

# The Digital Twin – A comparative study of material simulation on $\mu$ CT-scanned and modelled microstructures

**GEO**DICT  
The Digital Material Laboratory

**Constantin Bauer**  
**Math2Market GmbH**

**MATH**  
**2 MARKET**

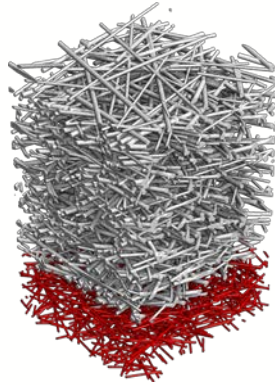
# What is GeoDict?

## IMPORT



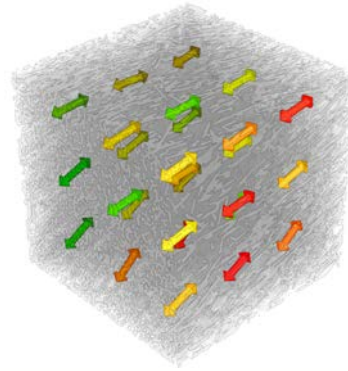
Diverse ways to import materials for modeling

## MODEL



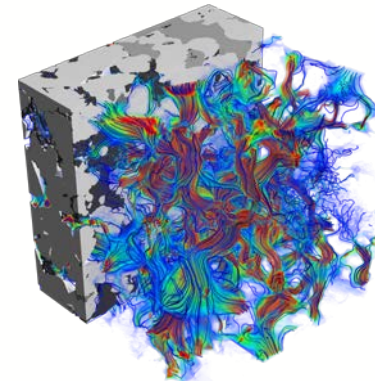
Detailed material models created in 3D

## ANALYZE



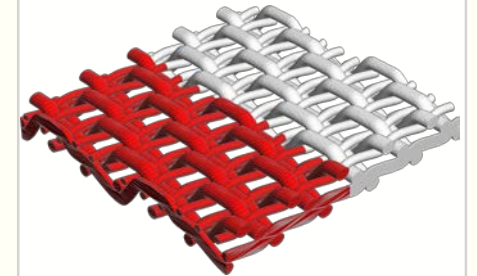
Extensive analysis and evaluation of structural material properties

## PREDICT



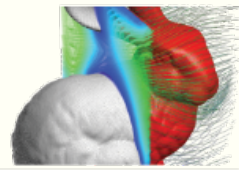
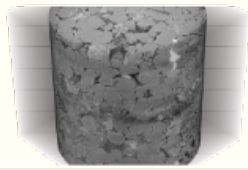
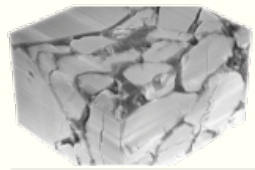
In-depth analysis and prediction of material behavior

## EXPORT

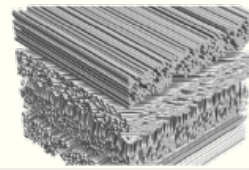
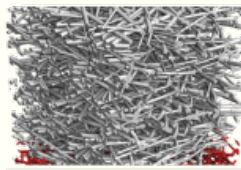


GeoDict models made available for standard workflows

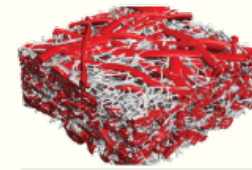
# GeoDict Module Overview



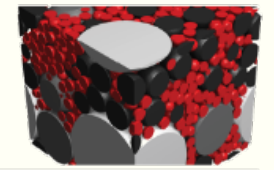
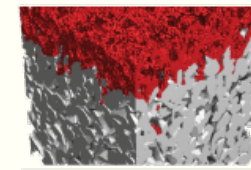
IMPORTGEO



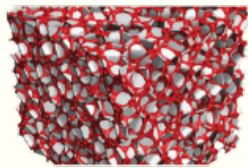
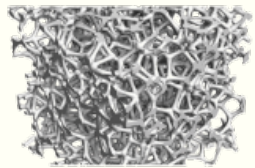
FIBERGEO



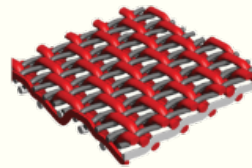
PAPERGEO



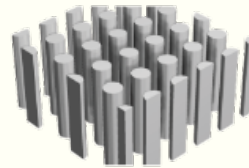
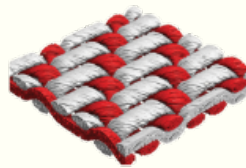
GRAINGEO



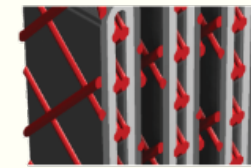
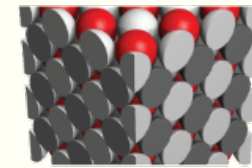
FOAMGEO



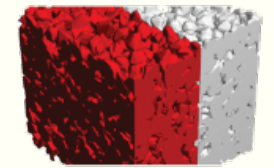
WEAVEGEO



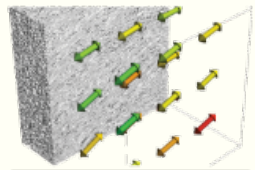
GRIDGEO



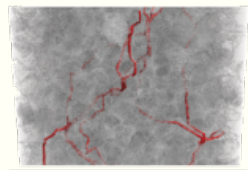
PLEATGEO



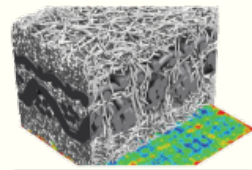
EXPORTGEO



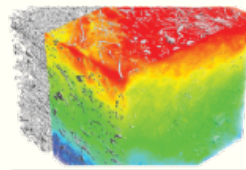
FIBERGUESS



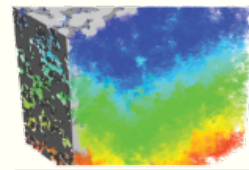
PORODICT



MATDICT



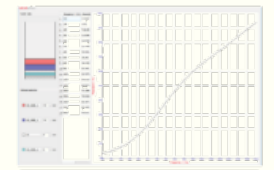
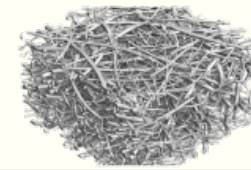
CONDUCTODICT



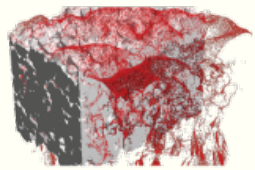
DIFFUDICT



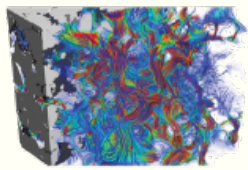
ELASTODICT



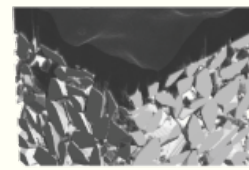
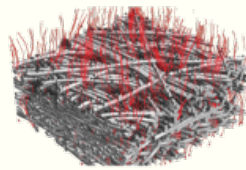
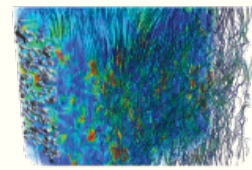
ACOUSTODICT



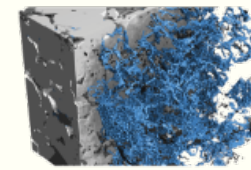
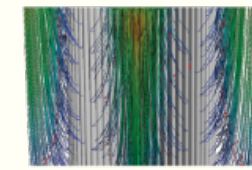
ADDIDICT



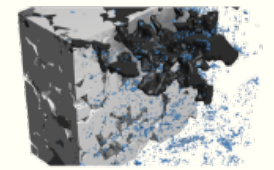
FLOWDICT



FILTERDICT MEDIA & ELEMENT

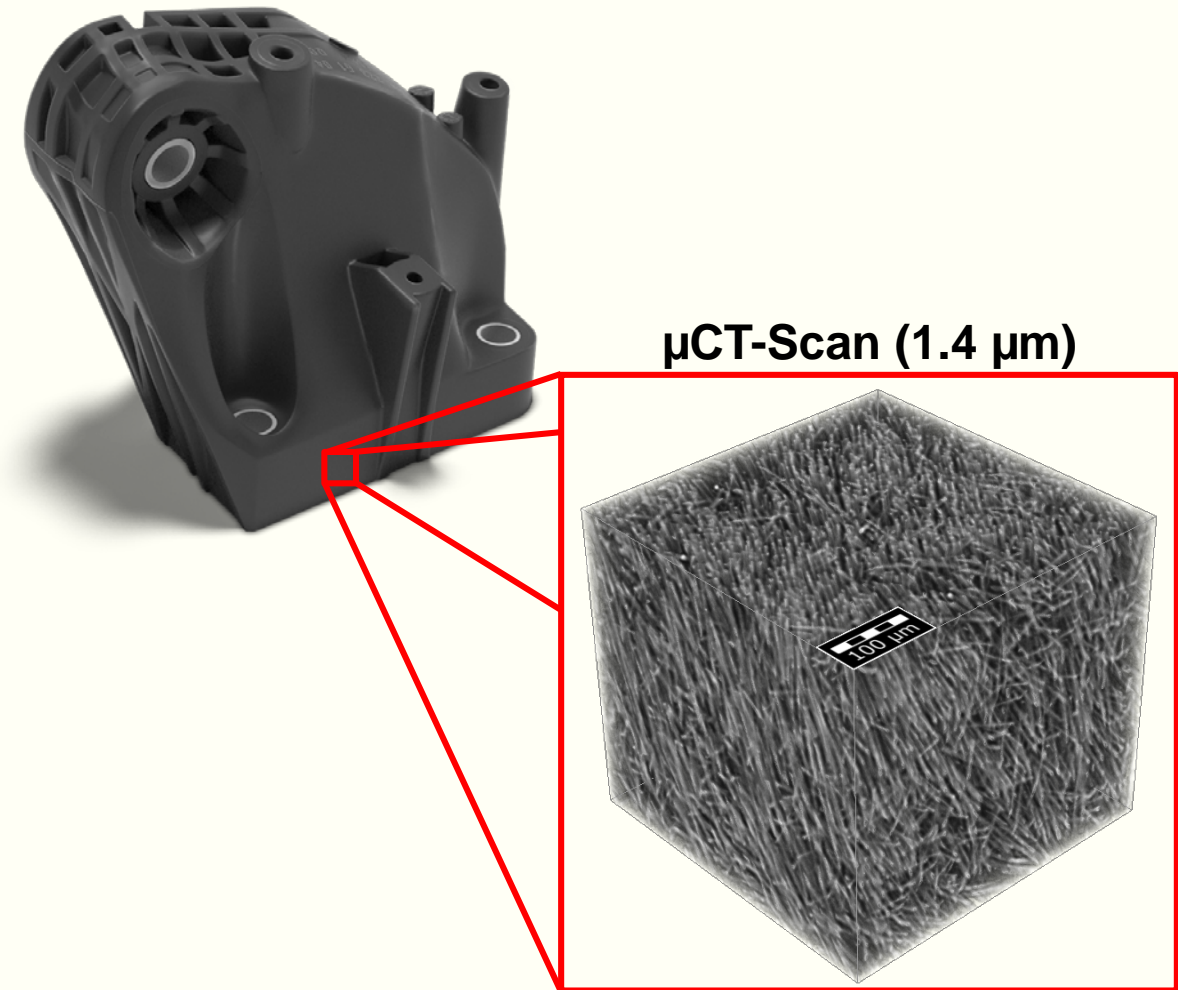


SATUDICT



# What material are we looking at?

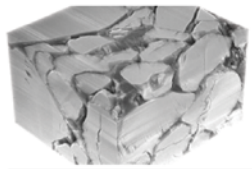
- PA6GF50
  - Polyamide 6 matrix
  - short glass fiber reinforcement
  - 50 % fibers by weight
- produced by injection molding
- used in mass production for structural components (e.g. engine bearer)



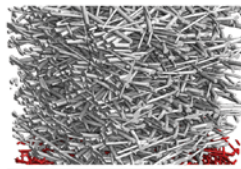
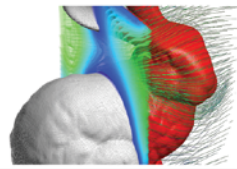
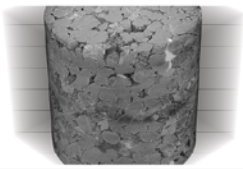
# 6 Steps to the Digital Twin

1. Import, process and segment the  $\mu$ CT-scan
2. Calculate the mechanical properties directly on the  $\mu$ CT-scan
3. Determine the geometrical properties of the material  
(fiber diameter, fiber orientation, fiber length)
4. Model the digital twin
5. Calculate the mechanical properties of the digital twin
6. Comparison of the results

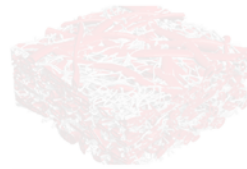
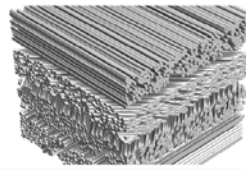
# used GeoDict Modules



IMPORTGEO



FIBERGEO



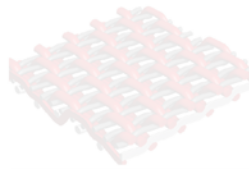
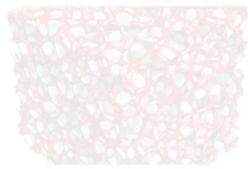
PAPERGEO



GRAINGEO



FOAMGEO



WEAVEGEO



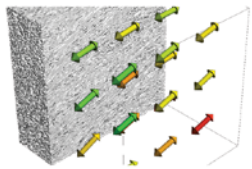
GRIDG



PLEATGEO



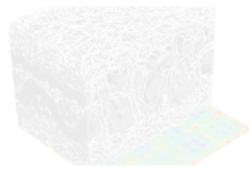
EXPORTGEO



FIBERGUESS



PORODICT



MATDICT



CONDUCTODICT



DIFFUDICT



ELASTODICT



ACOUSTODICT



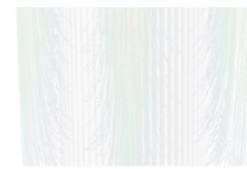
ADDIDICT



FLOWDICT



FILTERDICT MEDIA & ELEMENT



SATUDICT



# Import and Segmentation

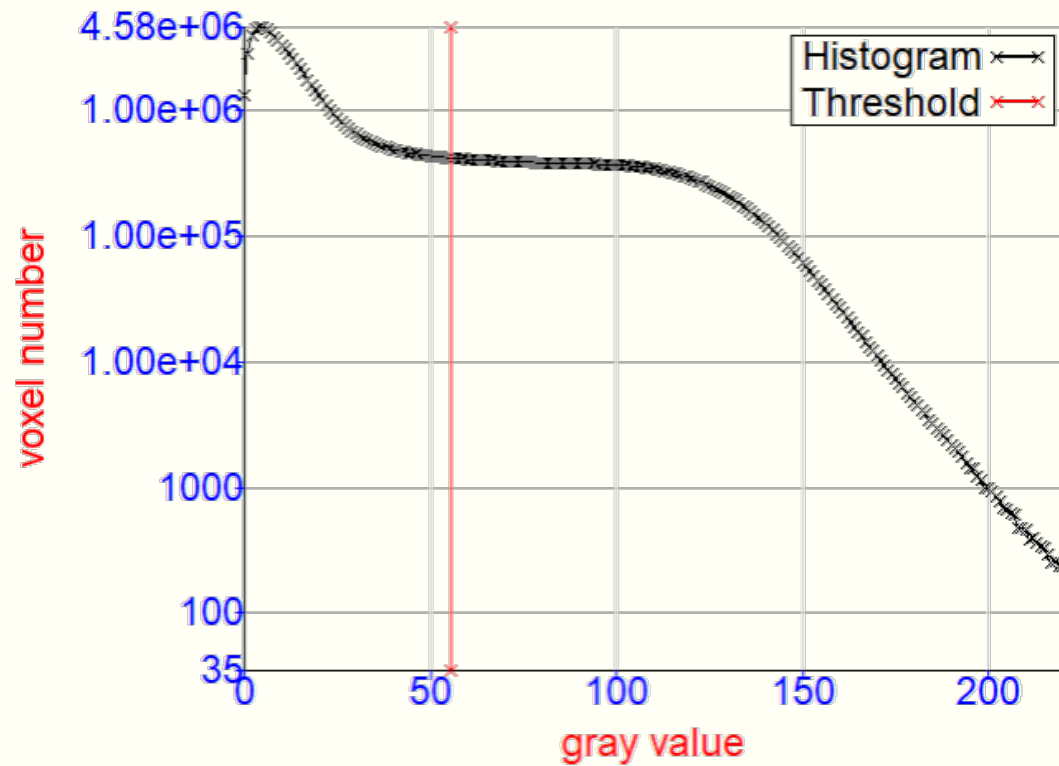
- Import a stack of 2d images
- Image processing to improve quality for segmentation  
(e.g. noise reduction, edge sharpening)



Applying a Non-Local Means Filter for noise reduction

# Import and Segmentation

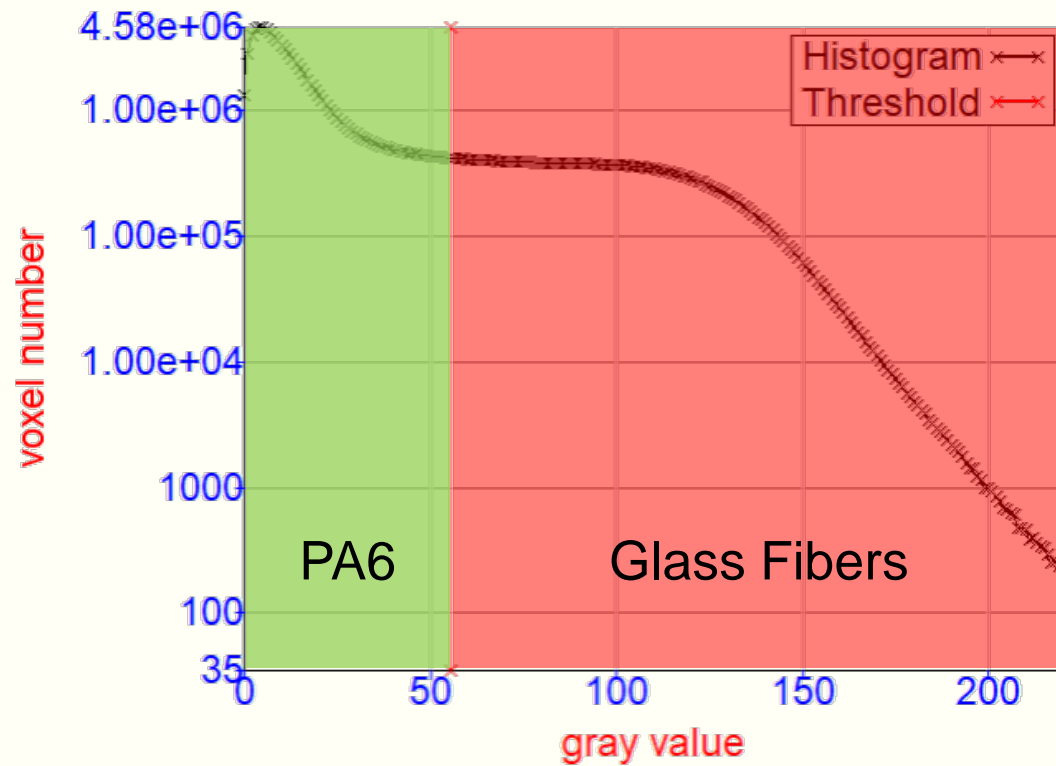
- automated thresholding using OTSU<sup>1</sup> algorithm



<sup>1</sup>Nobuyuki Otsu (1979). "A threshold selection method from gray-level histograms". IEEE Trans. Sys., Man., Cyber. 9 (1): 62–66

# Import and Segmentation

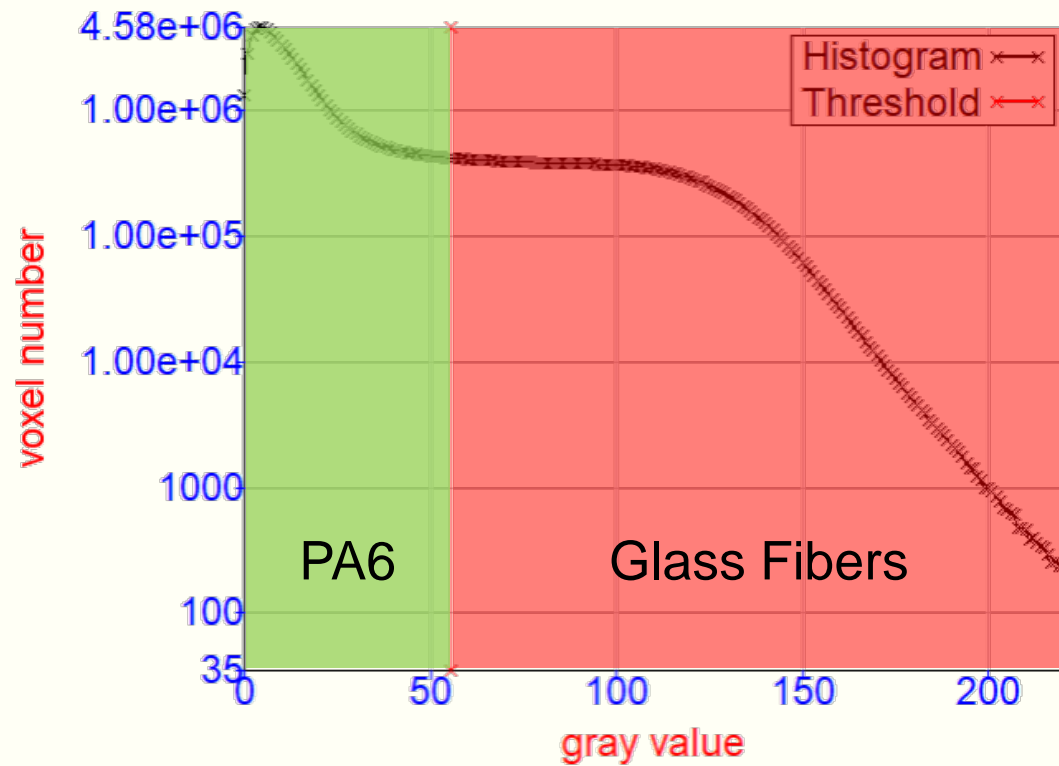
- automated thresholding using OTSU<sup>1</sup> algorithm



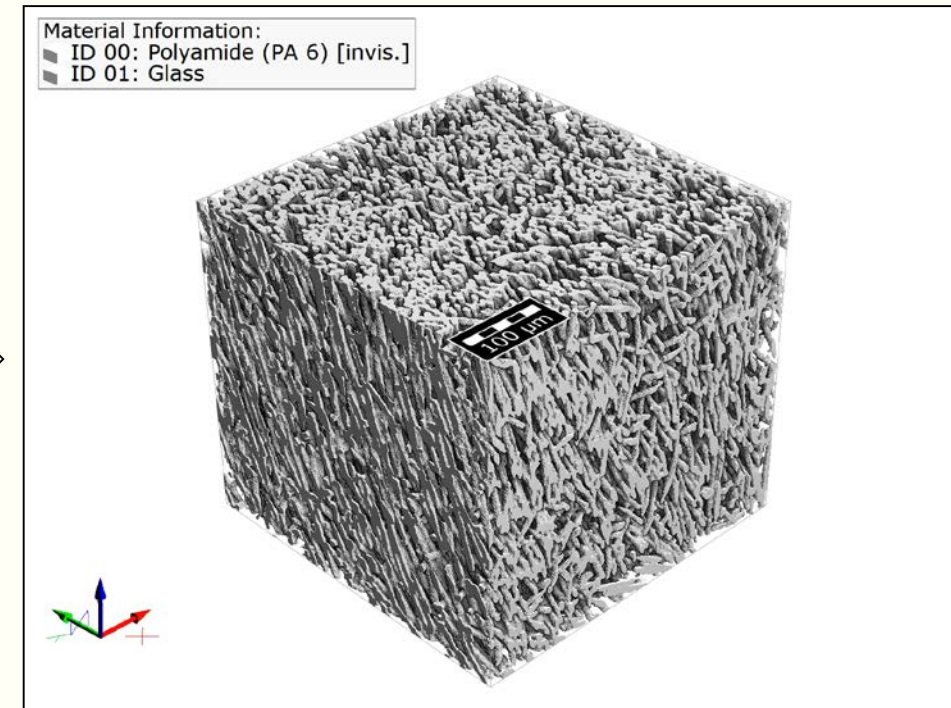
<sup>1</sup>Nobuyuki Otsu (1979). "A threshold selection method from gray-level histograms". IEEE Trans. Sys., Man., Cyber. 9 (1): 62–66

# Import and Segmentation

- automated thresholding using OTSU<sup>1</sup> algorithm



segmentation



<sup>1</sup>Nobuyuki Otsu (1979). "A threshold selection method from gray-level histograms". IEEE Trans. Sys., Man., Cyber. 9 (1): 62–66

# Mechanical Analysis - $\mu$ CT scan

- linear elastic simulation of 6 different load cases
  - 3 uniaxial experiments
  - 3 shear experiments

- used material properties
  - PA6:  $E=2.8$  GPa /  $\nu=0.39$
  - Glass:  $E=72$  GPa /  $\nu=0.22$

$$C_{\alpha\beta} = \begin{bmatrix} C_{11} & C_{12} & C_{13} & C_{14} & C_{15} & C_{16} \\ C_{12} & C_{22} & C_{23} & C_{24} & C_{25} & C_{26} \\ C_{13} & C_{23} & C_{33} & C_{34} & C_{35} & C_{36} \\ C_{14} & C_{24} & C_{34} & C_{44} & C_{45} & C_{46} \\ C_{15} & C_{25} & C_{35} & C_{45} & C_{55} & C_{56} \\ C_{16} & C_{26} & C_{36} & C_{46} & C_{56} & C_{66} \end{bmatrix}$$

- computation time: 589 s
  - 4 CPUs
  - 0.5 GB memory

# Mechanical Analysis - $\mu$ CT scan

- calculated engineering parameters and stiffness tensor

## Orthotropic Approximation

	Strain Equivalence	Energy Equivalence	Mean Value
Young's Modulus $E_1$ / (GPa)	7.1211	7.1213	7.1212 $\pm$ 0.0001
Young's Modulus $E_2$ / (GPa)	7.9283	7.9285	7.9284 $\pm$ 0.0001
Young's Modulus $E_3$ / (GPa)	11.3851	11.3852	11.3852 $\pm$ 0.0000
Poisson Ratio $V_{12}$	0.3547	0.3547	0.3547 $\pm$ 0.0000
Poisson Ratio $V_{13}$	0.2160	0.2160	0.2160 $\pm$ 0.0000
Poisson Ratio $V_{23}$	0.2517	0.2517	0.2517 $\pm$ 0.0000
Poisson Ratio $V_{21}$	0.3949	0.3949	0.3949 $\pm$ 0.0000
Poisson Ratio $V_{31}$	0.3454	0.3454	0.3454 $\pm$ 0.0000
Poisson Ratio $V_{32}$	0.3614	0.3614	0.3614 $\pm$ 0.0000
Shear Modulus $G_{12}$ / (GPa)	2.7558	2.7557	2.7558 $\pm$ 0.0001
Shear Modulus $G_{13}$ / (GPa)	3.0113	3.0111	3.0112 $\pm$ 0.0001
Shear Modulus $G_{23}$ / (GPa)	3.8636	3.8635	3.8636 $\pm$ 0.0001

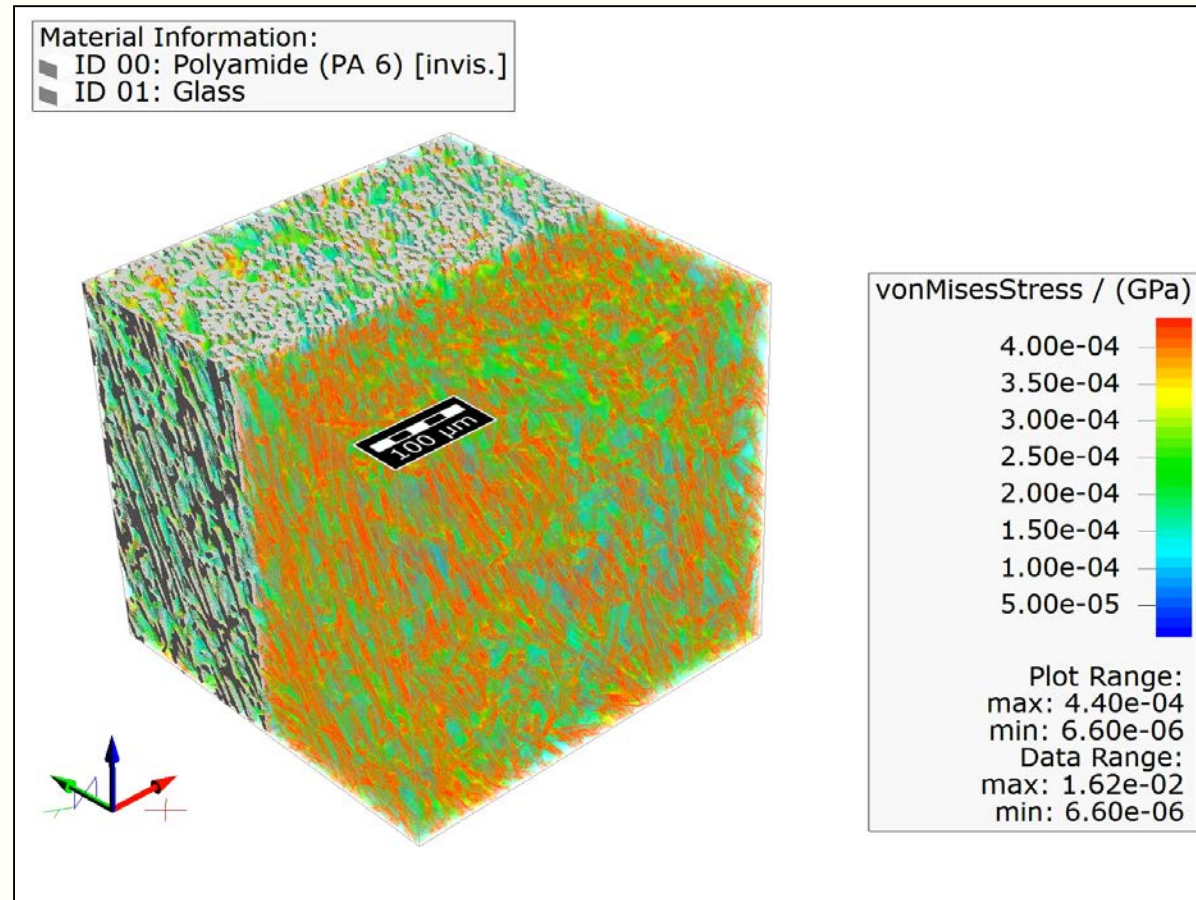
## ----- Anisotropic Elasticity Tensor -----

### Stiffness Formulation for Strain Equivalence / (GPa)

<b>10.232</b>	<b>5.4243</b>	<b>5.4948</b>	0.025524	-0.010267	0.14141
<b>5.4244</b>	<b>11.597</b>	<b>6.0651</b>	0.80216	-0.08876	0.12121
<b>5.4949</b>	<b>6.0652</b>	<b>15.475</b>	1.5932	-0.28255	-0.12848
0.025595	0.80212	1.5932	<b>3.8636</b>	-0.24775	-0.17071
-0.010275	-0.088766	-0.28258	-0.24774	<b>3.0113</b>	0.091551
0.14133	0.12119	-0.12859	-0.17072	0.091522	<b>2.7558</b>

# Mechanical Analysis - $\mu$ CT scan

- visualization of the von-Mises stress



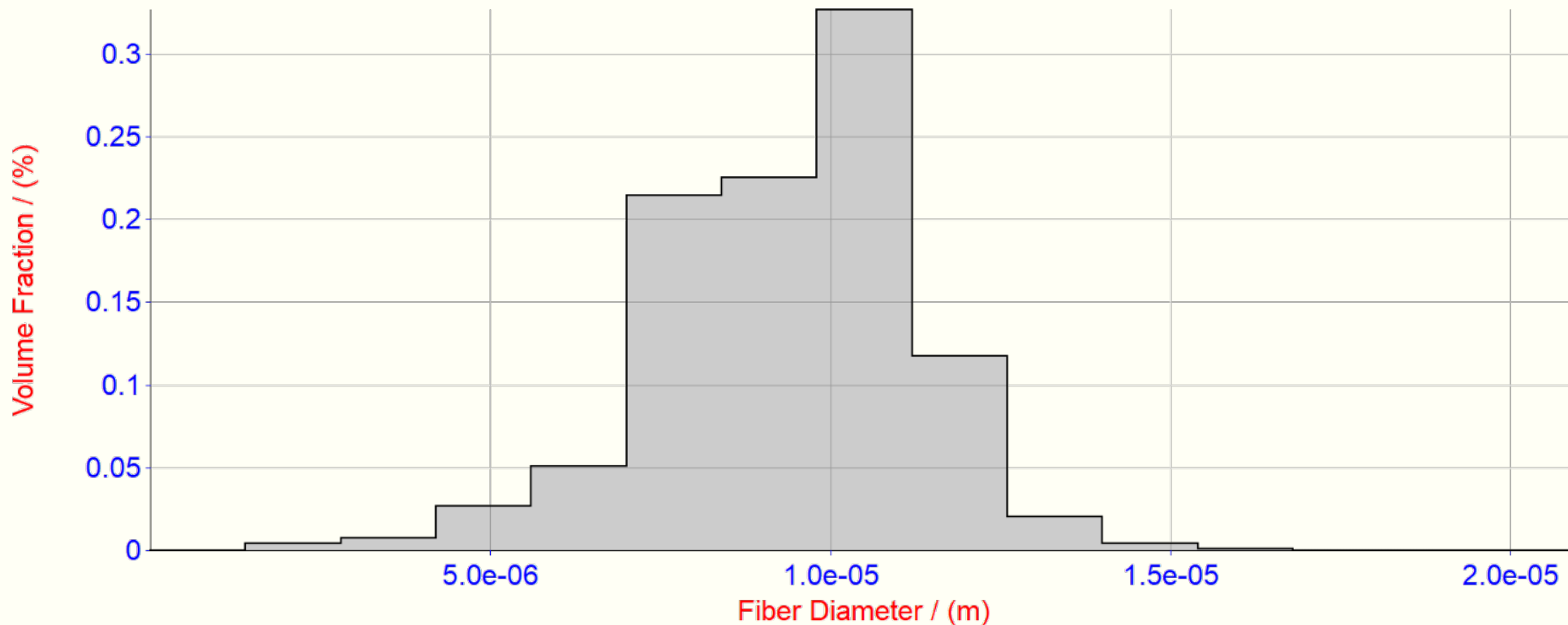
# Modeling the Digital Twin

# Digital Twin – Geometrical Analysis of $\mu$ CT-Scan

- fiber diameter distribution

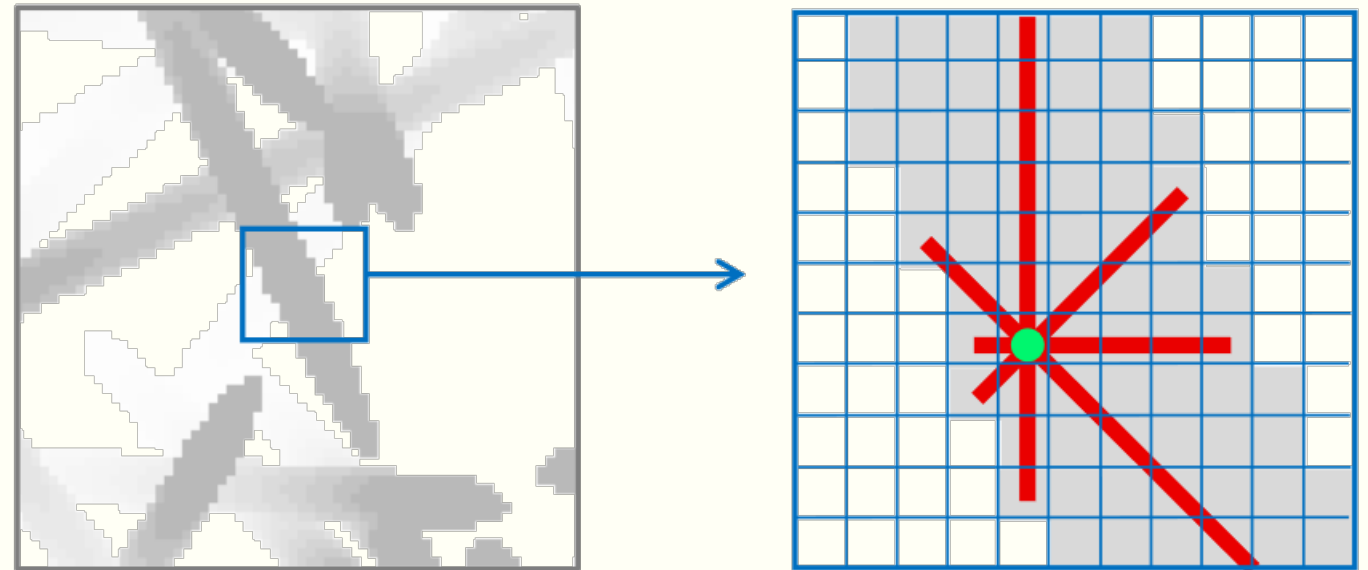
**Average fiber diameter:  $9.38167e-06$  m**

**Standard deviation:  $1.95088e-06$  m**



# Digital Twin – Geometrical Analysis of $\mu$ CT-Scan

- fiber orientation analysis
  - using Star Length Distribution Algorithm
  - works on a per-voxel basis
  - analyzes the chord lengths through the voxel for a pre-defined set of directions
  - the relative length of the cords gives the per-voxel orientation tensor
  - tensors are averaged

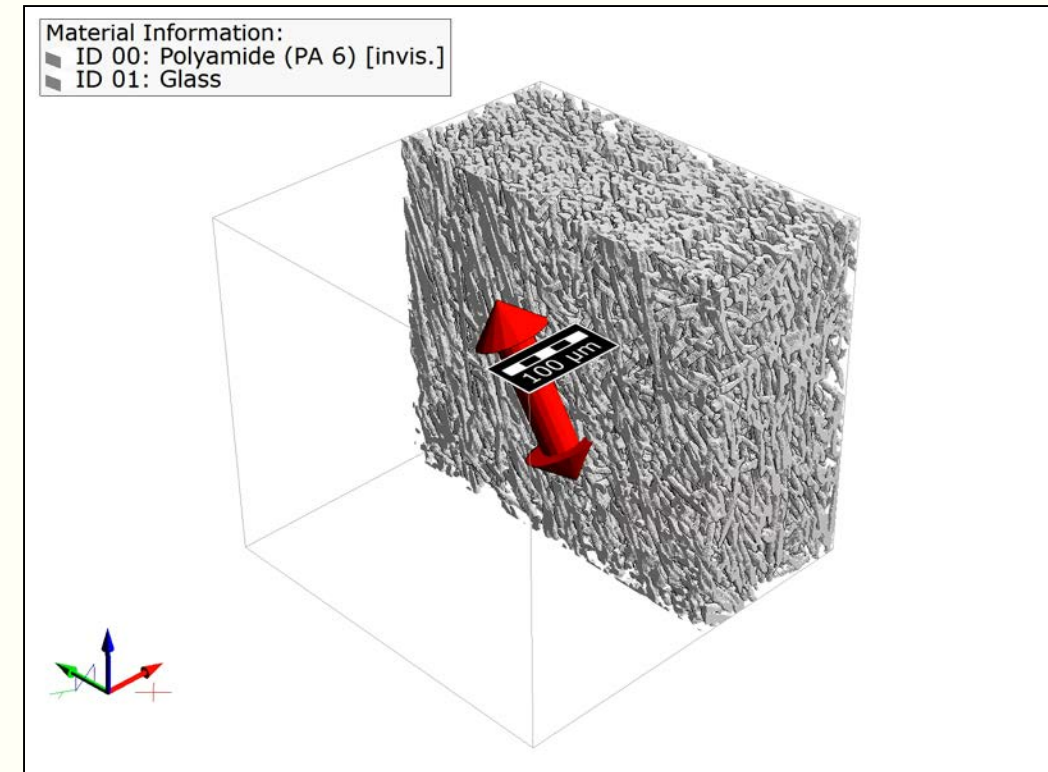


# Digital Twin – Geometrical Analysis of $\mu$ CT-Scan

- fiber orientation analysis
  - homogenized orientation tensor for the entire scan
  - visualization of the main orientation
- calculation of the fiber volume fraction

**Block 0,0,0: Solid Volume Fraction = 30.9137%**

0.165335	-0.0166808	-0.0524757
-	0.289308	0.155508
-	-	0.545357



# Digital Twin – Modelling

- use all collected geometrical properties of the material for modelling the digital twin in **FiberGeo**

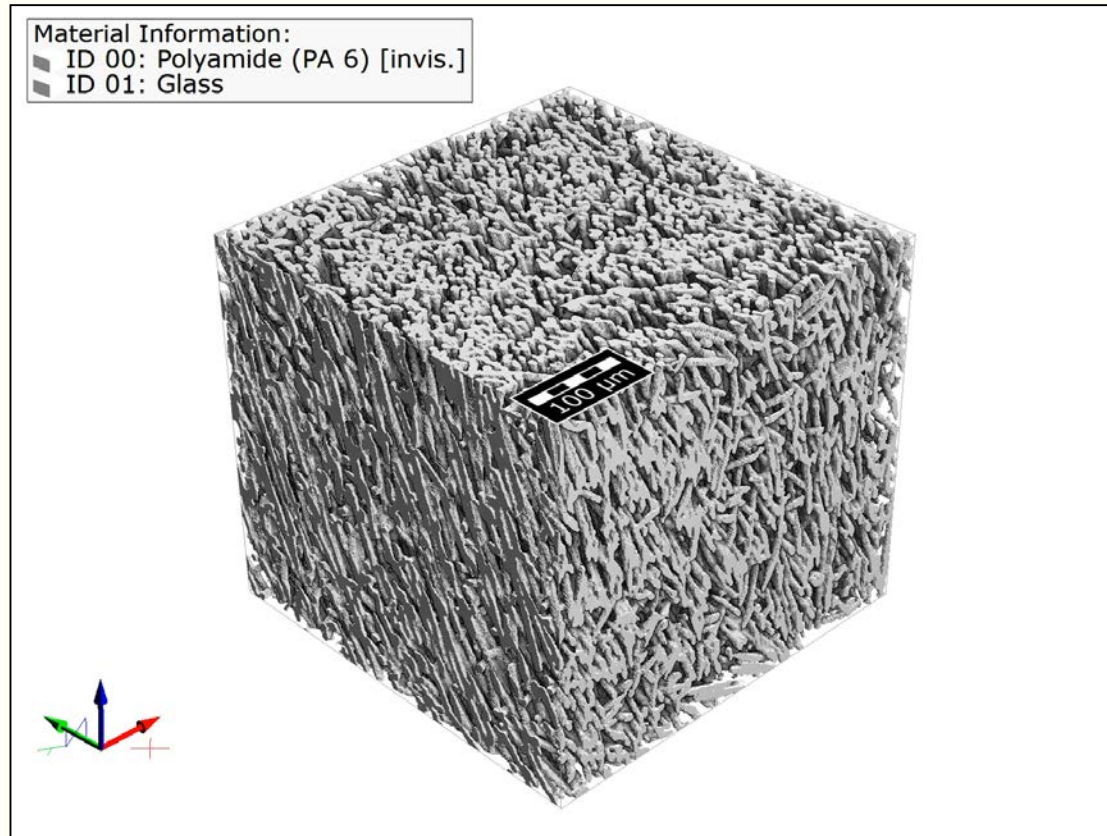
The screenshot displays the GEO-DICT software interface with four dialog boxes open, each with red boxes highlighting specific parameters:

- Main Interface:** Shows the 'DigitalTwin.gdr' result file name and 'Voxel Length / (μm)' set to 1.4.
- Orientation Dialog:** Shows 'Anisotropic Orientation' selected, 'Orientation Mode' set to 'Orientation Tensor', and a 3x3 orientation tensor matrix:

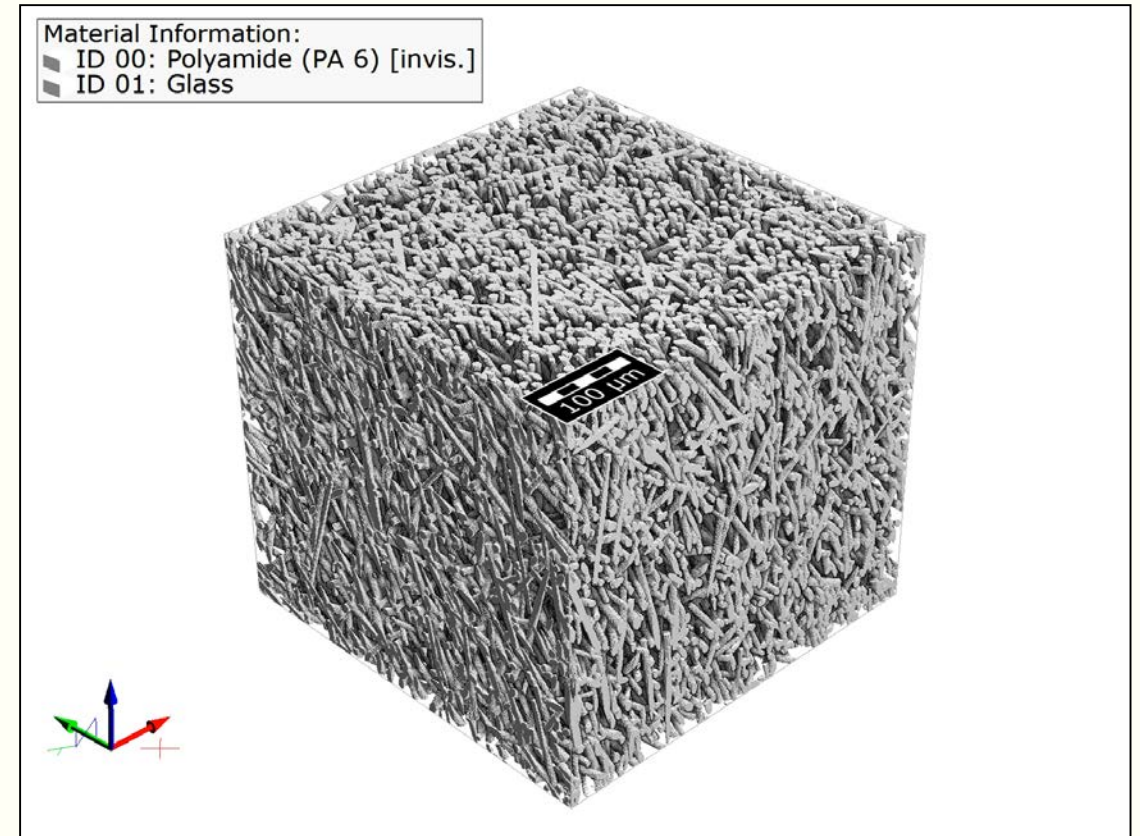
0.165335	-0.0166808	-0.0524757
0.0	0.289308	0.155508
0.0	0.0	0.545357
- Length / (μm) Dialog:** Shows 'Uniformly in interval' selected, with 'Minimum / (μm)' set to 150 and 'Maximum / (μm)' set to 250.
- Diameter / (μm) Dialog:** Shows 'Gaussian' selected, with 'Mean Value / (μm)' set to 9.38167, 'Standard Deviation / (μm)' set to 1.95088, and 'Distribution Bound / (μm)' set to 5.

# Digital Twin – Modelling

- visual comparison of the twin and the  $\mu$ CT-scan



$\mu$ CT-Scan



Digital Twin

# Digital Twin – Mechanical Analysis

- comparison of the stiffness tensor

----- Anisotropic Elasticity Tensor -----

Stiffness Formulation for Strain Equivalence / (GPa)

10.232	5.4243	5.4948	0.025524	-0.010267	0.14141
5.4244	11.597	6.0651	0.80216	-0.08876	0.12121
5.4949	6.0652	15.475	1.5932	-0.28255	-0.12848
0.025595	0.80212	1.5932	3.8636	-0.24775	-0.17071
-0.010275	-0.088766	-0.28258	-0.24774	3.0113	0.091551
0.14133	0.12119	-0.12859	-0.17072	0.091522	2.7558

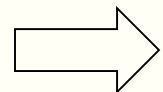
μCT-Scan

----- Anisotropic Elasticity Tensor -----

Stiffness Formulation for Strain Equivalence / (GPa)

10.757	5.4859	5.5878	0.053966	0.06989	0.16679
5.4859	11.688	6.0427	0.78271	-0.070062	0.16912
5.5879	6.0427	14.307	1.1605	-0.031768	-0.05373
0.054045	0.78275	1.1605	3.6667	-0.15612	-0.11499
0.069986	-0.069923	-0.031719	-0.15614	3.1619	0.081569
0.16684	0.16916	-0.053757	-0.11499	0.081581	2.9358

Digital Twin

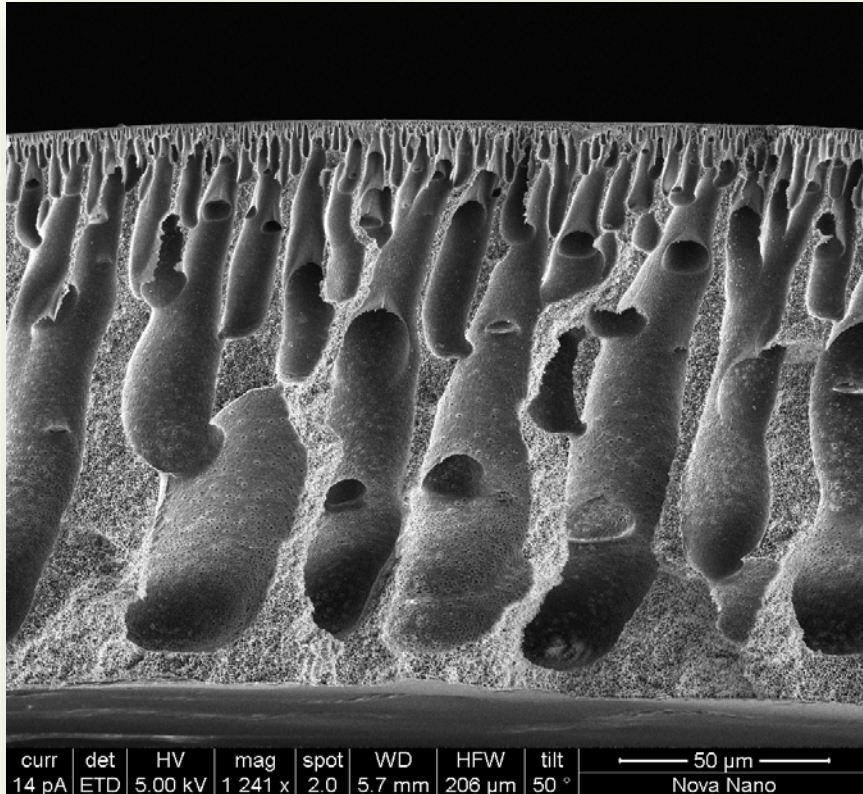


very good agreement between μCT-scan and digital twin

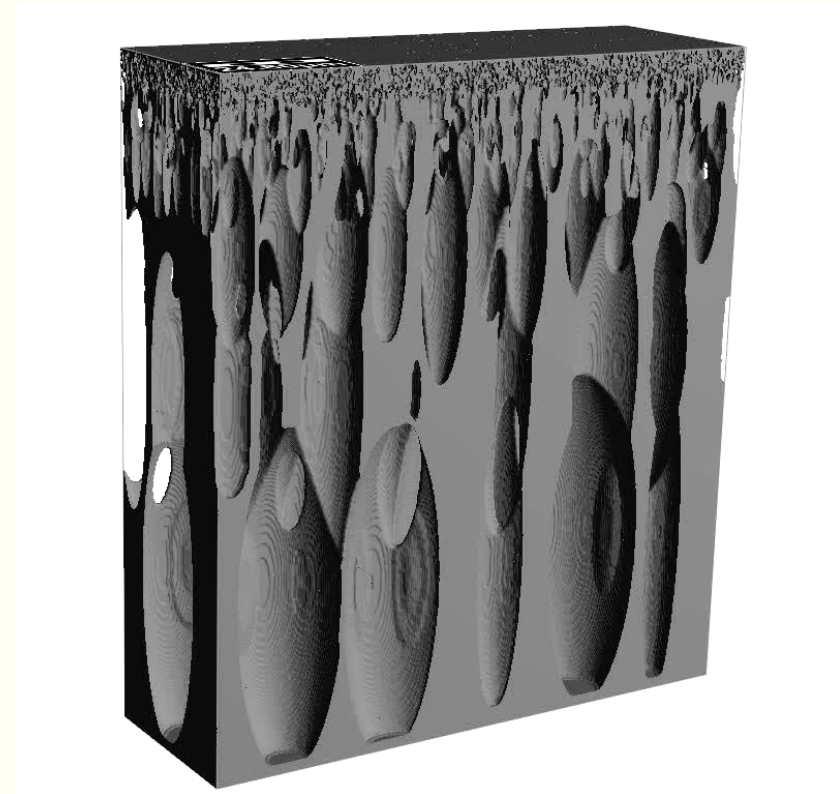
# Digital Twin – Some Examples

# Digital Twin – Polysulfone micromembrane

- used for seawater desalination



SEM image

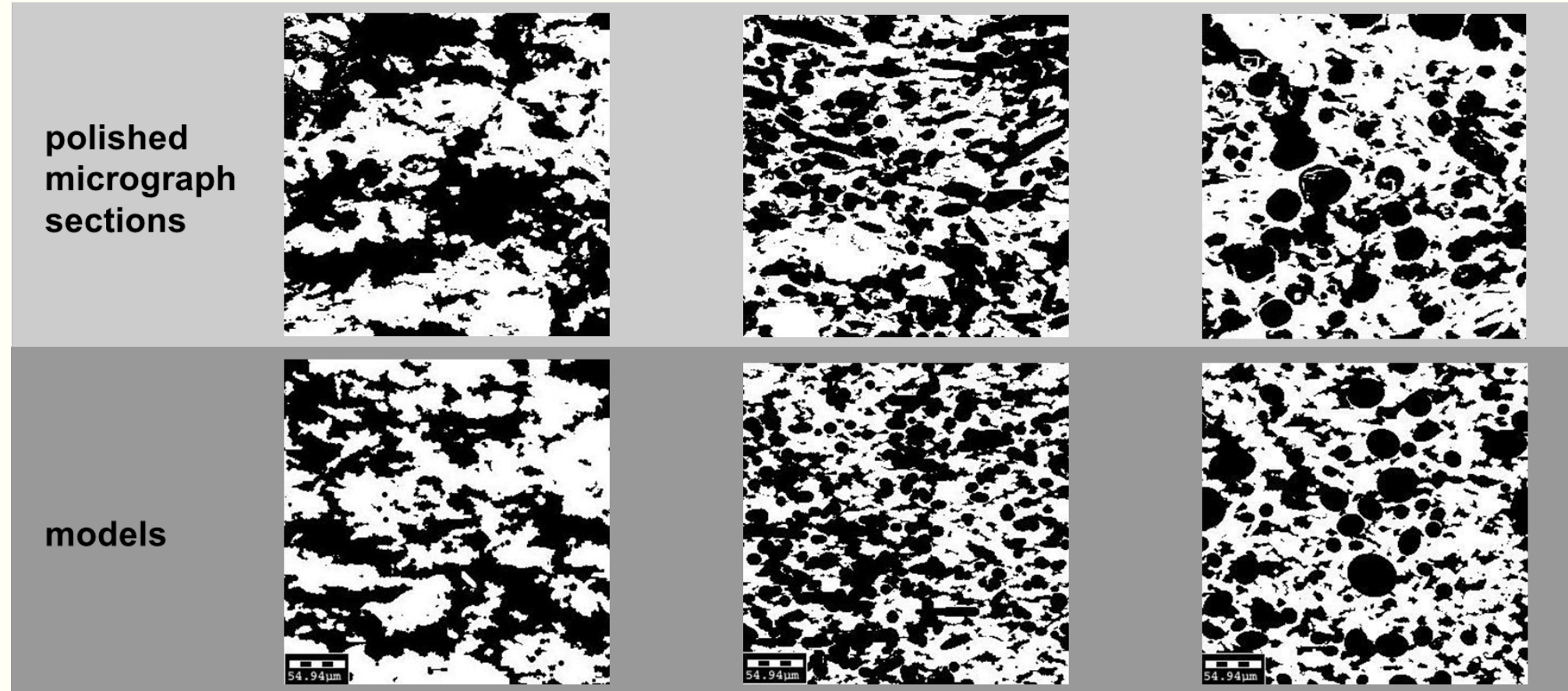


Digital Twin

[Shi et al., Water flow prediction for Membranes using 3D simulations with detailed morphology, 2015, Journal of Membrane Science]

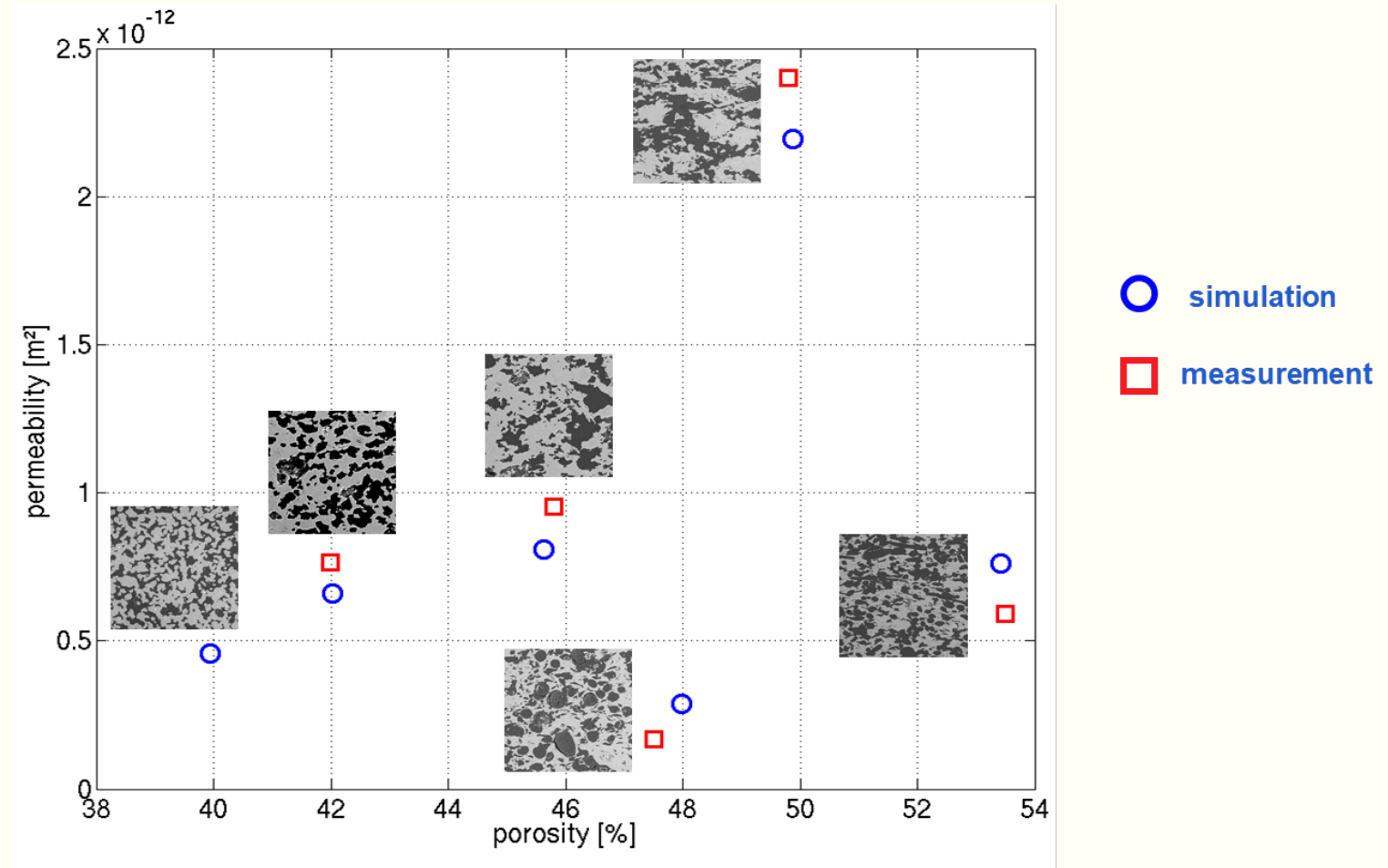
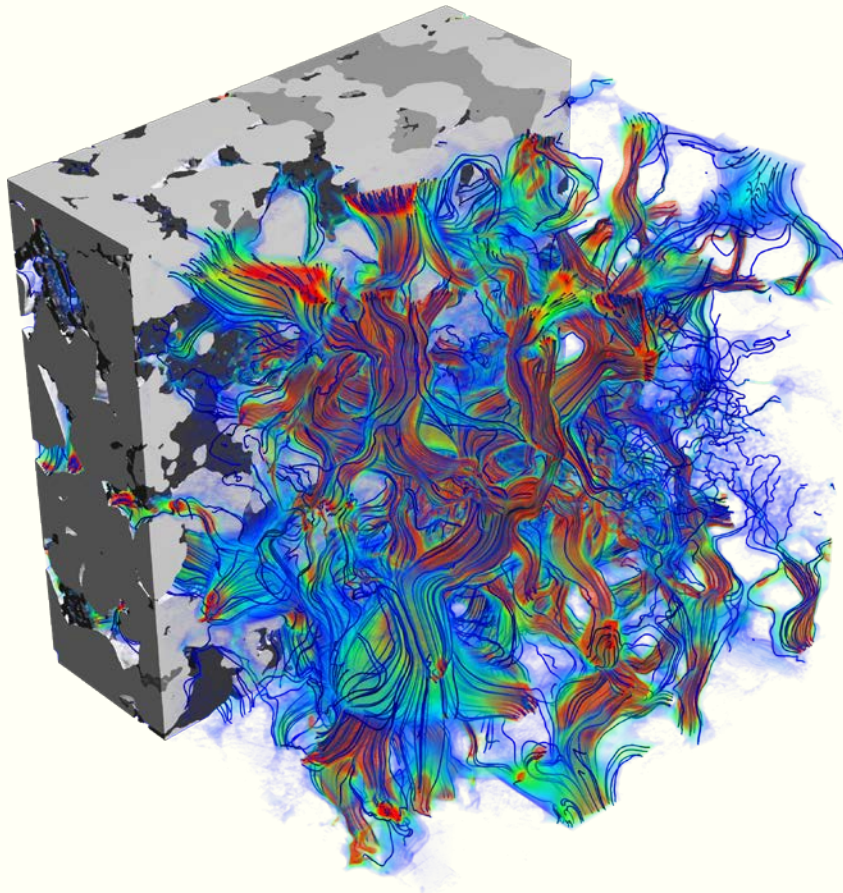
# Digital Twin – Sintered Ceramic

- used for soot particle filters



[Schmidt and Becker, Generating Validated 3D Models of Microporous Ceramics, 2013, Advanced Engineering Materials]

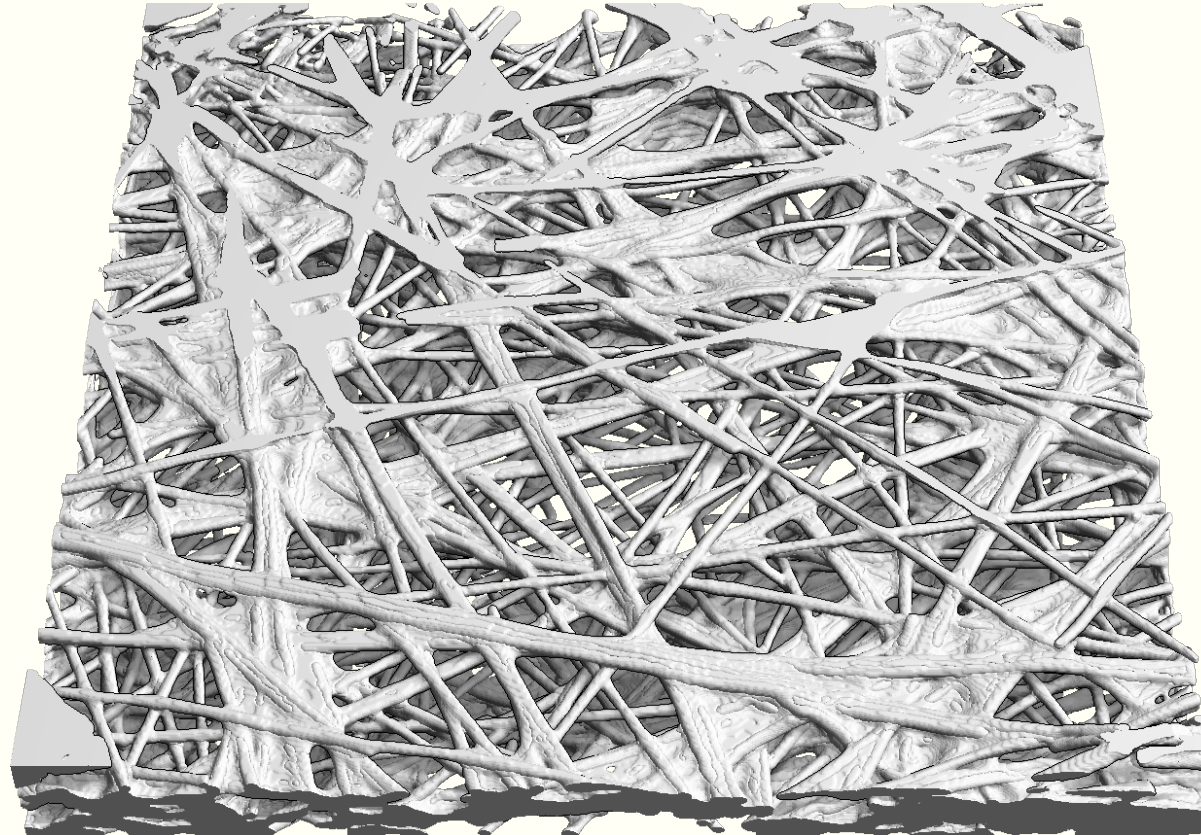
# Digital Twin – Sintered Ceramic



[Schmidt and Becker, Generating Validated 3D Models of Microporous Ceramics, 2013, Advanced Engineering Materials]

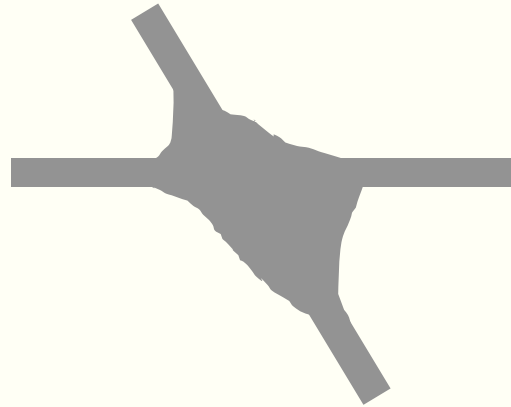
# Digital Twin – Gas Diffusion Layer

- used in fuel cells

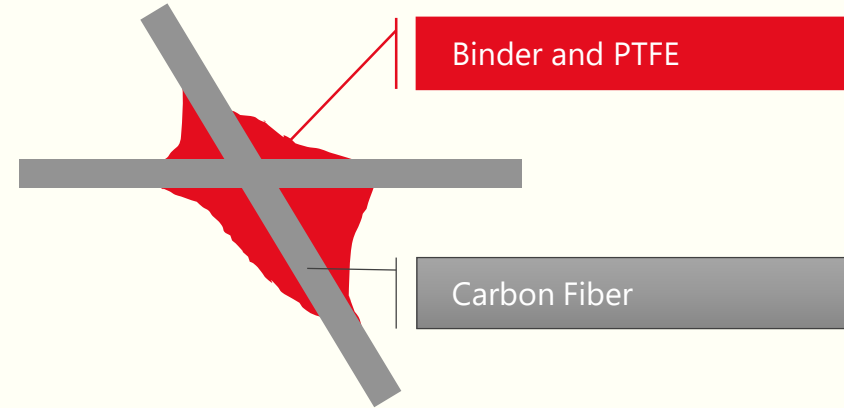


$\mu$ CT-Scan

# Digital Twin – Gas Diffusion Layer

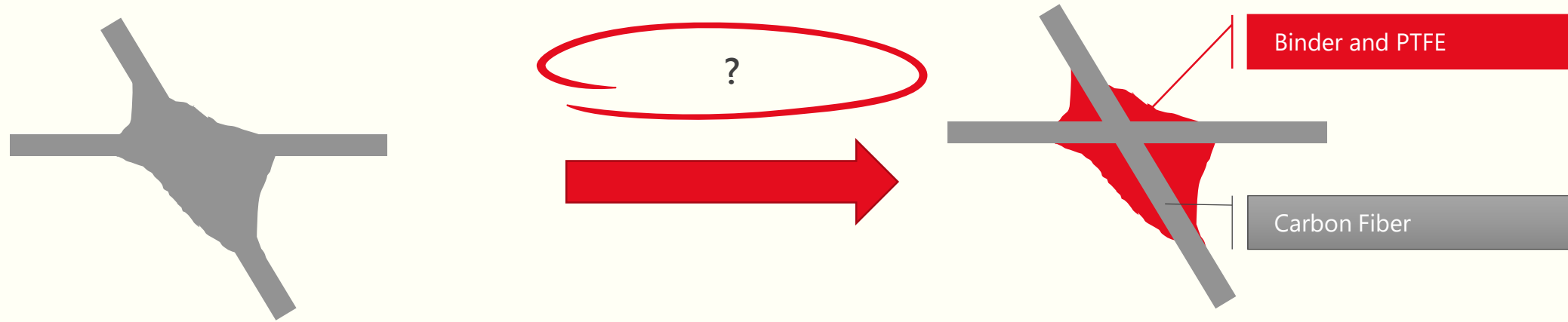


In the original CT Scan binder and fiber can not be separated

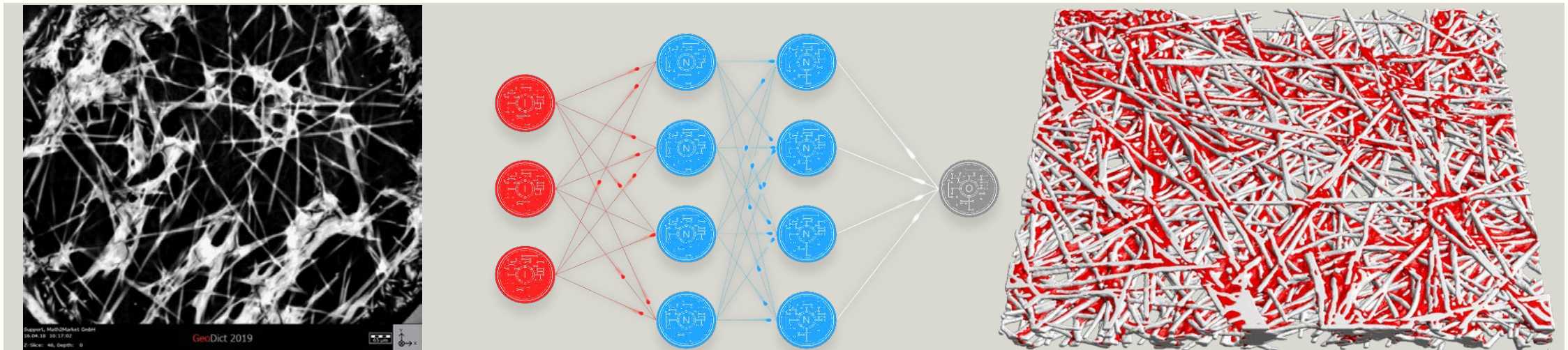


It is necessary to differentiate fibers from binder based on the shape

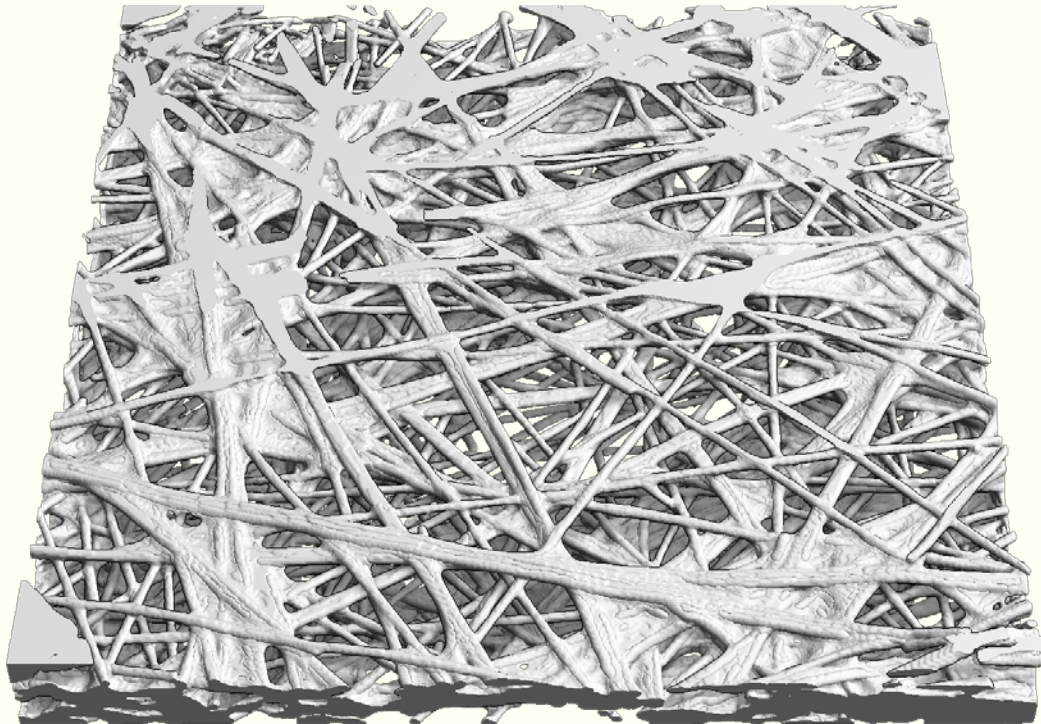
# Digital Twin – Gas Diffusion Layer



## Identifying binder with Machine Learning



# Digital Twin – Gas Diffusion Layer



μCT-Scan



Fibers: 16.2%  
Binder: 13.2%

segmented image

# Thank You!

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