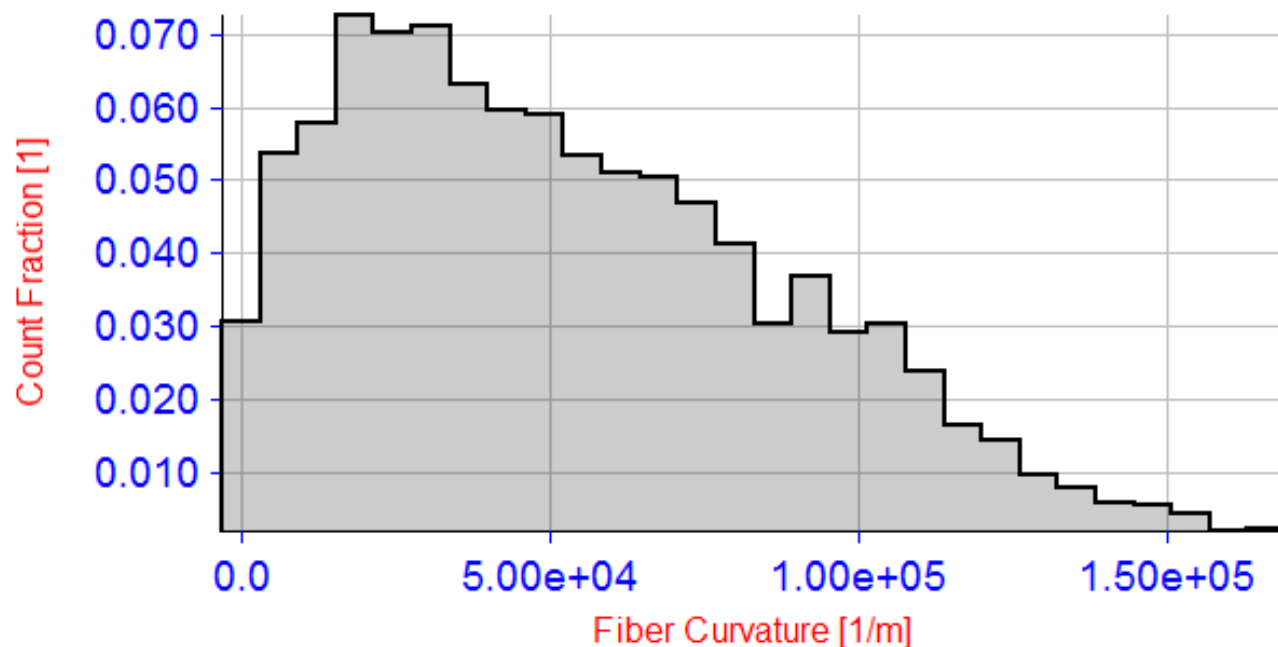
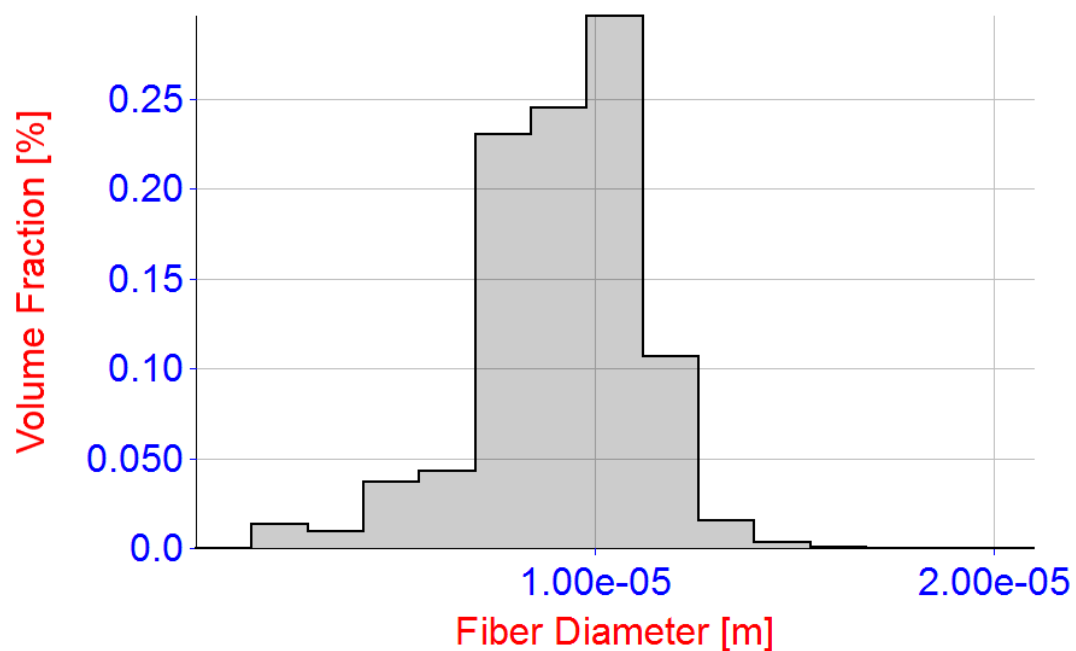


$$\overline{A_{PCA}} = \begin{bmatrix} 0.545 & -0.034 & 0.023 \\ sym & 0.190 & 0.020 \\ sym & sym & 0.265 \end{bmatrix} \quad \overline{A_{SLD}} = \begin{bmatrix} 0.640 & -0.042 & 0.106 \\ sym & 0.109 & 0.019 \\ sym & sym & 0.251 \end{bmatrix}$$



# Short Glass Fiber Reinforced Plastic

- Calculation of other geometric characteristics
  - fiber diameter distribution
  - fiber curviness








# Short Glass Fiber Reinforced Plastic

- Input for the mechanical simulation using ElastoDict-VOX
  - model of the microstructure
    - imported and segmented  $\mu$ CT scan
    - generated model (FiberGeo, WeaveGeo, ...)
  - material properties of the single constituents
    - from datasheet
    - from measurement



# Short Glass Fiber Reinforced Plastic

- Input for the mechanical simulation using ElastoDict
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$E_{\text{fiber}}$	= 72 GPa
$\nu_{\text{fiber}}$	= 0.22
$E_{\text{matrix}}$	= 3.3 GPa
$\nu_{\text{matrix}}$	= 0.39



# Short Glass Fiber Reinforced Plastic

- Linear elastic properties of the homogenized material
  - applying small strain/stress increment
  - periodic boundary conditions
  - simulation of six load cases
    - three uniaxial experiments: XX, YY, ZZ
    - three shear experiments: XY, YZ, XZ
  - obtaining the general anisotropic Hooke's Law to calculate the elasticity tensor

$$\sigma_{ij} = \sum_{r,s=1}^3 c_{ijrs} \epsilon_{rs} \quad , \quad i, j \in \{1,2,3\}$$





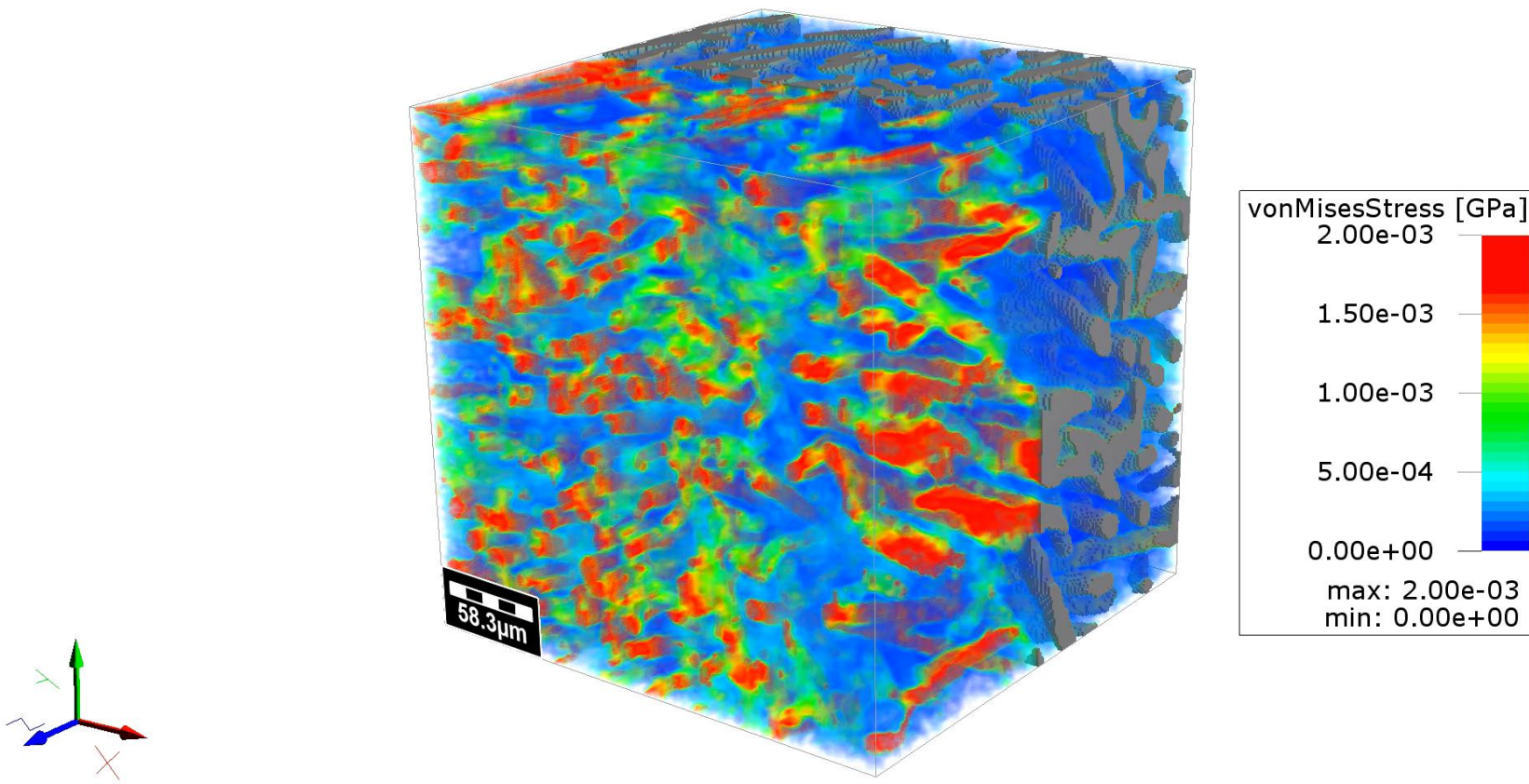
# Short Glass Fiber Reinforced Plastic

- Visualization of the results
  - displacement
  - stress
  - strain
- Homogenized material properties
  - anisotropic elasticity tensor
  - approximation of the engineering constants
    - orthotropic
    - isotropic
  - thermal expansion properties



# Short Glass Fiber Reinforced Plastic

- Visualization of the results
  - e.g. von Mises stress





# Short Glass Fiber Reinforced Plastic

- Homogenized material properties
  - elasticity tensor
  - engineering constants

—— Anisotropic Elasticity Tensor ——

Stiffness Formulation for Strain Equivalence [GPa]

10.016	5.3594	5.4999	0.045512	-0.094108	0.12392
5.3596	10.716	5.7295	0.51863	-0.093485	0.082552
5.4998	5.7296	15.377	1.1905	-0.60699	-0.20454
0.045524	0.51862	1.1905	3.4158	-0.34325	-0.21146
-0.094059	-0.09342	-0.60689	-0.34327	3.0735	0.083305
0.12388	0.08248	-0.20462	-0.21149	0.08328	2.6627



Orthotropic Approximation

	Strain Equivalence	Energy Equivalence	Mean Value
Young's Modulus $E_1$ [GPa]	6.7722	6.7725	6.7724 +- 0.0001
Young's Modulus $E_2$ [GPa]	7.2198	7.2201	7.2200 +- 0.0002
Young's Modulus $E_3$ [GPa]	11.3678	11.3680	11.3679 +- 0.0001
Poisson Ratio $\nu_{12}$	0.3858	0.3857	0.3858 +- 0.0000
Poisson Ratio $\nu_{13}$	0.2139	0.2139	0.2139 +- 0.0000
Poisson Ratio $\nu_{23}$	0.2255	0.2255	0.2255 +- 0.0000
Poisson Ratio $\nu_{21}$	0.4112	0.4112	0.4112 +- 0.0000
Poisson Ratio $\nu_{31}$	0.3591	0.3591	0.3591 +- 0.0000
Poisson Ratio $\nu_{32}$	0.3551	0.3551	0.3551 +- 0.0000
Shear Modulus $G_{12}$ [GPa]	2.6627	2.6625	2.6626 +- 0.0001
Shear Modulus $G_{13}$ [GPa]	3.0735	3.0733	3.0734 +- 0.0001
Shear Modulus $G_{23}$ [GPa]	3.4158	3.4156	3.4157 +- 0.0001



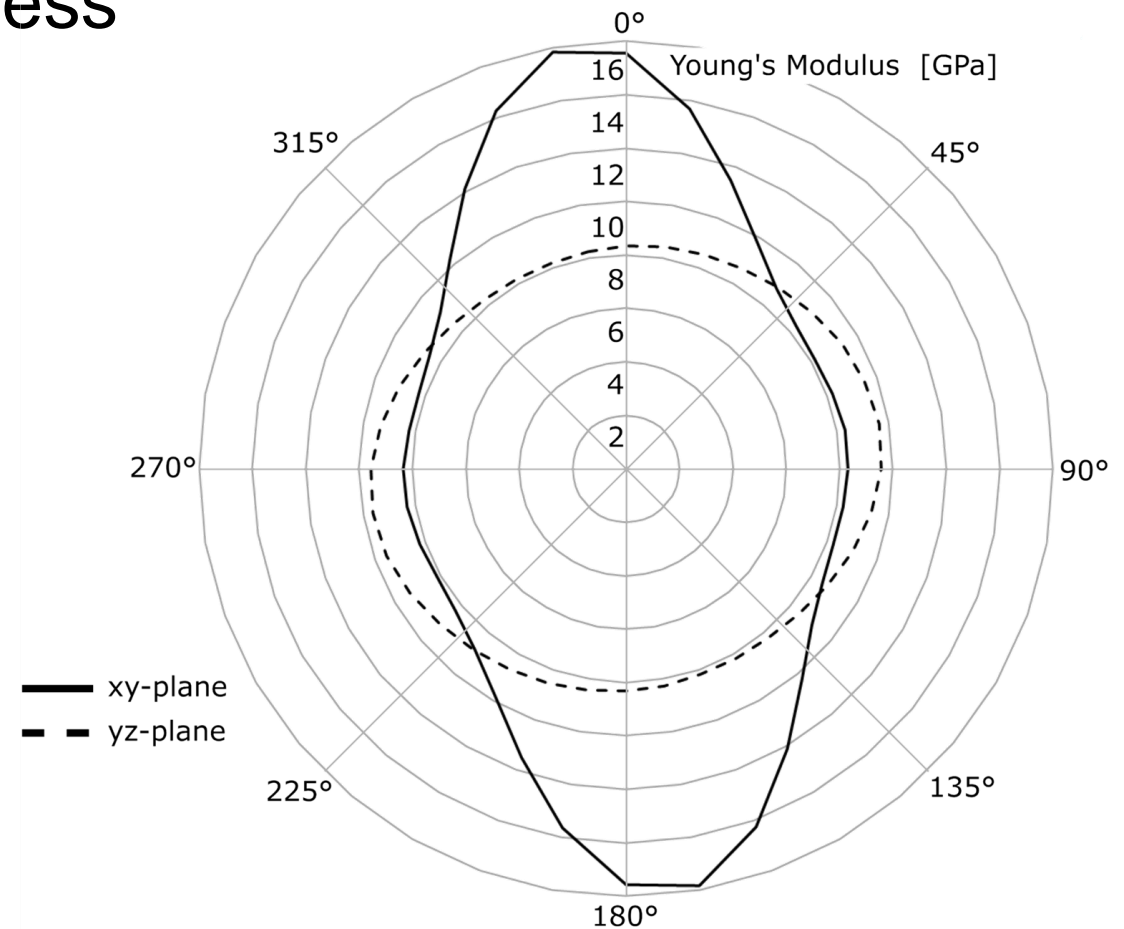
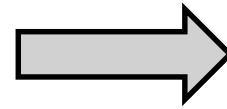
# Short Glass Fiber Reinforced Plastic

- Homogenized material properties
  - angle dependency of the stiffness

—— Anisotropic Elasticity Tensor ——

Stiffness Formulation for Strain Equivalence [GPa]

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# Short Glass Fiber Reinforced Plastic

- Homogenized material properties
  - defining the expansion coefficient of the single constituents
  - calculating the macroscopic expansion properties

Thermal Stress Tensor GPa/K

<b>-0.001047</b>	4.82e-07	9.271e-07
4.82e-07	<b>-0.001058</b>	6.252e-07
9.271e-07	6.252e-07	<b>-0.001056</b>



# Short Glass Fiber Reinforced Plastic

- Parameter studies based on modelled microstructures
  - short fiber structures with different fiber volume fractions
  - constant fiber length: 200  $\mu\text{m}$
  - constant fiber diameter: 9.2  $\mu\text{m}$   
(average diameter from the imported  $\mu\text{CT}$  structure)
  - definition of the fiber orientation tensor

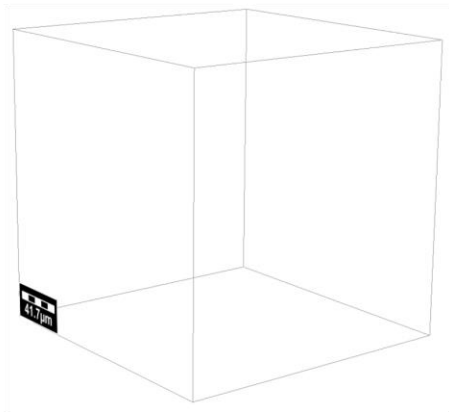
$$\overline{A}_{fiber} = \begin{bmatrix} 0.8 & 0 & 0 \\ sym & 0.1 & 0 \\ sym & sym & 0.1 \end{bmatrix}$$

- automated study using the Python-Interface GeoPython

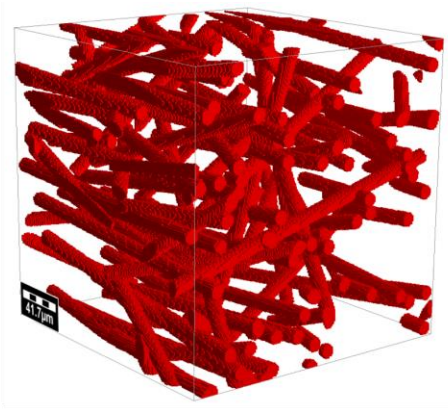


# Short Glass Fiber Reinforced Plastic

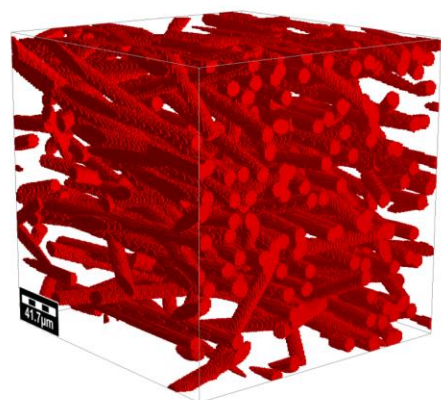
- Influence of the fiber volume fraction on the Young's modulus



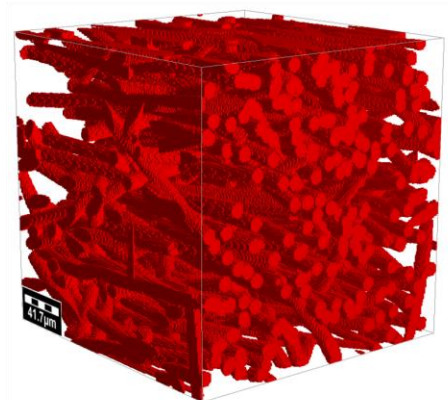
0 %



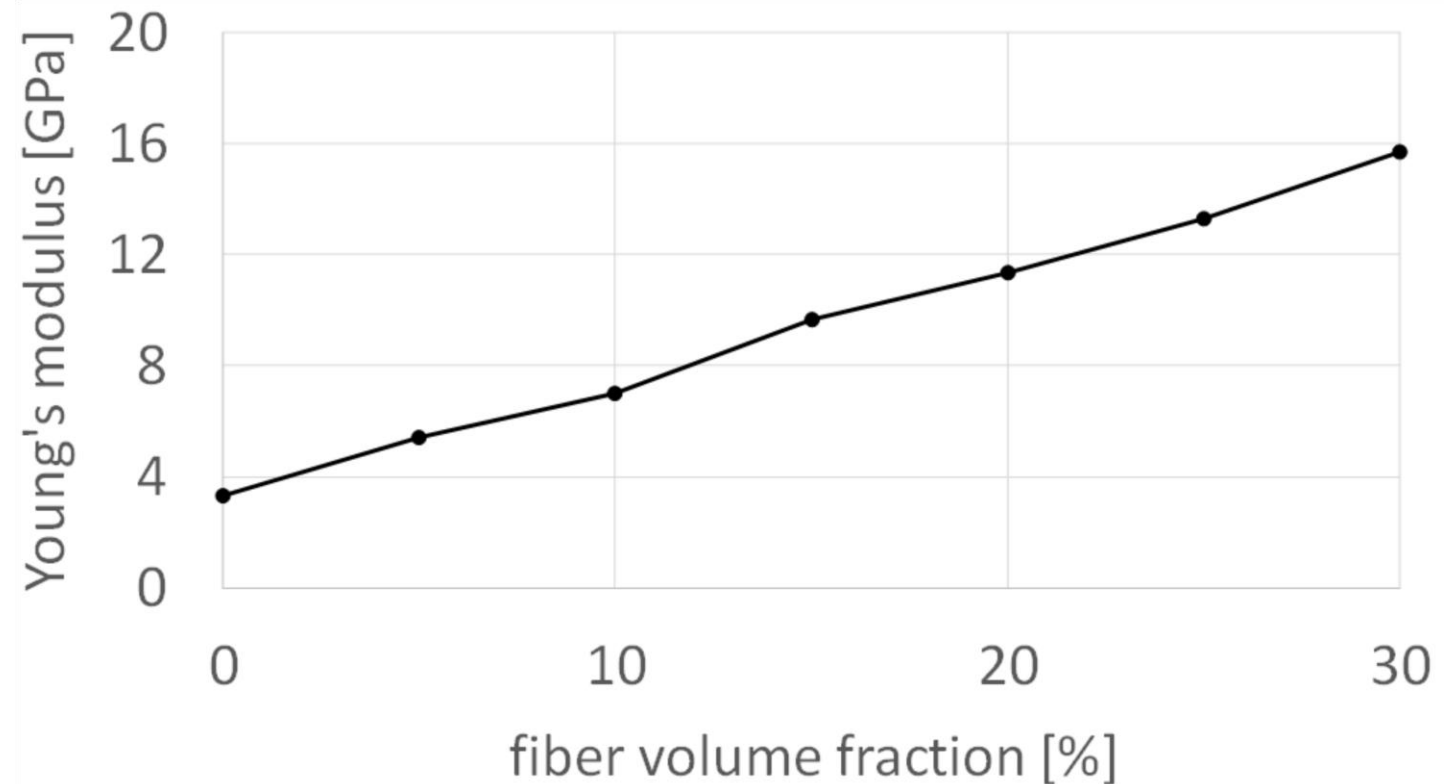
10 %



20 %



30 %





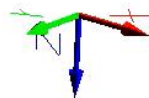
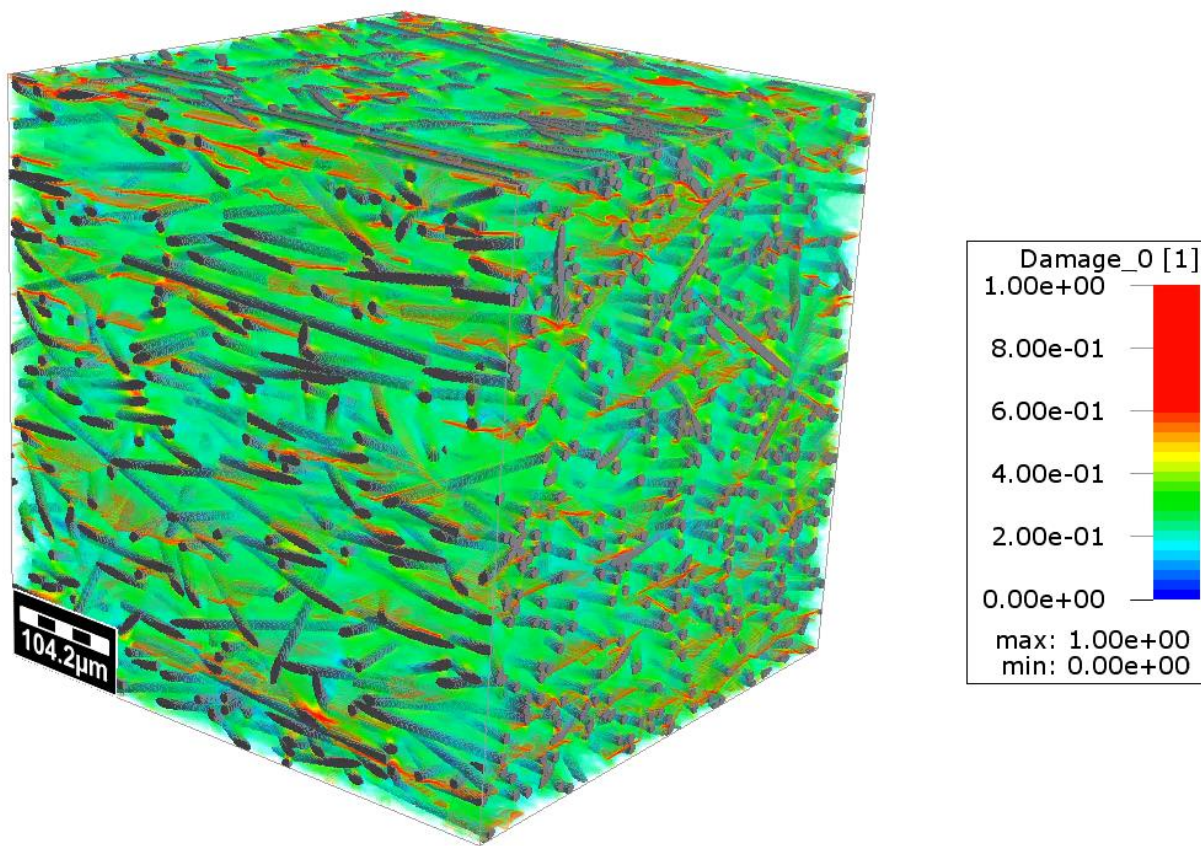
# Short Glass Fiber Reinforced Plastic

- Simulation of matrix damage using ElastoDict-LD
  - nonlinear material models available, e.g.:
    - Neo-Hookean
    - Mooney-Rivlin
    - plastic deformation
  - user defined materials (UMAT interface)
  - nonlinear geometry option
  - different loading types
    - uniaxial/shear
    - complex (free definition of the deformation gradient)
  - free or confined boundary conditions



# Short Glass Fiber Reinforced Plastic

- Simulation of matrix damage using ElastoDict-LD
  - visualization of UMAT-state variables (e.g. damage)

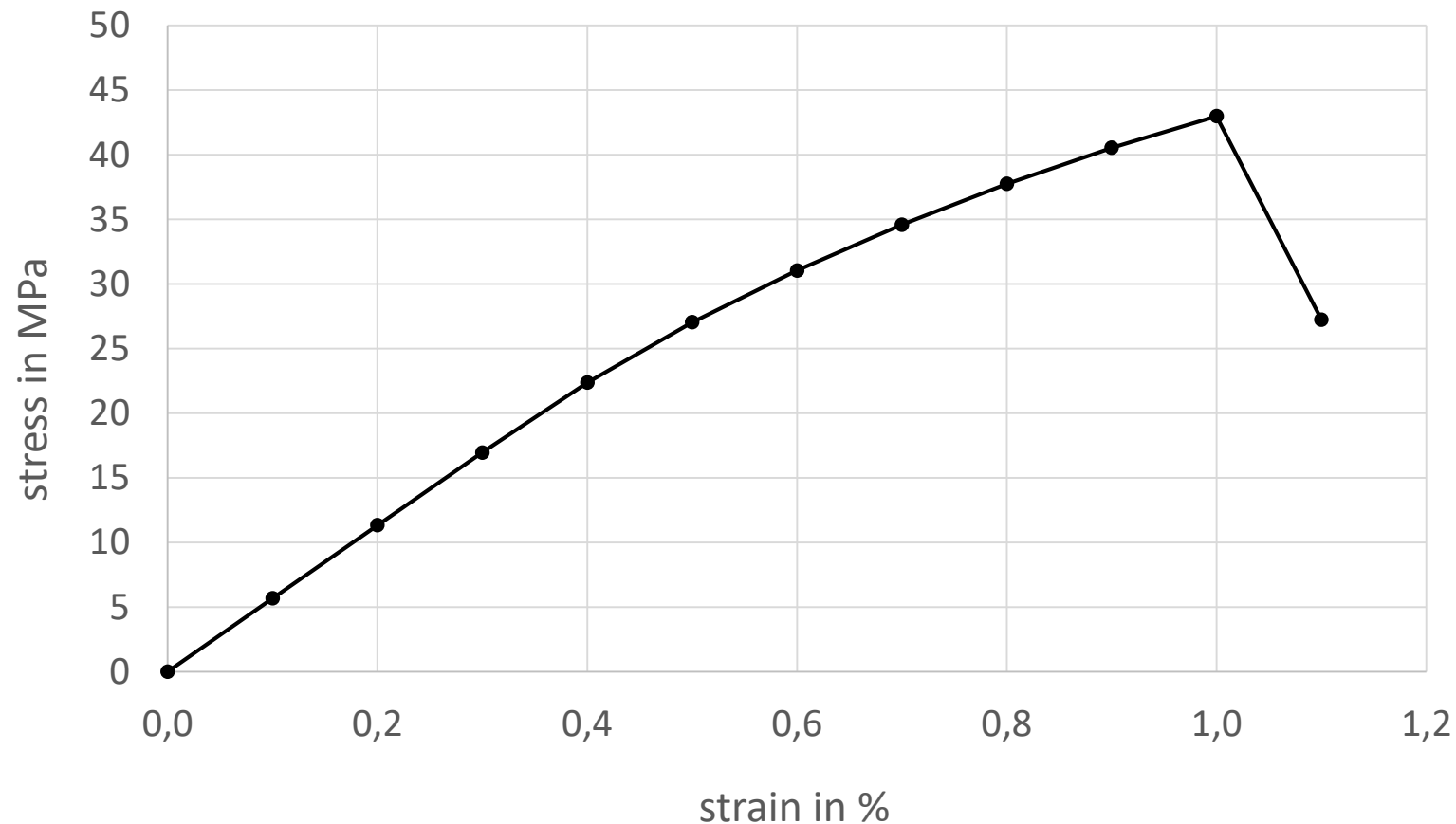






# Short Glass Fiber Reinforced Plastic

- Simulation of matrix damage using ElastoDict-LD
  - macroscopic stress strain curve





# Conclusion

- Micromechanical model
  - import your  $\mu$ CT scan and segment the single constituents
  - generate your microstructure using FiberGeo, FoamGeo, ...
- Geometric analysis
  - Fiber orientation analysis
  - Fiber diameter and curvature distribution
- Mechanical simulation
  - elasticity tensor of the homogenized material
  - thermal stress tensor
  - nonlinear material properties



# Thank you!

